Complete collision data set for electrons scattering on molecular hydrogen and its isotopologues

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Overview

• MCCC method : fixed-nuclei (FN) approach

Cross sections obtained with the FN MCCC method

• MCCC method : adiabatic nuclei (AN) approach

Vibrationally-resolved cross sections from AN MCCC Accessing MCCC collision data: MCCC database

- Example: modeling Collisional Radiative Model for H₂
- Scattering from the excited states ($n=2: a {}^{3}\Sigma_{g}^{+}, c {}^{3}\Pi_{u},...$)
- Isotopic and vibrational-level dependence of H₂ dissociation by electron impact
- Conclusions



MCCC method: fixed-nuclei (FN) approach

- Born-Oppenheimer approximation
- Fixed-nuclei approximation, R = fixed
- Diagonalization of the target Hamiltonian H_T in a Sturmian (Laguerre) basis

Solve for the electronic wave function

modeling of *infinite* number of bound & continuum states with a *finite* number of pseudostates

$$\langle \phi_f | H_T | \phi_i \rangle = \varepsilon_f \delta_{fi}$$

$$\Psi_i^{(+)}(\mathbf{x}_p, \mathbf{x}_t) = \mathcal{A} \sum_{n=1}^N F_n(\mathbf{x}_p) \phi_n(\mathbf{x}_t)$$

- Solve integral LS equation for the *T* matrix
- Cross sections

 $T_{fi}(\vec{k}_{f},\vec{k}_{i}) = V_{fi}(\vec{k}_{f},\vec{k}_{i}) + \sum_{n=1}^{N} \int d^{3}k \frac{V_{fn}(\vec{k}_{f},\vec{k})T_{ni}(\vec{k},\vec{k}_{i})}{E + i0 - \varepsilon_{n} - k^{2}/2}$ $\sigma_{fi}(R) \propto \left|T_{fi}(R)\right|^{2}$

Why electron-molecule is difficult: no central potential

→ multi-channel expansion + projectile partial wave expansion lead to a very large size of coupled equations, to solve need fast computers, effective parallelization, etc....

Cross sections for electron scattering from H₂ FN single-centre spherical coordinate MCCC approach

Established convergence in cross sections by performing: 491, 427, 259, 92, 9-state close-coupling

- total cross section, total ionization cross section, stopping power
- elastic scattering (ICS, DCS)
- excitation cross sections (ICS, DCS) for
 - $b \, {}^{3}\Sigma_{u}{}^{+}$, $a \, {}^{3}\Sigma_{g}{}^{+}$, $c \, {}^{3}\Pi_{u}$, $e \, {}^{3}\Sigma_{u}{}^{+}$, $h \, {}^{3}\Sigma_{g}{}^{+}$, $d \, {}^{3}\Pi_{u}$, $i \, {}^{3}\Pi_{g}$, $j \, {}^{3}\Delta_{u}$
 - $B^{1}\Sigma_{u}^{+}, C^{1}\Pi_{u}, EF^{1}\Sigma_{g}^{+}, B^{'1}\Sigma_{u}^{+}, D^{1}\Pi_{u}, B^{''1}\Sigma_{u}^{+}, D^{'1}\Pi_{u}, H^{1}\Sigma_{g}^{+}, GK^{1}\Sigma_{g}^{+}, I^{1}\Pi_{u}, J^{1}\Delta_{g}^{-}$

Scarlett *et al.*, Phys. Rev. A **96** (2017) 062708 Zammit *et al.*, Phys. Rev. A **95** (2017) 022708 Zammit *et al.*, Phys. Rev. Lett. **116** (2016) 233201

Often found large disagreement with previous experimental and theoretical results



Cross sections for the b ${}^{3}\Sigma_{u}^{+}$ state





Cross sections for the b ${}^{3}\Sigma_{u}^{+}$ state

New time of flight (TOF) spectrometer at California State University, Fullerton





UKRMol+ and MCCC calculations: good agreement



ICS

Meltzer et al., J. Phys. B. 53 (2020) 145204





Energy (eV)

MCCC method: adiabatic nuclei (AN) approach



AN T matrix

$$T_{f\mu,i\nu}(E) = \int dR \ \varphi_{f\mu}(R) T_{fi}(E;R) \ \varphi_{i\nu}(R)$$

- $\varphi_{n\mu}(R)$ are vibrational wave functions
- vibrationally-resolved cross sections

$$\sigma_{f\mu,i\nu}(E) \propto \left| T_{f\mu,i\nu}(E) \right|^2$$

- computationally expensive (many *R*)
- need high accuracy of FN model at large R

Single-center spherical-coordinate formulation is inadequate \downarrow Spheroidal-coordinate formulation of the MCCC method Many FN calculations have to be performed on a grid of *R* Computationally efficient / feasible approach is required



MCCC method: spheroidal coordinate formulation





MCCC(210) fully vibrationally resolved cross sections

Calculations have been performed for over 58,000 transitions in H₂ and its 5 isotopologues includes dissociation cross sections





Number of bound vibrational levels

Accessing MCCC data

All cross sections and fits available online

Atom. Data Nucl. Data Tables supplementary materials

Complete collision data set for electrons scattering on molecular hydrogen and its isotopologues:

I. Fully vibrationally-resolved electronic excitation of $H_2(X^{1}\Sigma_{q}^{+})$

Atomic Data and Nuclear Data Tables 137 (2021) 101361

II. Fully vibrationally-resolved electronic excitation of the isotopologues of H_2(X $^1\Sigma_g{}^+)$

Atomic Data and Nuclear Data Tables 139 (2021) 101403

- LXCat Database Ixcat.net
- IAEA hcdb: Atomic and Molecular Data for Fusion Energy Research https://db-amdis.org/hcdb/
- MCCC Database mccc-db.org

TABASE	ê mece-da ung 🔿	å Ø
	Electron-molecule scattering cross sections calculated using the Molecular Convergent Close-Coupling method	
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	projectile 💌	
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MCCC D



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MCCC DATABASE cattering sys Home Reference: Scarlett et al. Atom. Data Nucl. Data Tables 73, 101361 (2021) electron Database H2 Contact Plot Data file Fit parameters 0.12 Display data 0.1 - Select initial state section (a₀²) + 4 Ŧ X1Sg 0.08 excitation - Select final state v Dissociativ... v Bp1Su Integrated cross 0.06 0.04 Download data - Select initial state -0.02 electronic vibrational v collision process 0 50 100 150 200 250 300 350 400 450 500 0 Incident electron energy (eV) Change to log x scale Change to log y scale

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Dissociative excitation

Tapley et al., Phys. Rev. A 98 (2018) 032701

B' ${}^{1}\Sigma_{u}^{+}$ state has the largest DE cross section for scattering on v = 0 ground state $X {}^{1}\Sigma_{q}^{+}$

exp.: Liu et. al, J. Phys B 45 (2012)
IP: semiclassical impact-parameter method – Bari group Celiberto et al., Atom. Data Nucl. Data Tables 77 (2001) 161
FBA: Borges et al., Phys. Rev. A 57 (1998) 1025



2.0

0.0

10

 $C^{1}\Pi_{\mu}$



CCC-S(210)

 \odot

100

Incident energy (eV)

 \odot

CC(27

Liu *et al.* Borges *et al.* Celiberto *et al.*

0

Collisions data & plasma physics applications: Janev & Miles comparisons

 \rightarrow

Miles, Thompson, Green, J. App. Phys. **43** (1972) 678; Janev, Reiter, Samm, JÜL-4105, Jülich, 2003



used by Ursel Fantz & Dirk Wuenderlich (Garching) in their CR model





J. Phys. D: Appl. Phys. 54 (2021) 115201 (12pp)

Application of molecular convergent close-coupling cross sections in a collisional radiative model for the triplet system of molecular hydrogen

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depending on the collision dataset used

Significant differences in the simulation results

Further improvements:

- more accurate account of cascading from high level states
- use of vibrationally resolved cross sections
- use of rotationally resolved cross sections

Comparison of measured population densities of the d^3 state to the ones calculated with the CR model Yacora H₂ using cross section from either Miles et al. [25], Janev et al. [21] or the MCCC data.



³ Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87545, United States of America

Vertical excitation energies at R = 2

		Energ	Energy (Ha)		ΔE (eV)	
State	R _m	Present	Ref.	Present	Ref.	
		avarrel	n = 1	National States	1000000	
$X^{-1}\Sigma_{o}^{+}$	1.448	-1.1360	-1.1381ª	-10.86	-10.90	
$b^3 \Sigma_{\mu}^+$		-0.8967	-0.8971 ^b	-4.347	-4.344	
			n = 2			
$B^1\Sigma_{\mu}^+$	2.518	-0.7503	-0.7521°	-0.364	-0.397	
$c^3\Pi_{\mu}$	2.022	-0.7369	-0.7375 ^b			
$a^3\Sigma_{o}^+$	1.928	-0.7357	-0.7361 ^b	0.032	0.037	
$C^{1}\Pi_{\mu}^{s}$	2.016	-0.7177	-0.7182 ^d	0.523	0.5237	
$EF^{1}\Sigma_{o}^{+}$	1.978	-0.7172	-0.7177 ^e	0.536	0.538	
8			n = 3			
$e^{3}\Sigma_{\mu}^{+}$		-0.6831	-0.6832 ^b	1.465	1.478	
$B'^{1}\Sigma_{\mu}^{+}$		-0.6650	-0.6655°	1.957	1.959	
$d^3 \Pi_{\mu}$		-0.6606	-0.6607^{b}	2.077	2.089	
$h^3 \Sigma_o^+$		-0.6602	-0.6606^{b}	2.088	2.093	
$GK^{1}\Sigma_{o}^{+}$		-0.6599	-0.6604^{e}	2.095	2.097	
$g^{3}\Sigma_{a}^{+}$		-0.6595	-0.6598 ^b	2.106	2.113	
i ³ ∏.		-0.6592	-0.6596 ^b	2.115	2.120	
$I^{1}\Pi_{e}$		-0.6591	-0.6595^{f}	2.117	2.121	
$i^{3}\Delta_{e}$		-0.6574	-0.6576 ^f	2.164	2.173	
$J^1 \Delta_{\varrho}$		-0.6573	-0.6576^{f}	2.166	2.174	
$D^1\Pi_{\mu}$		-0.6551	-0.6553 ^d	2.226	2.235	
$H^1\Sigma_{e}^+$		-0.6547	-0.6549e	2.238	2.246	



Excitation energies are relative to the $c {}^{3}\Pi_{u}$ state

Example: the $c {}^{3}\Pi_{u}(v=0)$ state

it is a metastable state it is lower than $a {}^{3}\Sigma_{g}^{+}(v=0)$ state by 0.0228 eV $c {}^{3}\Pi_{u} \rightarrow a {}^{3}\Sigma_{g}^{+}$ transition is by far the largest as it is a dipole allowed transition

small excitation energy means:

- (a) large projectile partial wave expansion is required
- (b) Born limit will be reached relatively fast
- (c) target structure accuracy is very important



- Much slower than for scattering on ground state ($L_{max} = 10$)
- Many dipole-allowed transitions unconverged even with $L_{\text{max}} = 25$
- Even with Analytical Born Completion $L_{\text{max}} = 20$ is necessary
- Agreement with recent UKRMol+ calculations $(L_{max} = 6)$ for dipole-forbidden and spin-exchange transitions, but not dipole-allowed transitions



UKRmol+ (FN): Meltzer et al., J. Phys. B 53 (2020) 245203

FBA (FN): Rescigno & Orel (from IEEE Trans. Plasma Sci. PS-11, 266 (1983).)



Partial-wave convergence:







R = 2.0 used in FN UKRMol+ calculations does not accurately model scattering on more diffuse $B^{-1}\Sigma_{u}^{+}$ state (average R = 2.5)





Isotopic and vibrational-level dependence of H₂ dissociation by electron impact

Standard formula to calculate energy-differential cross section for dissociation (used in MCCC):

$$\frac{\mathrm{d}\sigma}{\mathrm{d}E_{\mathrm{out}}} = \frac{\pi}{k_{\mathrm{in}}^2} \sum_{\substack{\ell'm'\\\ell m}} \left| \langle v_{E_k} | T_{\ell'm',\ell m}(R;E_{\mathrm{in}}) | v_v \rangle \right|^2 \quad \bigstar$$
$$E_k = E_{\mathrm{in}} - D_v - E_{\mathrm{out}}$$

Trevisan and Tennyson (J. Phys. B **34** (2001) 2935-2949) derived a different formula:

$$\frac{\mathrm{d}\sigma}{\mathrm{d}E_{\mathrm{out}}} = \frac{m_{\mathrm{H}}}{4\pi^{3}m_{\mathrm{e}}} \frac{E_{\mathrm{i}}}{E_{\mathrm{in}}} \sum_{\substack{\ell'm'\\\ell m}} \left| \langle v_{E_{\mathrm{k}}} | T_{\ell'm',\ell m}(R;E_{\mathrm{in}}) | v_{v} \rangle \right|^{2}$$

- Explicit mass dependence cross sections scale with mass
- Explicit dependence on the energy of the dissociating fragments E_k
- Formula was applied in *R*-matrix calculations of H₂ dissociation cross sections which are widely used in plasma modelling applications

- v_{E_k} energy-normalized continuum vibrational wave functions
- Isotopic dependence only from vibrational wave functions



R-matrix calculations TT02: Trevisan and Tennyson, Plasma Phys. Control. Fusion 44 (2002) 1263-1276, 2217-2230



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R-matrix calculations TT02: Trevisan and Tennyson, Plasma Phys. Control. Fusion 44 (2002) 1263-1276, 2217-2230



Isotopic and vibrational-level dependence of H₂ dissociation by electron impact

Which formula is correct?

9

$$\frac{\mathrm{d}\sigma}{\mathrm{d}E_{\mathrm{out}}} = \frac{\pi}{k_{\mathrm{in}}^2} \sum_{\substack{\ell'm'\\\ell m}} \left| \langle v_{E_k} | T_{\ell'm',\ell m}(R;E_{\mathrm{in}}) | v_v \rangle \right|^2$$

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and G Cartry^{1,•}

- In the paper we show that Trevisan and Tennyson's approach to deriving the dissociation cross section leads to the standard formula
- The differences in their formula are due to errors in the derivation



Curtin University

Conclusions

- Large-scale close-coupling calculations for H_2 : produced a comprehensive dataset of e^-H_2 vibrationally resolved excitation cross sections: from the ground to n=2,3 excited electronic states, isotopically resolved dataset.
- Collisional Radiative Model for the triplet system of molecular hydrogen: using MCCC cross sections
- Produced a set of cross sections for H_2 transitions between electronically excited states
- Identified & resolved a major discrepancy for the isotopic and vibrational-level dependence of H₂ dissociation by electron impact
- In preparation:
 - detailed data set of vibrationally resolved cross sections for H_2 for transitions between electronically excited states, + isotopologues (D₂, HD, ...)
 - rotationally-resolved electron scattering on H_2 + isotopologues (D₂, HD, ...) rovibrationally resolved cross sections polarization of radiation in Fulcher- α band emission (d³ \rightarrow a³)
 - vibrational close-coupling technique with exact account of coupling to electronic degrees of freedom
- Results available from LXCat and IAEA databases and MCCC database (mccc-db.org)

