

Electron scattering on molecules - partial (and total) cross sections: search for uncertainties and errors in experimental procedures

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Data needed:

1. Total cross section
2. Partial cross sections:

elastic scattering $e+A \rightarrow e+A$

rotational excitation $e+CH_4 (J=0) \rightarrow e+CH_4 (J=2)$

vibrational excitation $e+AB(v=0) \rightarrow e+AB(v>0)$

electron attachment (dissociative) $e+AB \rightarrow A^- + B$

electronic excitation $e+A \rightarrow e+A^*$

emission lines: $A^* \rightarrow A + h\nu$

neutral dissociation $e+AB \rightarrow A + B + e$

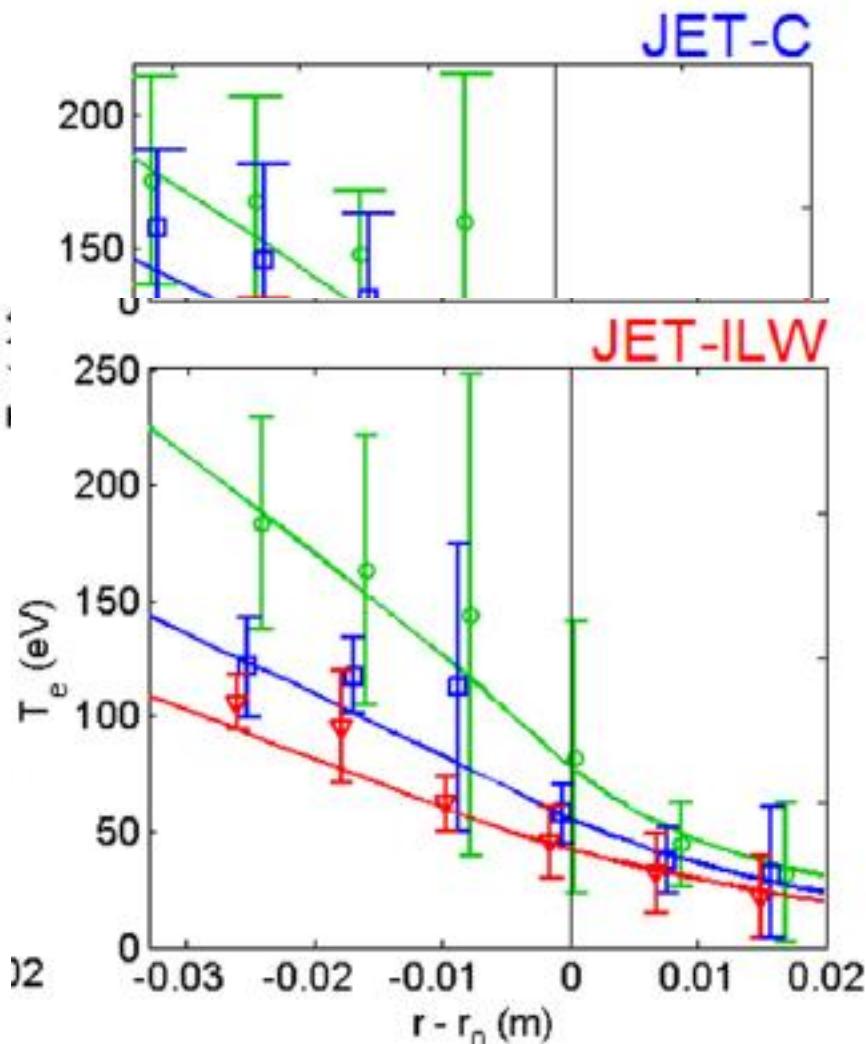
emission from dissociation $e + AB \rightarrow A^* + B + e + h\nu$

ionization $e+A \rightarrow A^+ + 2e$

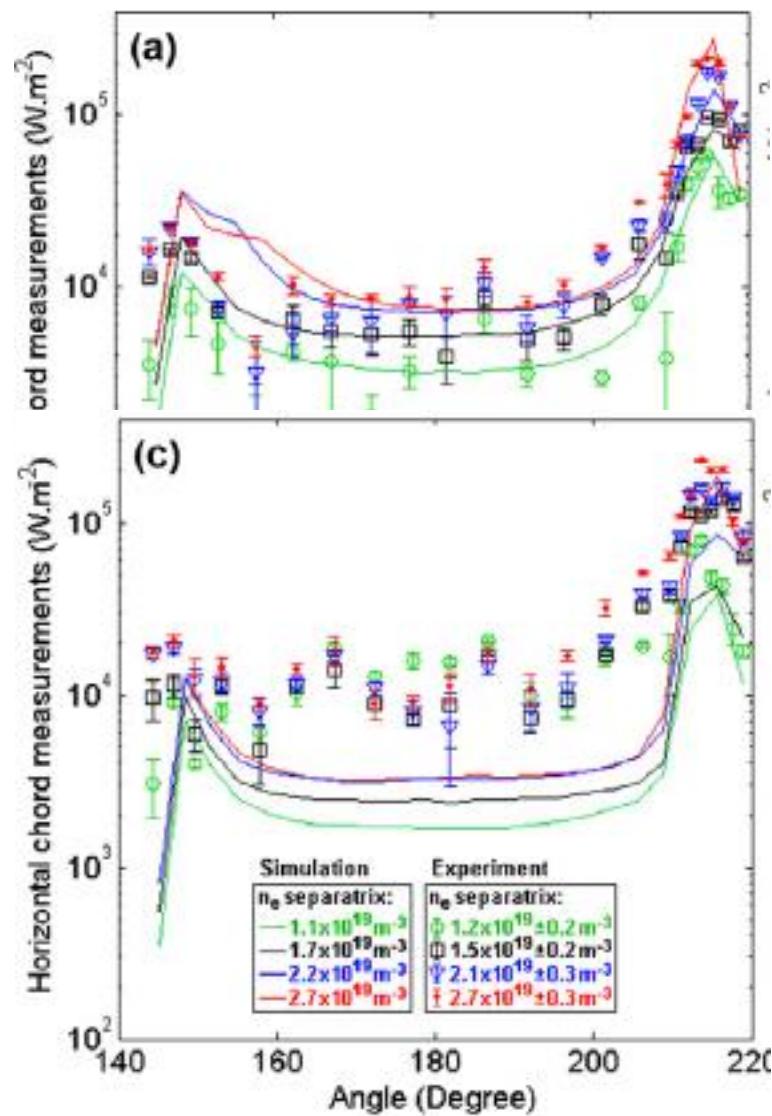
dissociative ionization $e+AB \rightarrow A + B^+ + 2e$

ionization into excited states $e + A \rightarrow (A^+)^* + 2e$

ITER: electron T and power irradiated



Electron temperature (and density)
during three points of density ramp



Power irradiated (0.5-1.5 MW) simulation:
JET-C <10% JET-ILW factor 3!

ITER: wall sputtering

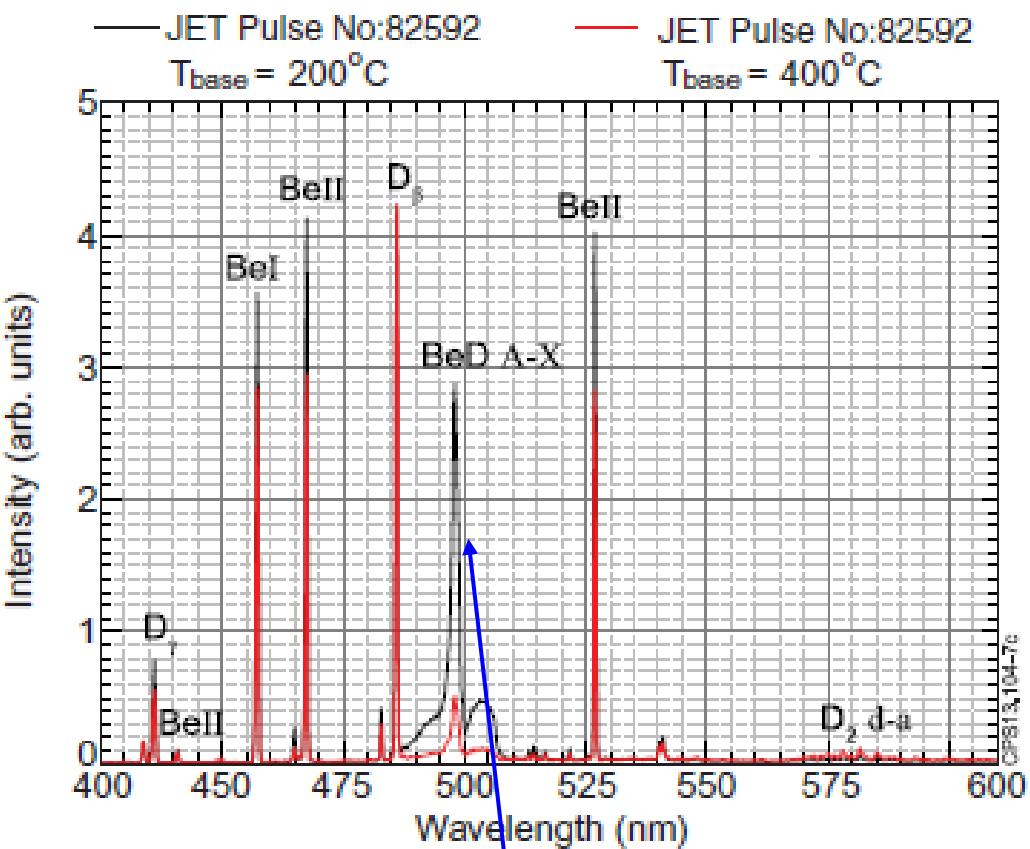
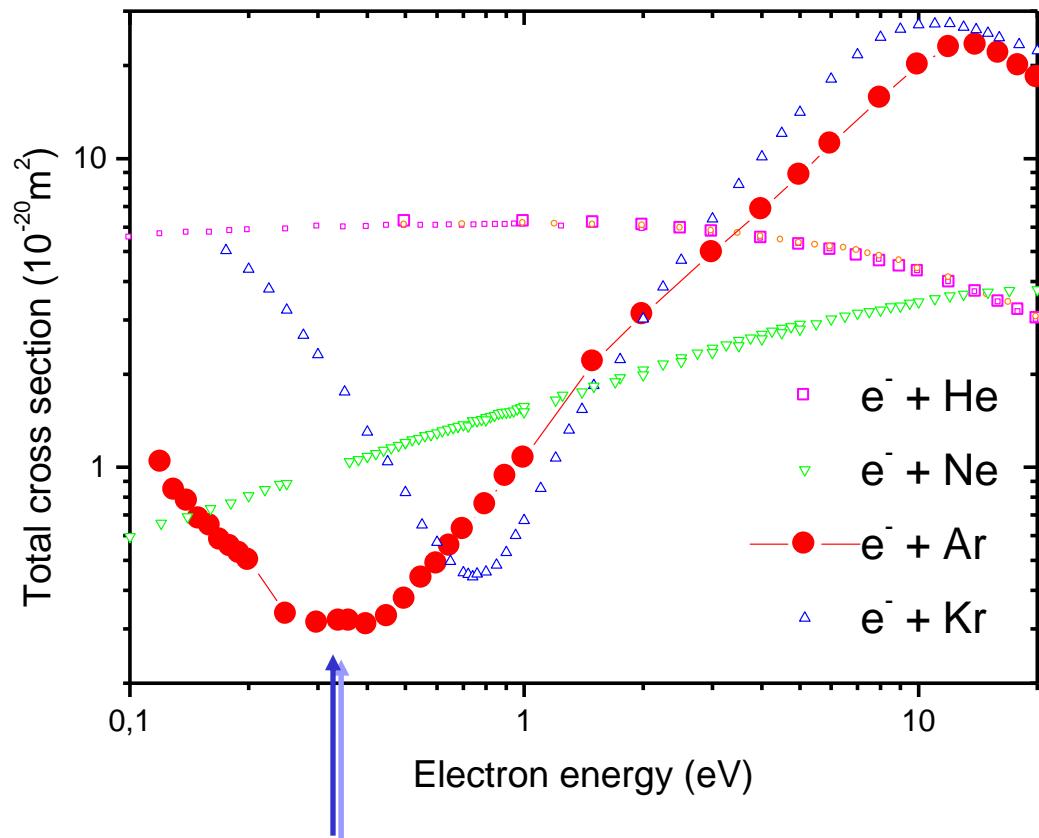


Figure 7. Emission spectra recorded at the Be limiter at the first and last discharge of the series in experiment I representing low T_{base} [JPN #82592] and high T_{base} [JPN #82626] conditions.

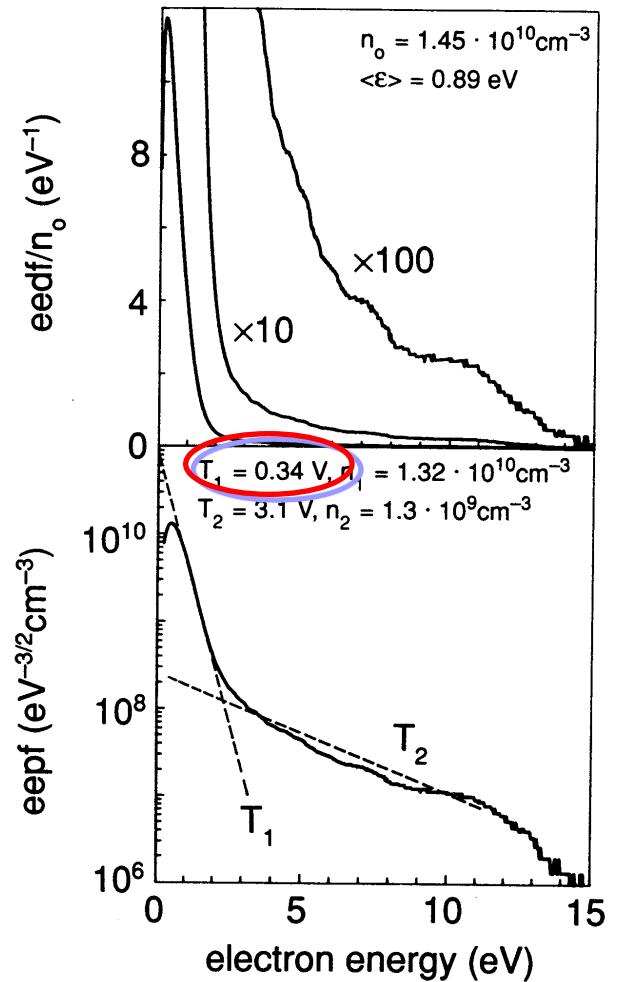
**Study of physical and chemical assisted
physical sputtering of beryllium in the JET
ITER-like wall**

BeD

Plasma temperature ← integral cross sections



Ramsauer
minimum
(zero in s-wave)



V. Godyak, Sendai 2006

Radiation damage in biological tissues

112

M.C. Fuss et al. / Chemical Phys.

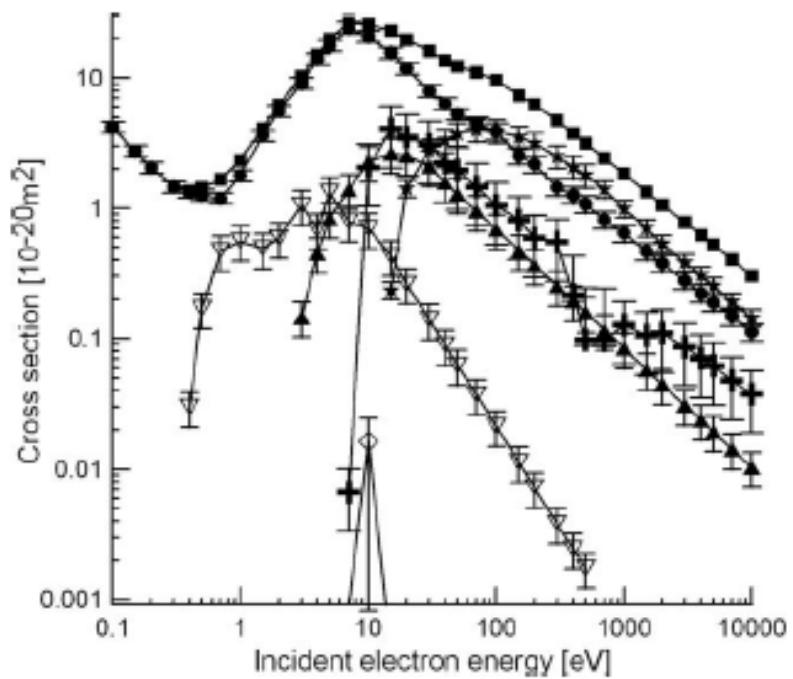


Fig. 1. Integral electron-methane interaction cross sections used in the present work (data of Table 1): ■, total interaction cross section; ●, elastic collision; ★, ionization; ▲, rotational excitation; ▽, vibrational excitation; +, neutral dissociation; ○, dissociative electron attachment. For the total interaction cross section, error bars fall within the size of the symbol used.

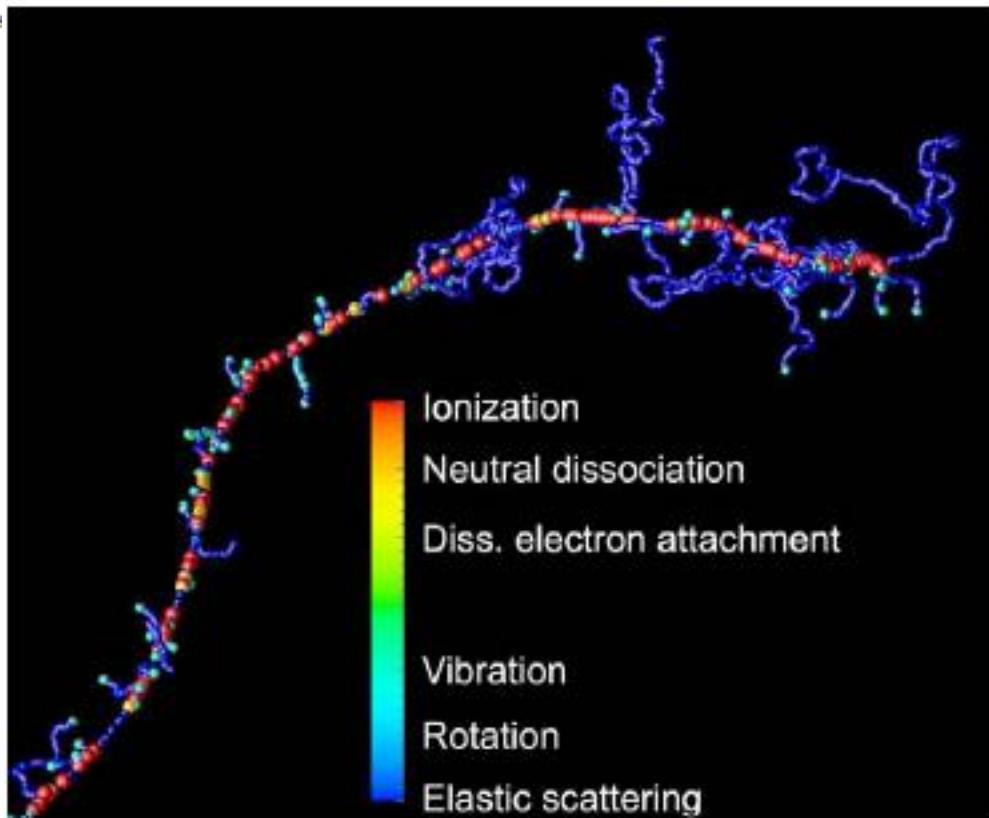
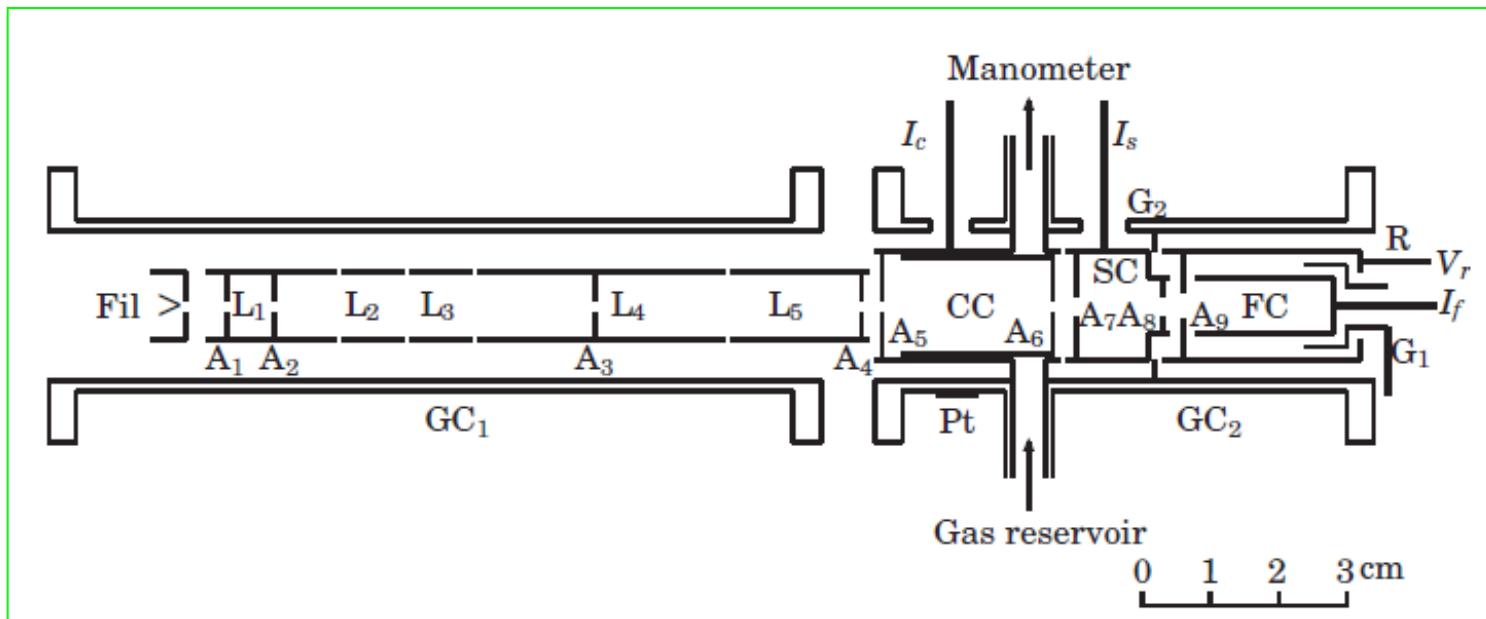
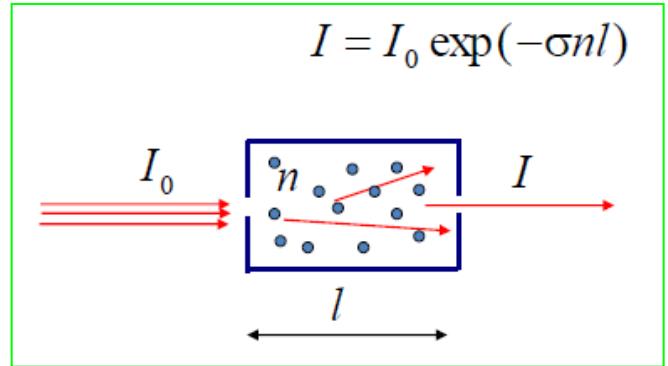


Fig. 6. Detail showing the final part ($\sim 1 \text{ cm}$) of one electron track. The colour does ..ere indicate the type of interaction undergone, including elastic collisions. The production of multiple secondary electrons can be discerned along the primary particle's path.

Experimental methods: total

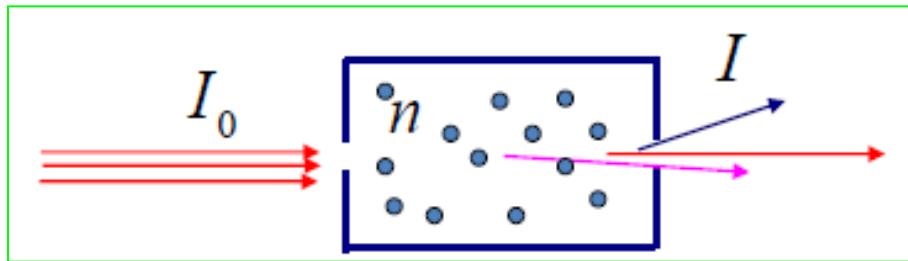
attenuation method $I = I_0 \exp(-\sigma n L)$

precision <5%, unless...



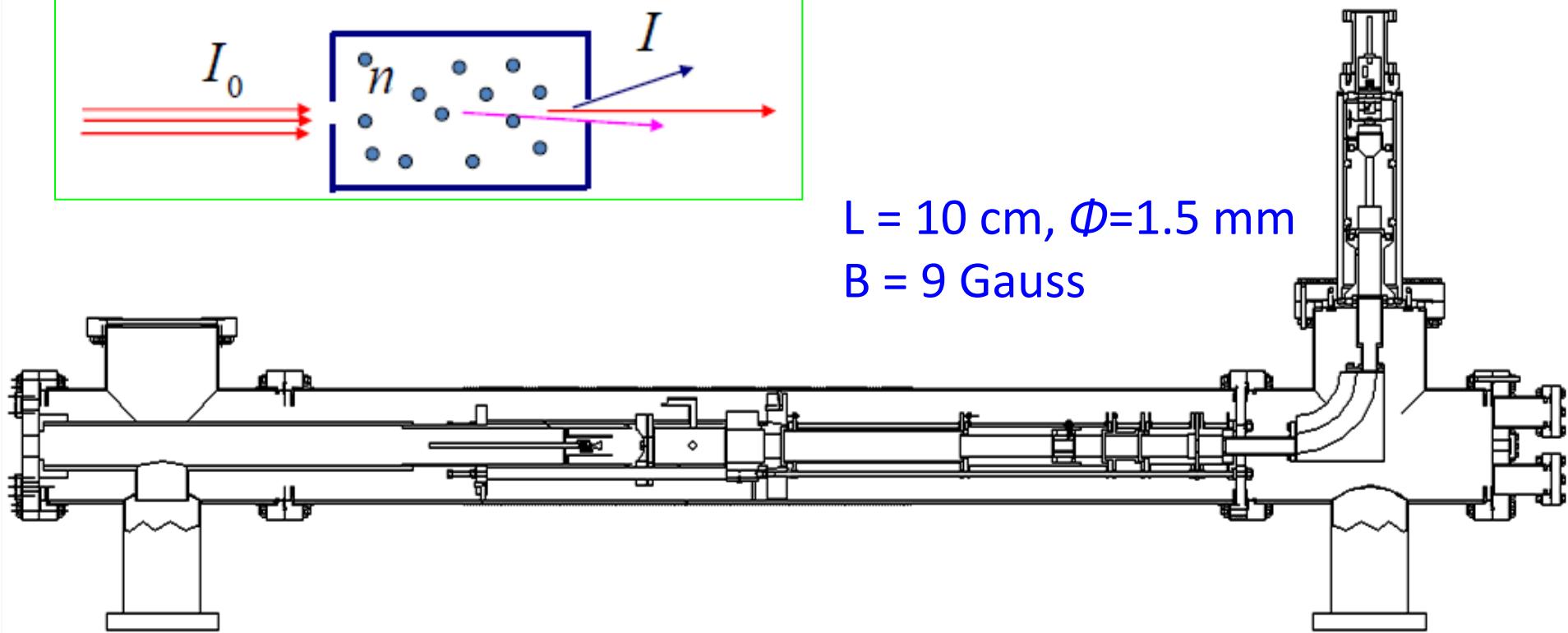
Experimental methods: total

Angular resolution error, leading to underestimation of TCS
→ avoid guiding magnetic field, use long scattering cells with small apertures

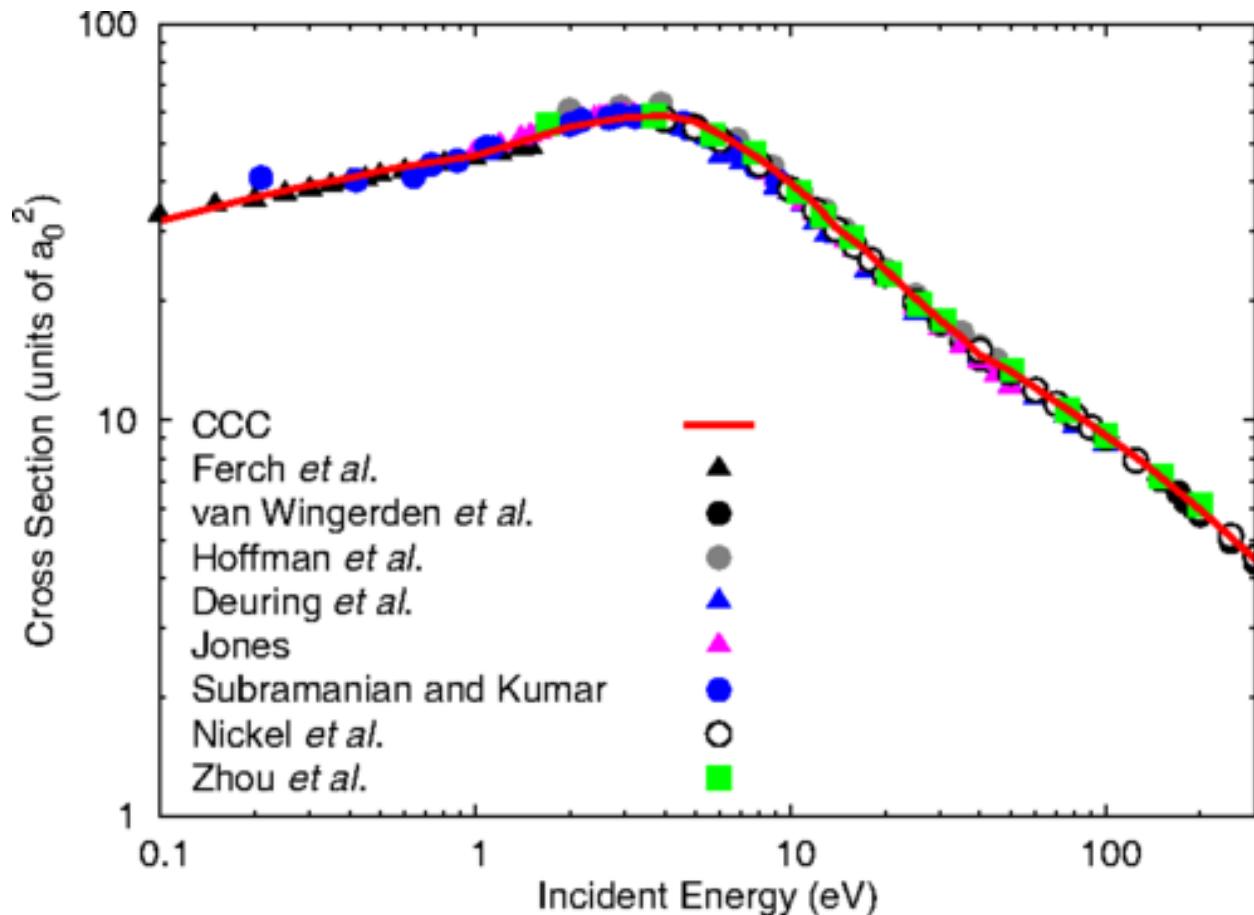


$L = 10 \text{ cm}$, $\Phi = 1.5 \text{ mm}$

$B = 9 \text{ Gauss}$

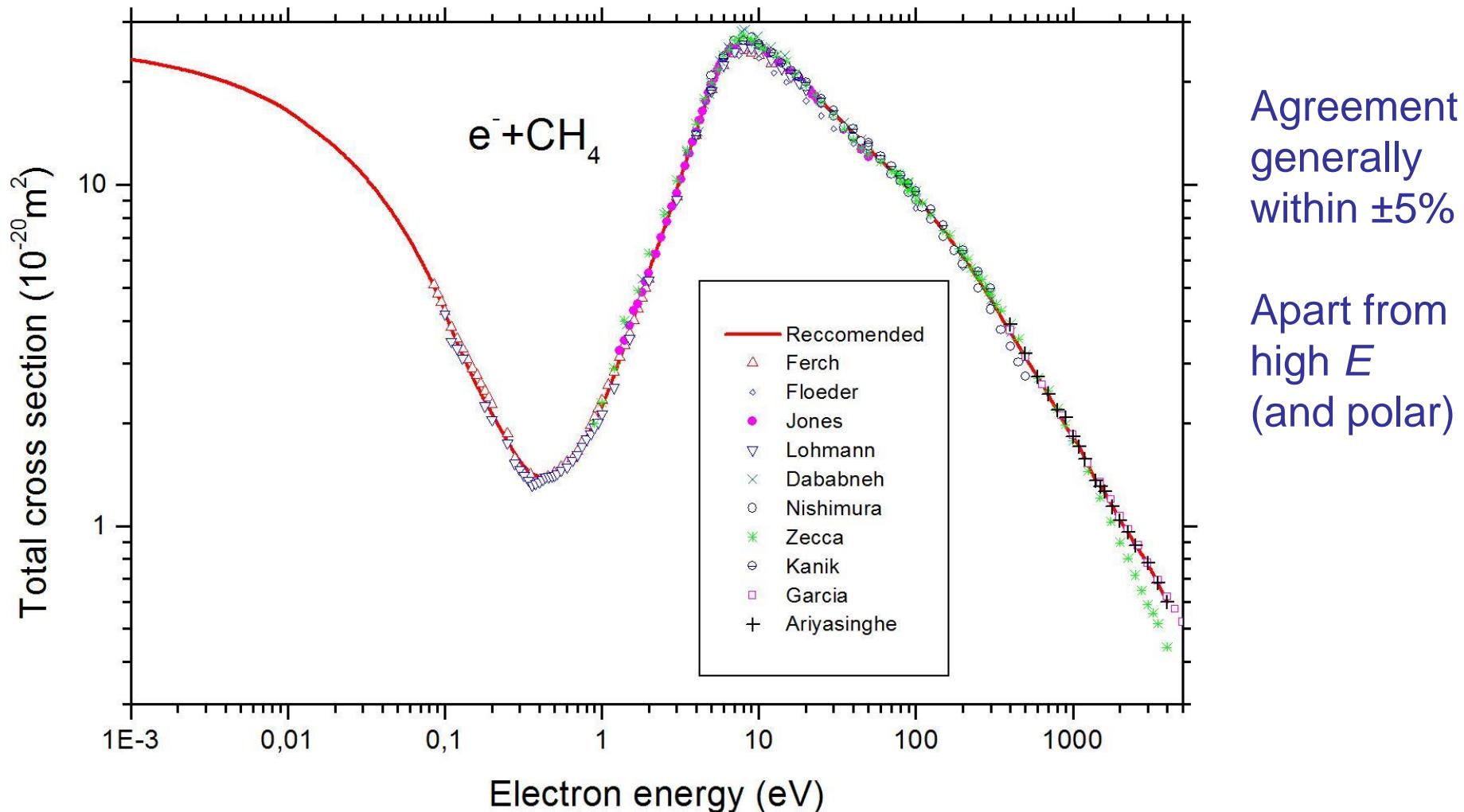


Hydrogen – total: experiment vs theory



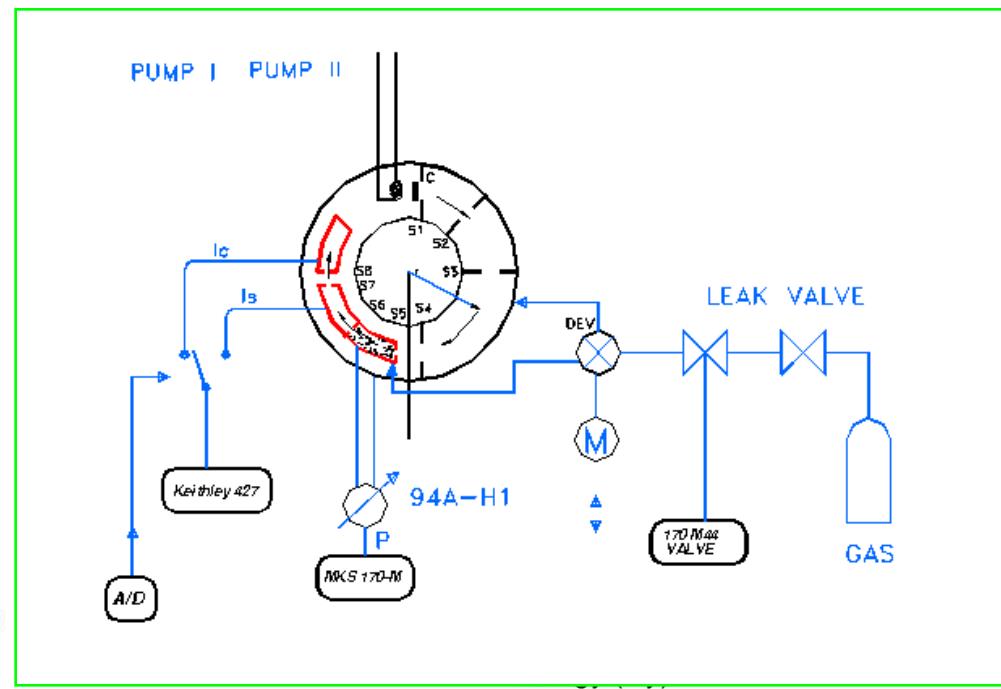
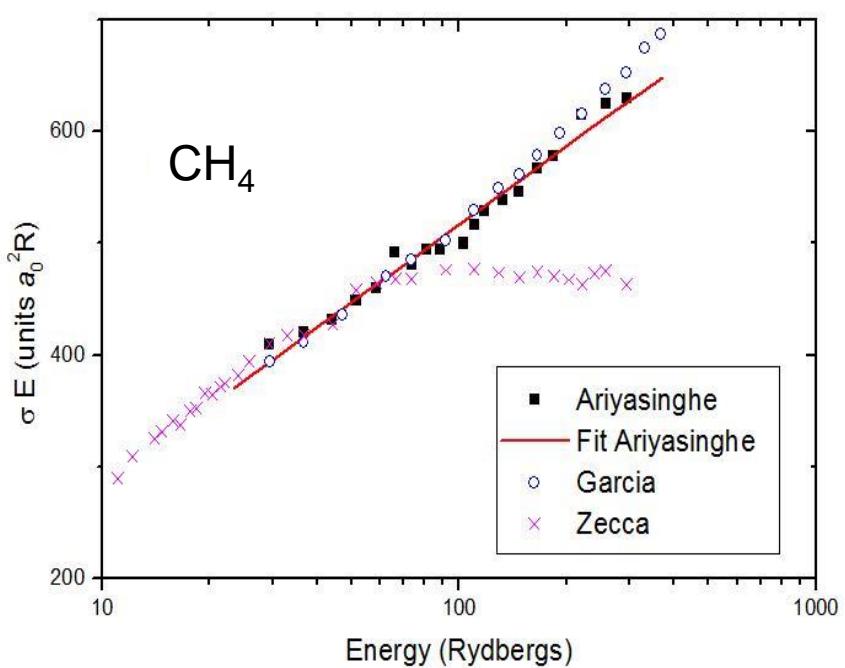
Mark C. Zammit, Jeremy S. Savage, Dmitry V. Fursa, and Igor Bray
Phys. Rev. Lett. 116, 233201
<http://journals.aps.org/prl/abstract/10.1103/PhysRevLett.116.233201>

Experimental methods: total



Total @ high energies: Born-Bethe fit

$$\sigma(E) = A + B \ln E$$

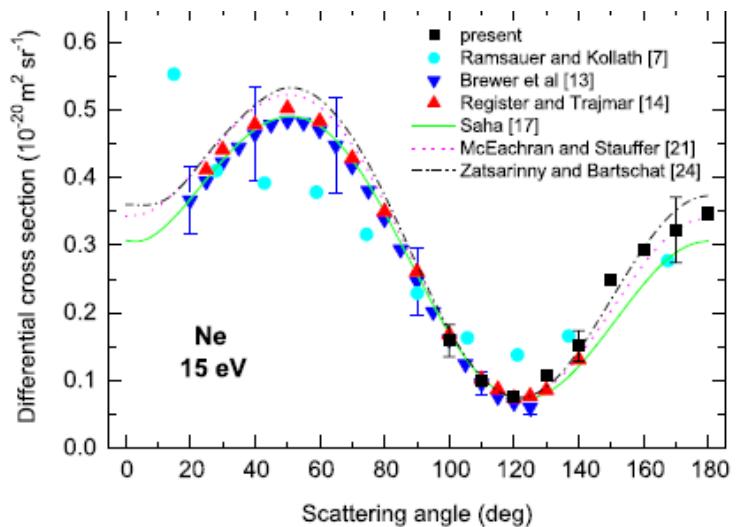
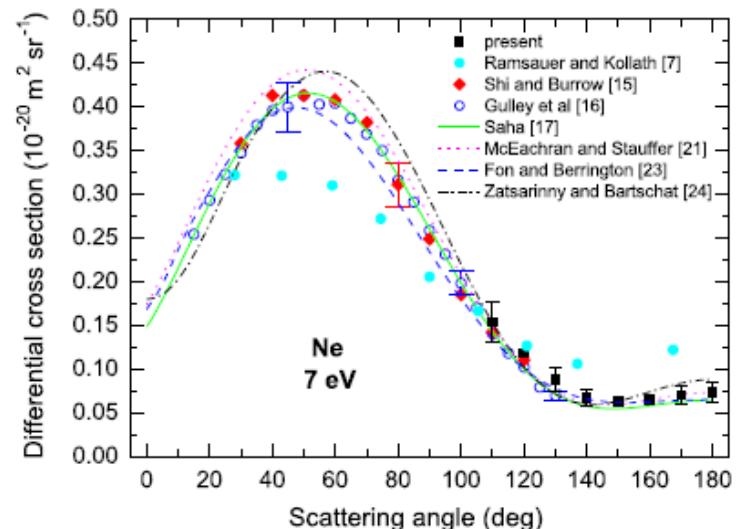
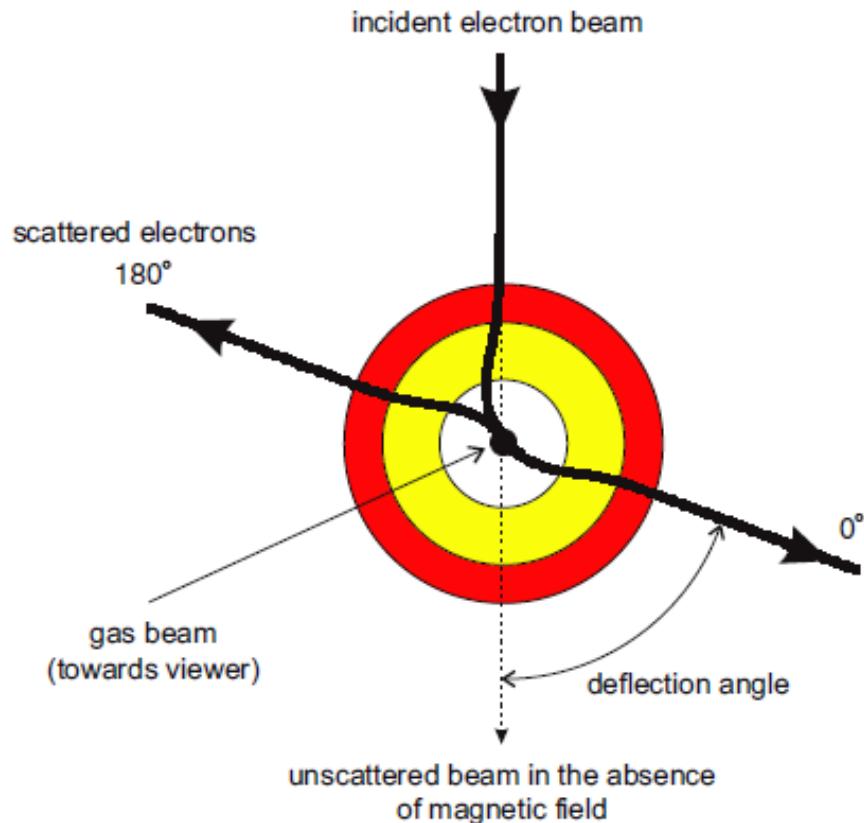


„In the high energy limit present (GK, Zecca) measurements are affected by angular resolution error. In order to evaluate it, differential cross sections at low angles would be needed. A rough evaluation from Born approximation for the elastic channel gives an error of a few percent. Note that the error in TCS can be higher, as Trento apparatus does not perform discrimination against inelastically forward-scattered electrons.

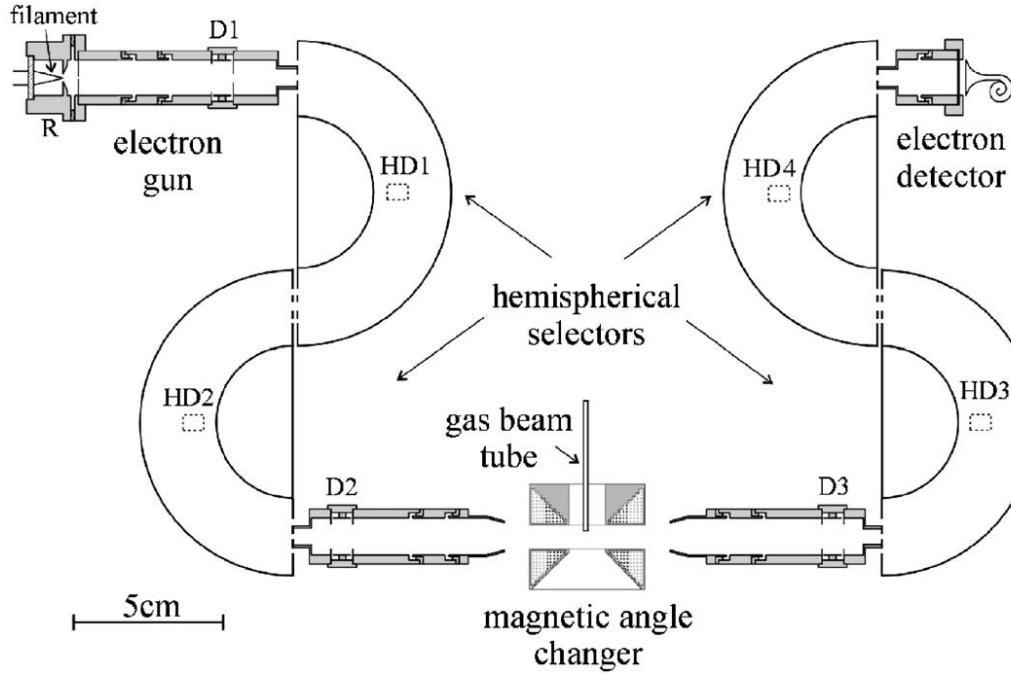
Fig.4. Born-Bethe fit (σ/a_0^2) (E/R) = $A + B \ln (E/R)$ to TCS from Ariysinghe: $A=52.31 \pm 17.3$, $B=232.2 \pm 8.6$ where Rydberg constant is $R=13.6$ eV and the cross sections is expressed in atomic units $a_0^2 = 0.28 \times 10^{-20} \text{m}^2$

Experimental methods: elastic

PHYSICAL REVIEW A 74, 042701 (2006)



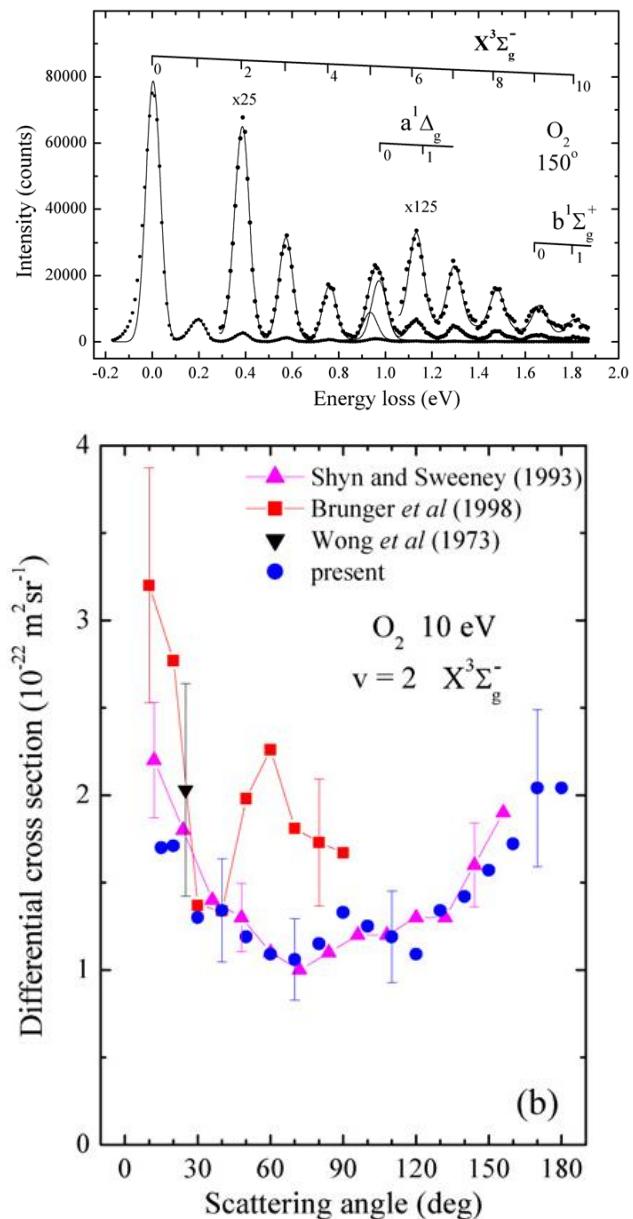
Experimental methods: excitation (electronic, vibrational)



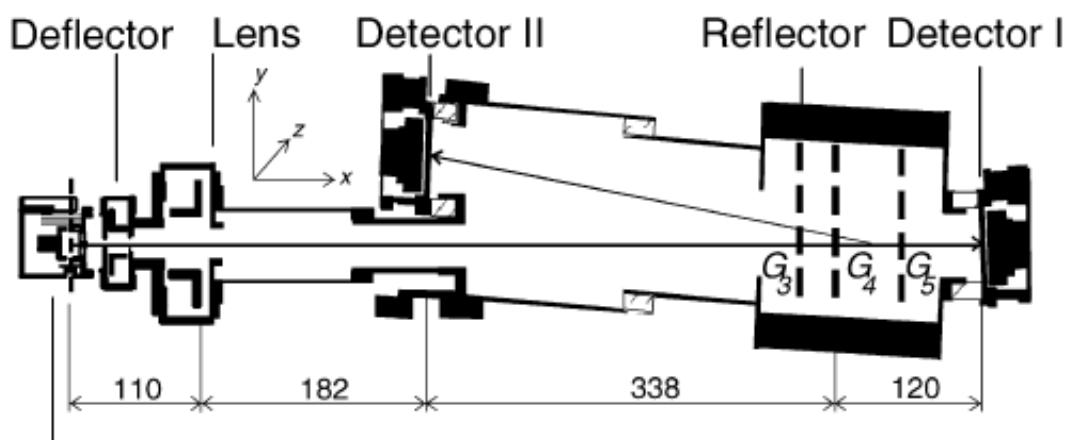
accuracy $\pm 20\text{-}40\%$

Experiments by:

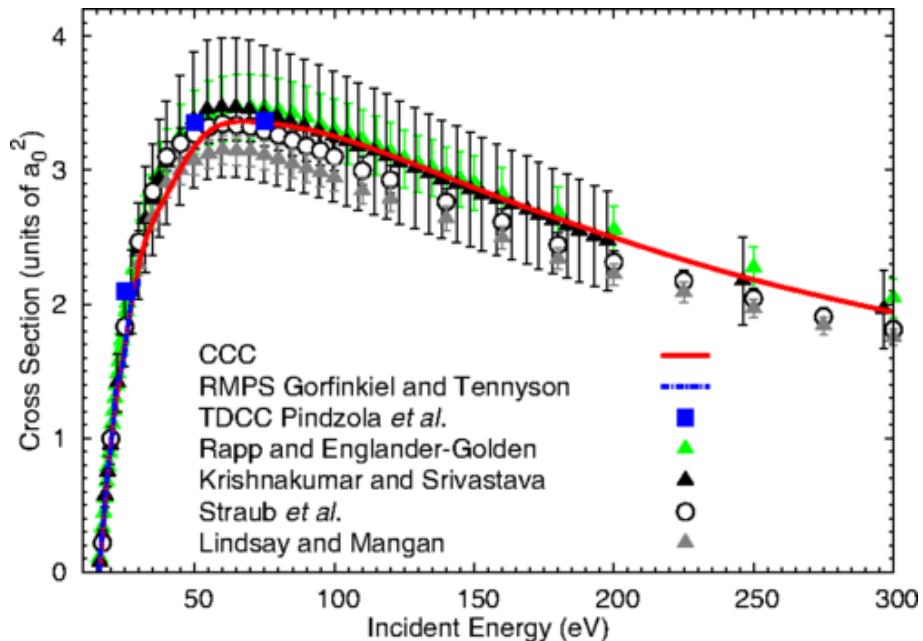
- I. Linert, M. Zubek (Gdansk) J. Phys. B **39** (2006)
- M. Khakoo et al. (Fullerton California)
- M. Allan (Freiburg University)/ J. Fedor (Prague)



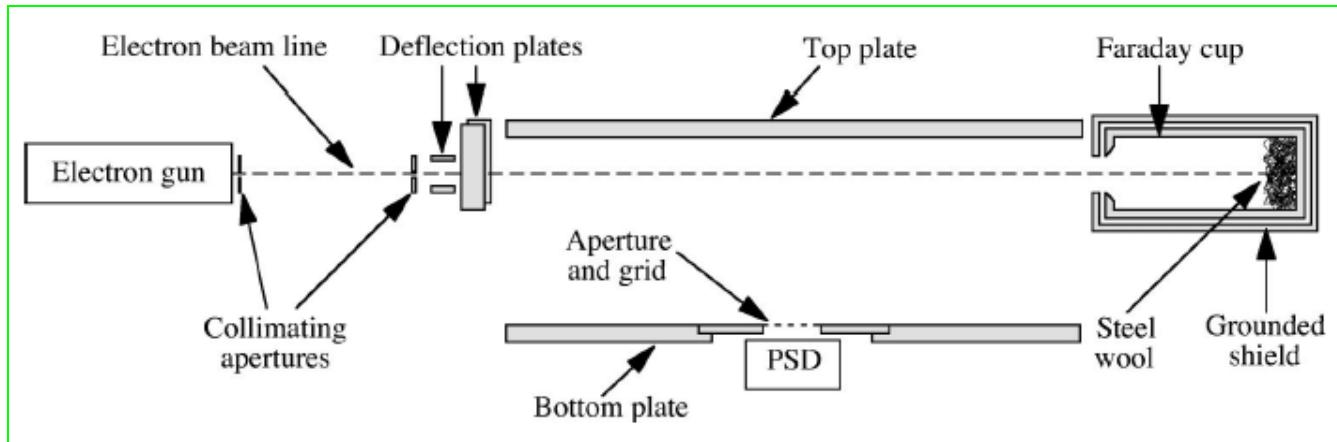
Experimental methods: ionization, total



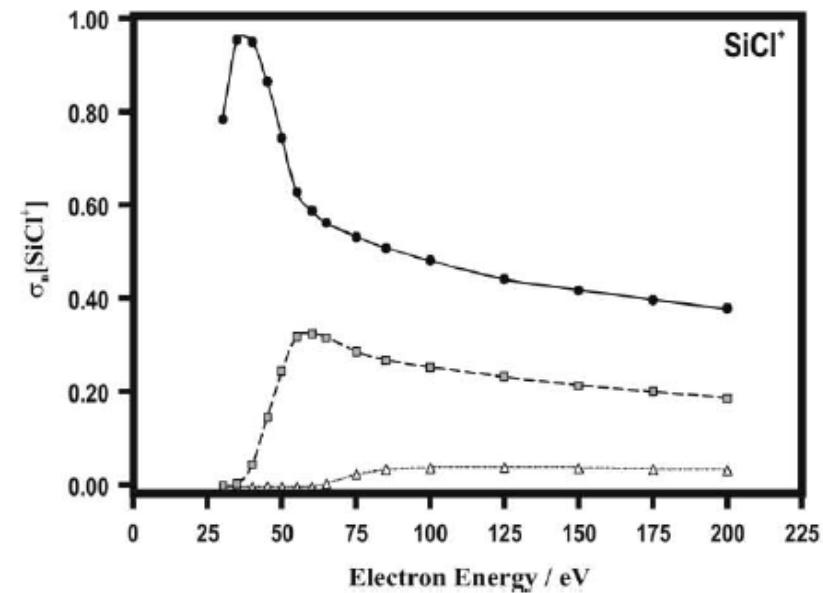
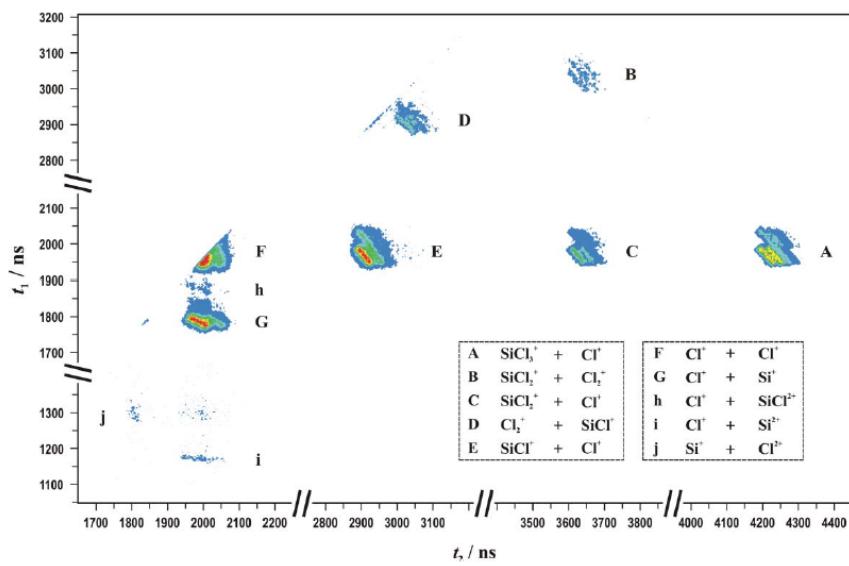
Accuracy: $\pm 10\text{-}15\%$



Experimental methods: ionization (2)

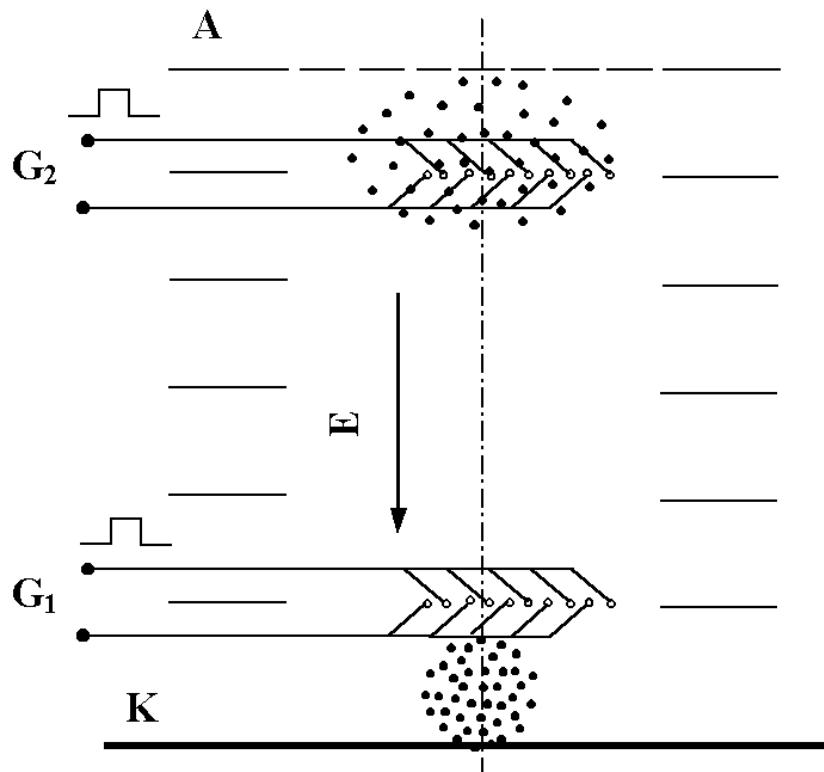


Accuracy: $\pm 15\text{-}20\%$



Diffusion coefficients → electronic distribution function $n_e(\mathbf{r}, \mathbf{v}, t)$

$$\frac{\partial}{\partial t} n_e(\mathbf{r}, t) = -w \frac{\partial}{\partial z} n_e(\mathbf{r}, t) + D_T \left[\frac{\partial^2}{\partial x^2} n_e(\mathbf{r}, t) + \frac{\partial^2}{\partial y^2} n_e(\mathbf{r}, t) \right] + D_L \frac{\partial^2}{\partial z^2} n_e(\mathbf{r}, t)$$



$$w = -\left(\frac{2}{m}\right)^{1/2} \frac{eF}{3N} \int_0^\infty \frac{E}{\sigma_m(E)} \frac{df_0(E)}{dE} dE$$

$$D_T = \left(\frac{2}{m}\right)^{1/2} \frac{1}{3N} \int_0^\infty \frac{E}{\sigma_m(E)} f_0(E) dE$$

Accuracy: ±5-10%

Non-unique modelling

W. Roznerski (+), J. Mechlinśka-Drewko (+),
Y. Nakamura

Hydrogen – electronic excitation (modelling)

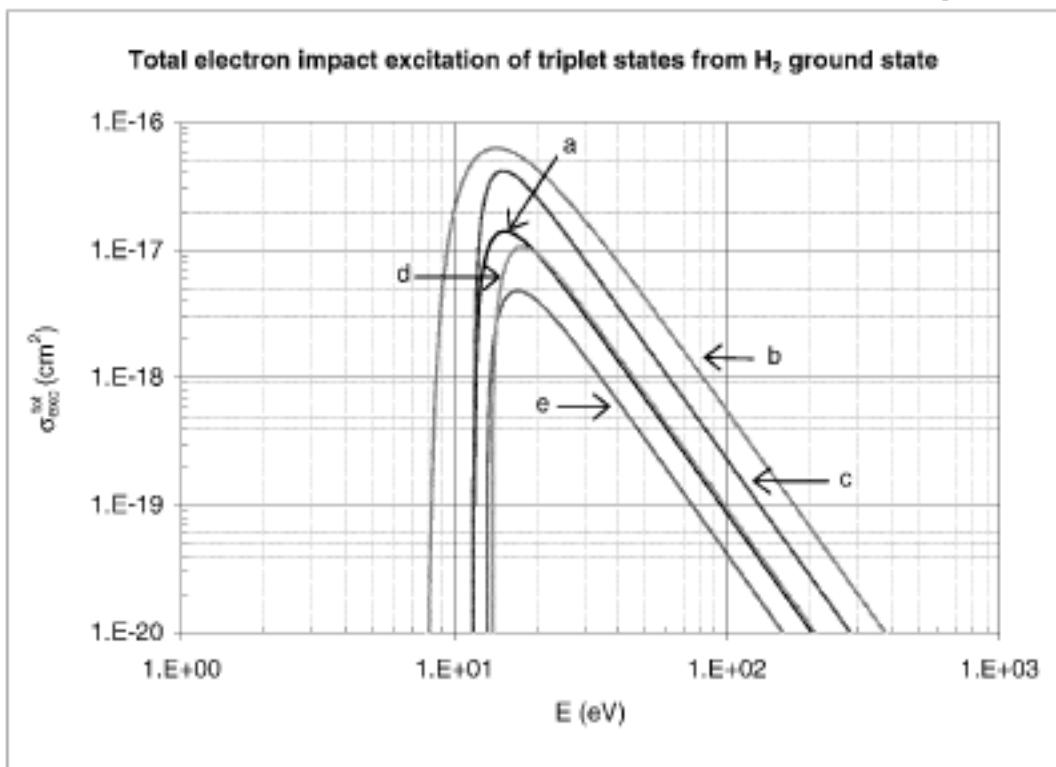
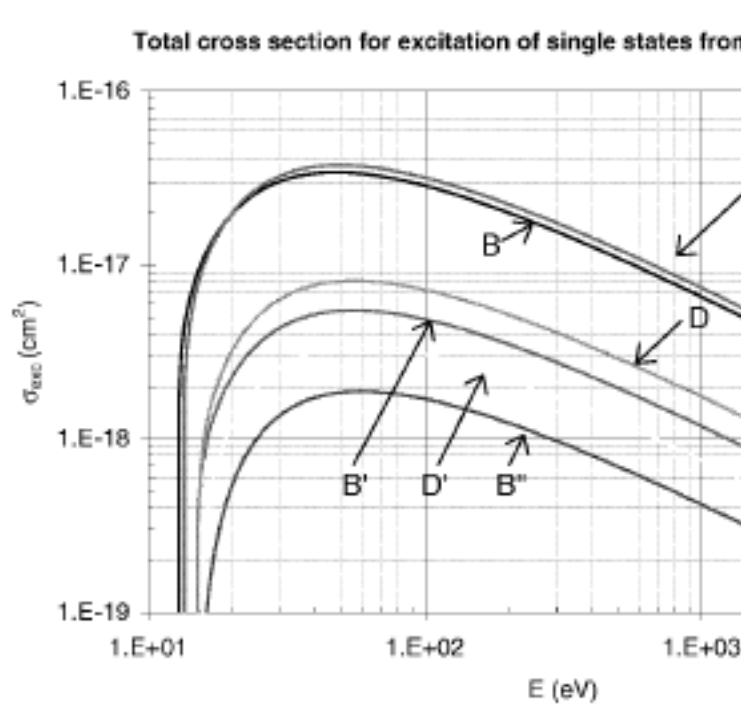


Figure 22: Total electron impact excitation cross section of singlet electronic states of H_2 from the $\text{H}_2(X^1\Sigma_g^+; v = 1)$ ground state.

Figure 25: Total electron impact excitation cross section of a,b,c,d and e triplet states of H_2 from its ($X^1\Sigma_g^+; v = 0$) ground state, Eq. (95).

Collision Processes in Low-Temperature Hydrogen Plasmas

Ratko K. Janev, Detlev Reiter, Ulrich Samm

JüL-4105
Dezember 2003
ISSN 0944-2952

Hydrogen – electronic excitation (2010)

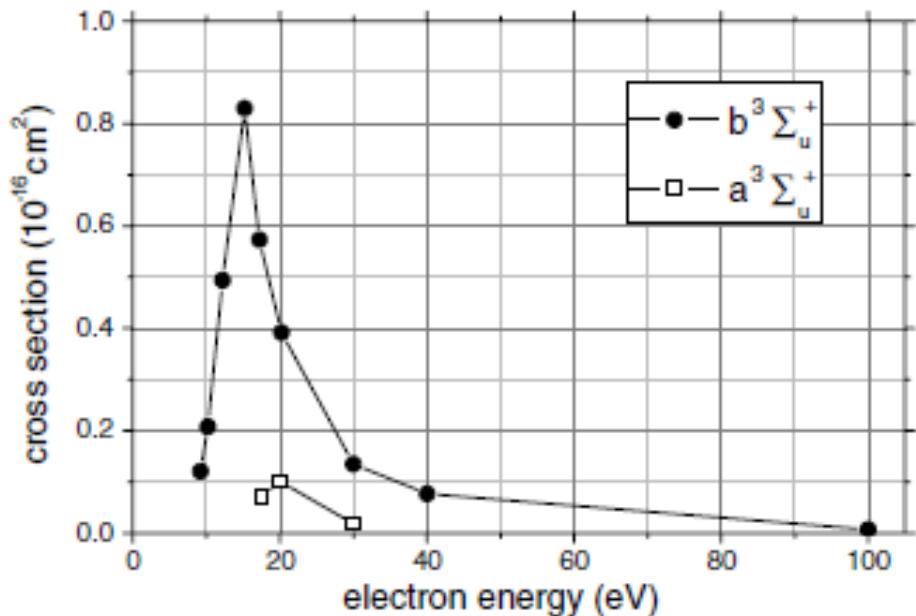


Figure 7. The electronic excitation cross sections for $b^3\Sigma_u^+$ and $a^3\Sigma_g^+$ states of H_2 as given by Yoon *et al* [36]. These cross sections

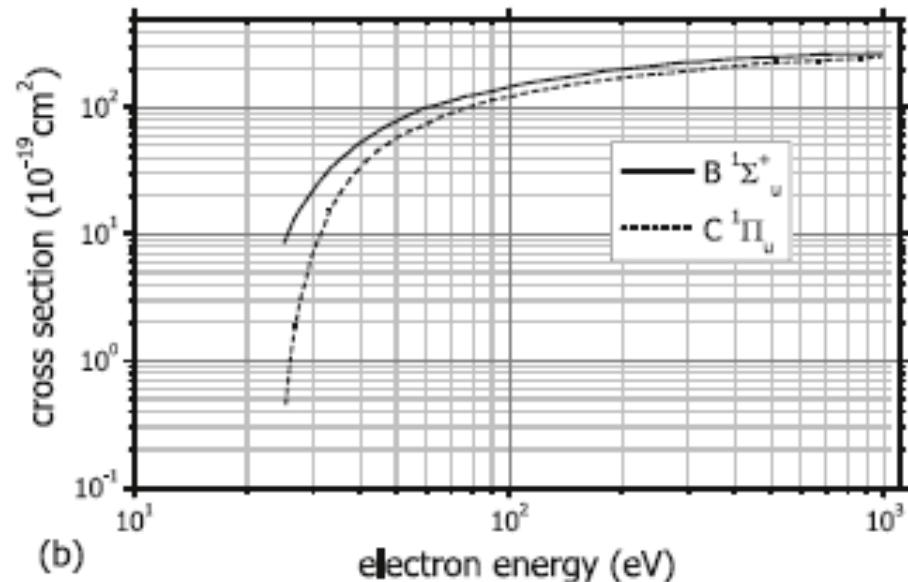


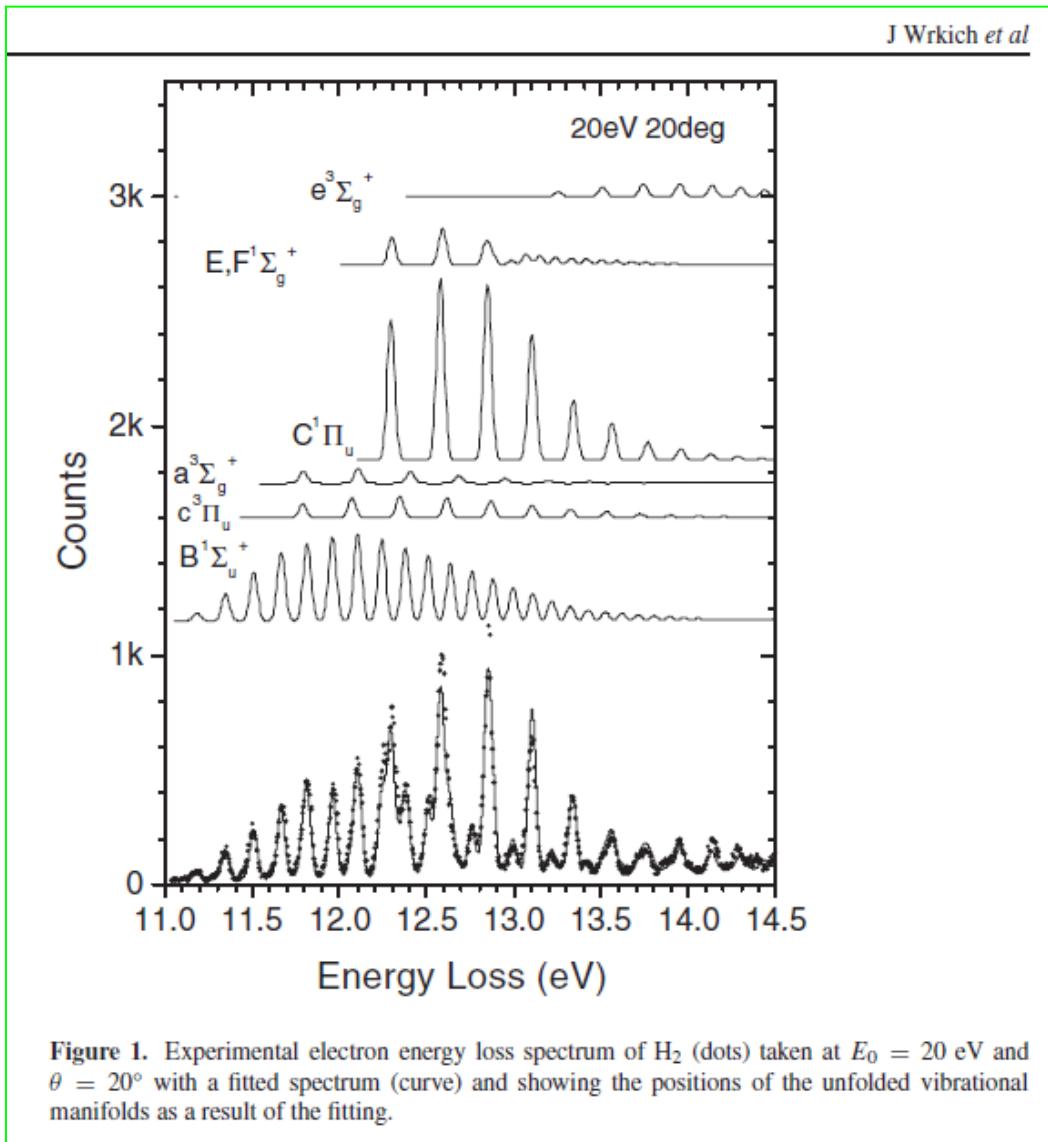
Figure 8. (a) Electron-impact excitation cross sections of Lyman and Werner bands of D_2 . Solid curve: Lyman bands; dots: Werner bands. (b) Log–log plot for cross sections of $B^1\Sigma_u^+$ (solid) and $C^1\Pi_u$ (dots) in the threshold energy region [53].

Jung-Sik Yoon¹, Young-Woo Kim¹, Deuk-Chul Kwon¹, Mi-Young Song¹, Won-Seok Chang¹, Chang-Geun Kim², Vijay Kumar³ and BongJu Lee¹

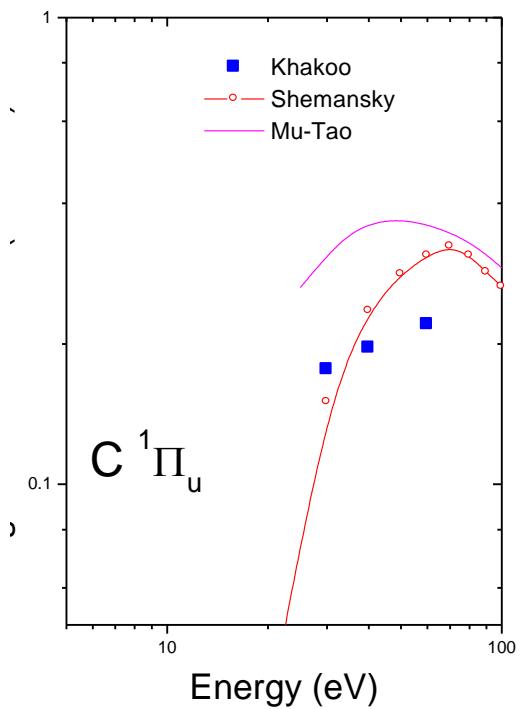
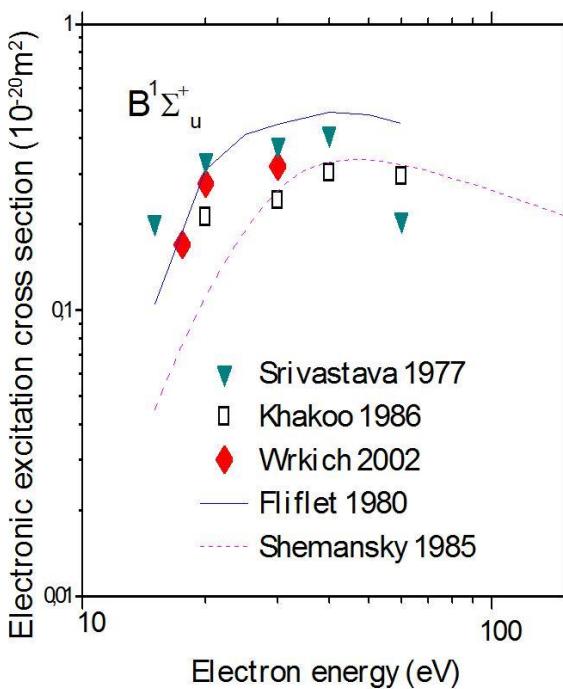
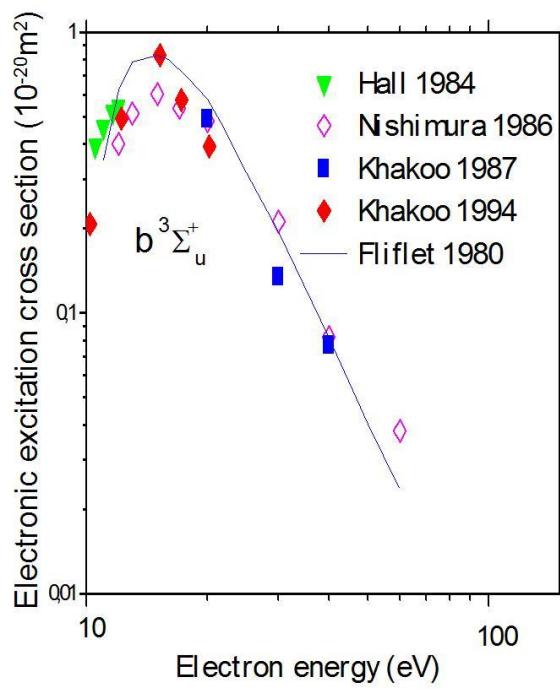
Rep. Prog. Phys. 73 (2010) 116401

Jung-Sik Yoon, Mi-Young Song, Jeong-Min Han, Sung Ha Hwang, Won-Seok Chang, and BongJu Lee
Journal of Physical and Chemical Reference Data. Volume 37, Issue 2 > 10.1063/1.2838023

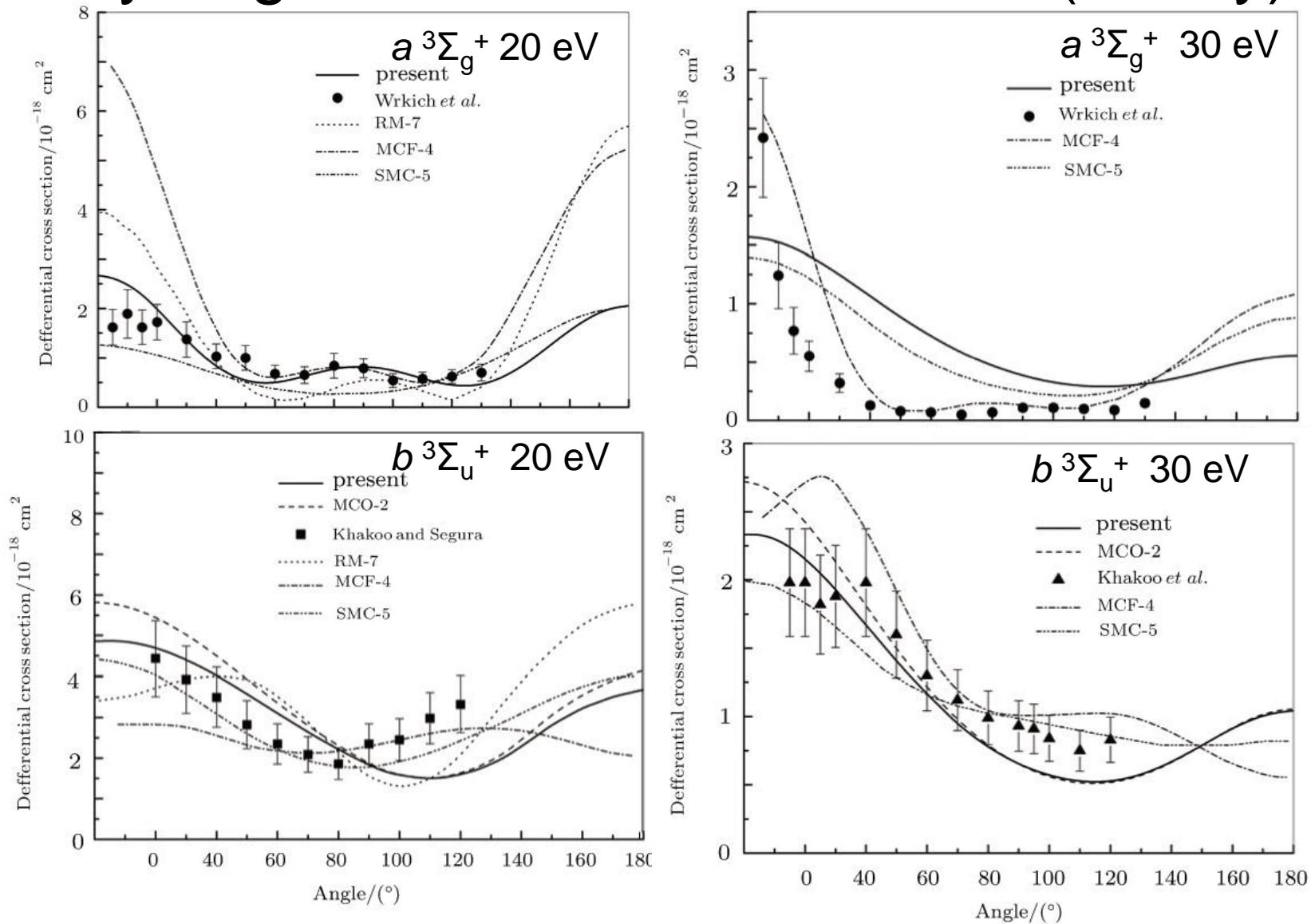
Electronic excitation – deconvolutions of spectra (H_2)



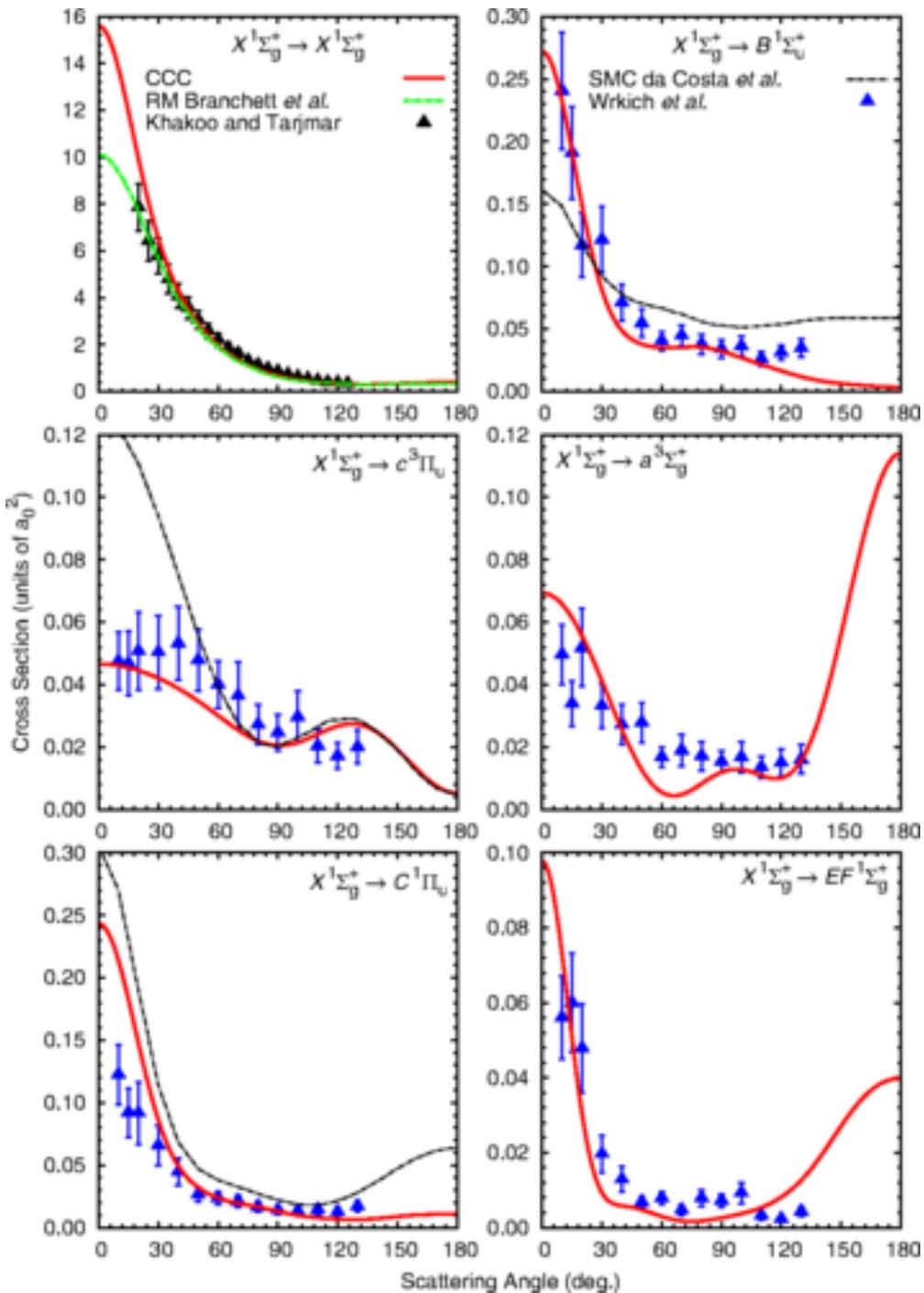
Electronic excitation – dipole allowed and forbidden in H₂



Hydrogen – electronic excitation (theory)



Hydrogen – a complete set of electronic excitations (singlet and triplet states)



Perfect agreement, i.e. within
experimental total uncertainties

Zammit et al. PRL 2016

Nitrogen – electronic excitation

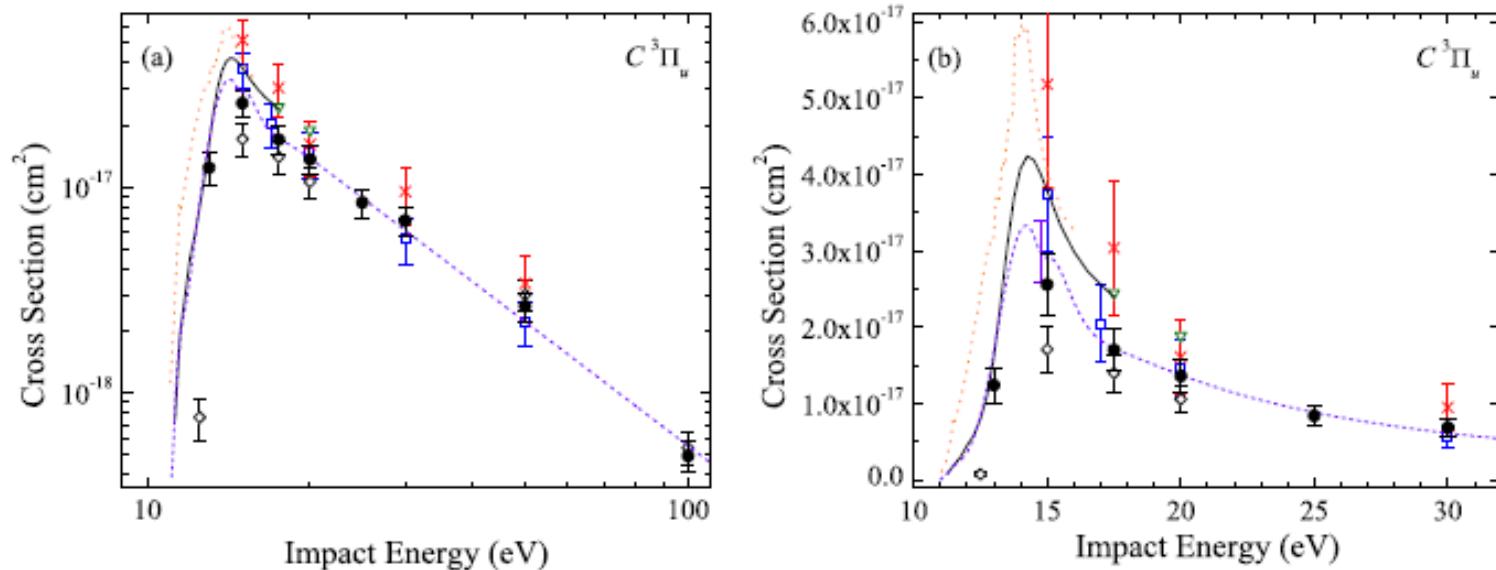


Figure 2. ICSs for electron-impact excitation of the $C^3\Pi_u$ state of N_2 . The plots illustrate (a) shape and (b) magnitude. Black solid circles, present data; black open diamonds, Johnson *et al* [1]; blue open squares, Trajmar *et al* [13]; green inverted open triangles, Zubek and King [4]; red crosses, Campbell *et al* [11]; black solid line, Zubek [27]; purple dashed line, Shemansky *et al* [10] (see the text); red dotted line, Poparić *et al* [28].

Good agreement between experiments, few theories

Nitrogen – electronic excitation

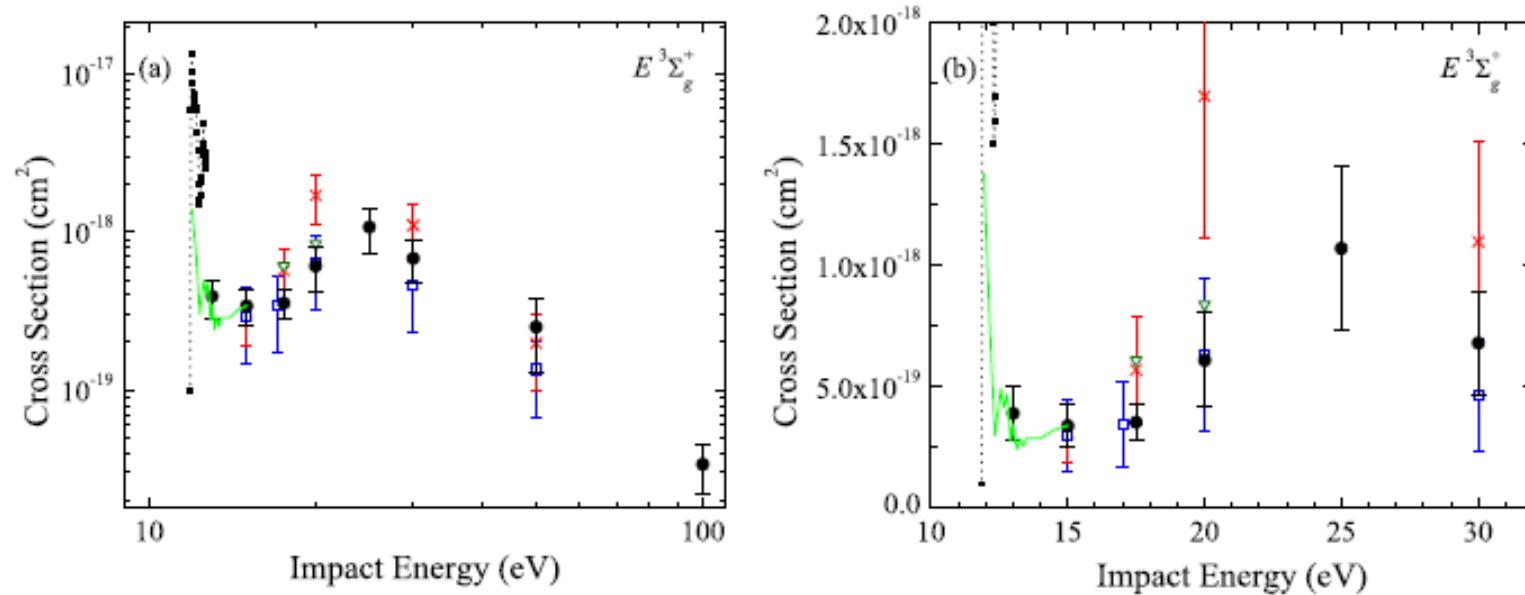


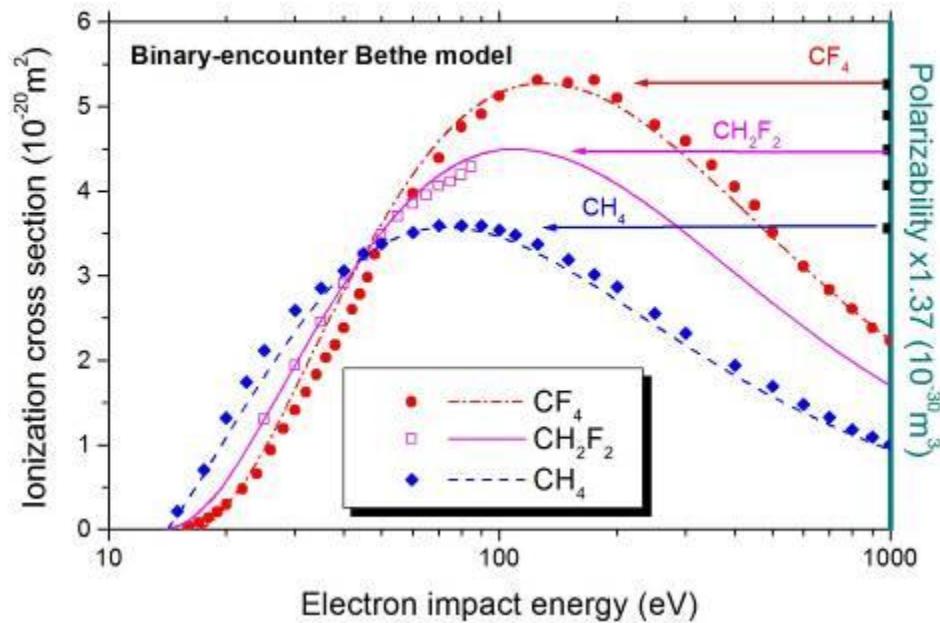
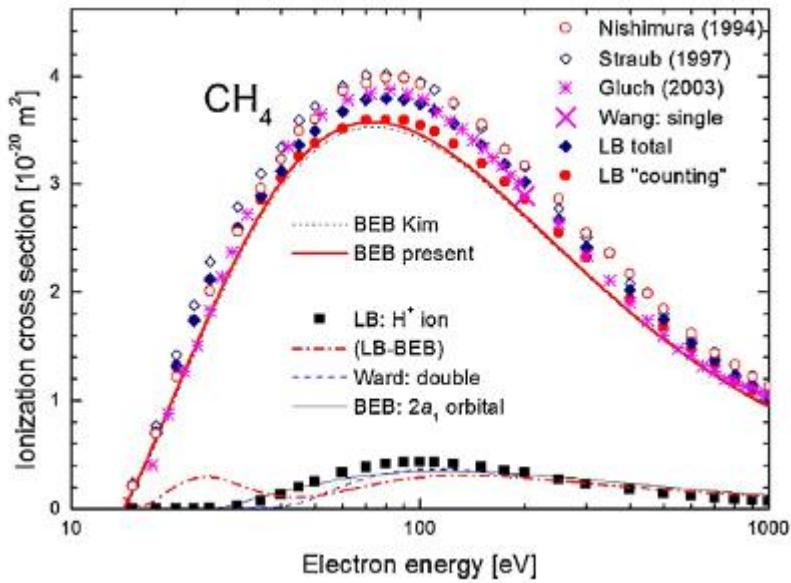
Figure 3. ICSs for electron-impact excitation of the $E\ ^3\Sigma_g^+$ state of N_2 . Black solid circles, present data; blue open squares, Trajmar *et al* [13]; green inverted open triangles, Zubek and King [4]; red crosses, Campbell *et al* [11]; light green solid line, Zubek [26]; black solid squares with dotted line, Brunger *et al* [25].

Qualitative agreement between experiments, few theories

Ionization: semiempirical formulae

$$\sigma [\text{cm}^2] = \frac{10^{-13}}{IE} \left\{ A_1 \ln(E/I) + \sum_{i=2}^N A_i \left(1 - \frac{I}{E}\right)^{i-1} \right\},$$

R. K. Janev, D. Reiter, Phys. Plasmas 9, 4071 (2002);



$$\sigma = \sum_n 4\pi a_0^2 \xi_n \left(\frac{R}{I_n}\right)^2 \frac{1}{t + u_n + 1} \left\{ 1 - \frac{1}{t} + \frac{\ln t}{2} \left(1 - \frac{1}{t^2}\right) - \frac{\ln t}{t+1} \right\}$$

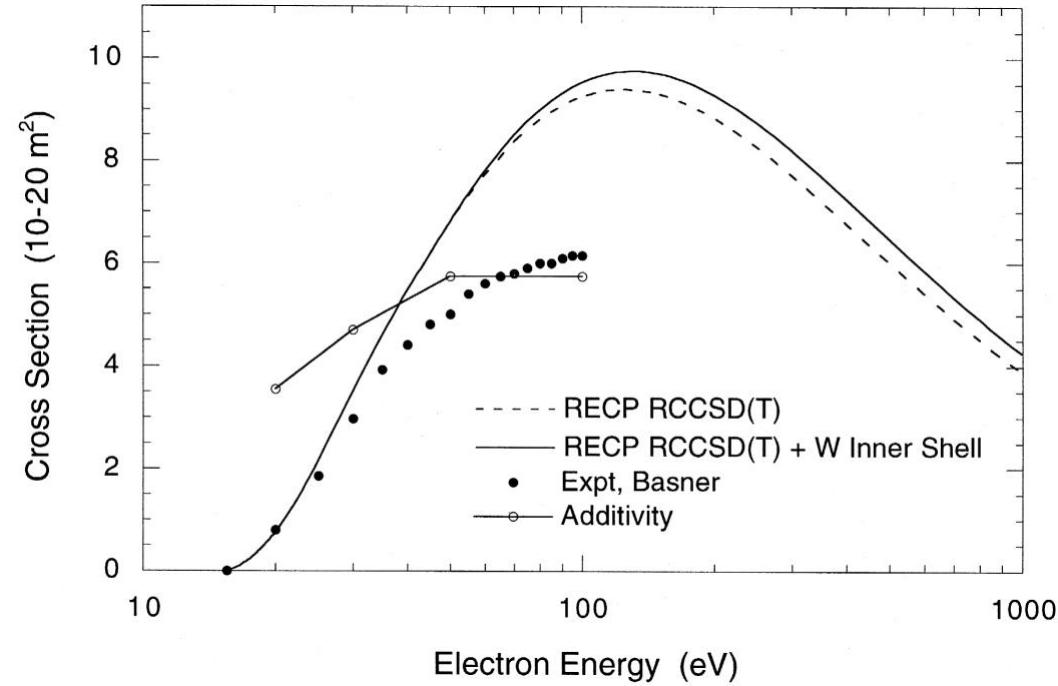
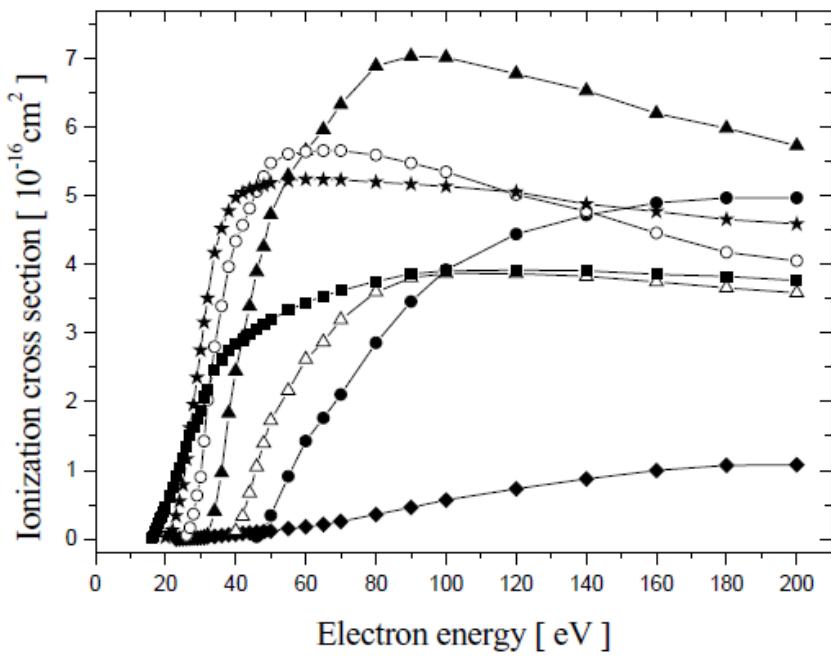
Normalized energies: $t = E/I_n$, $u_n = E_{kin}/I_n$ Only two values needed from QCh

Y.-K. Kim and M. E. Rudd, Phys. Rev. A 50 (1994) 3954

G. Karwasz, P. Mozejko, M.-Y. Song, Int. J. Mass Spectrometry (2014)

Partial (and total) ionization: WF_6

- WF_5^+ ; * WF_4^+ (x10); o WF_3^+ (x10); ▲ WF_2^+ (x10)

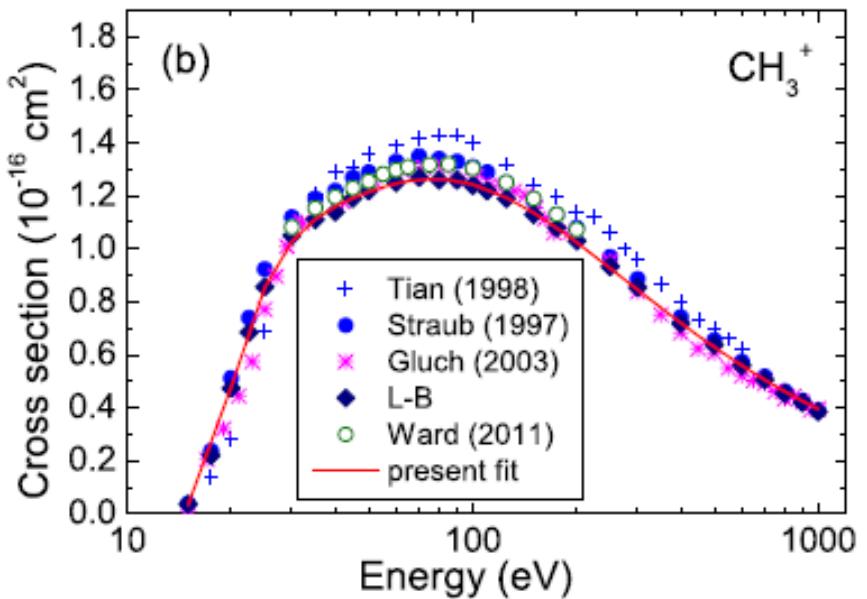
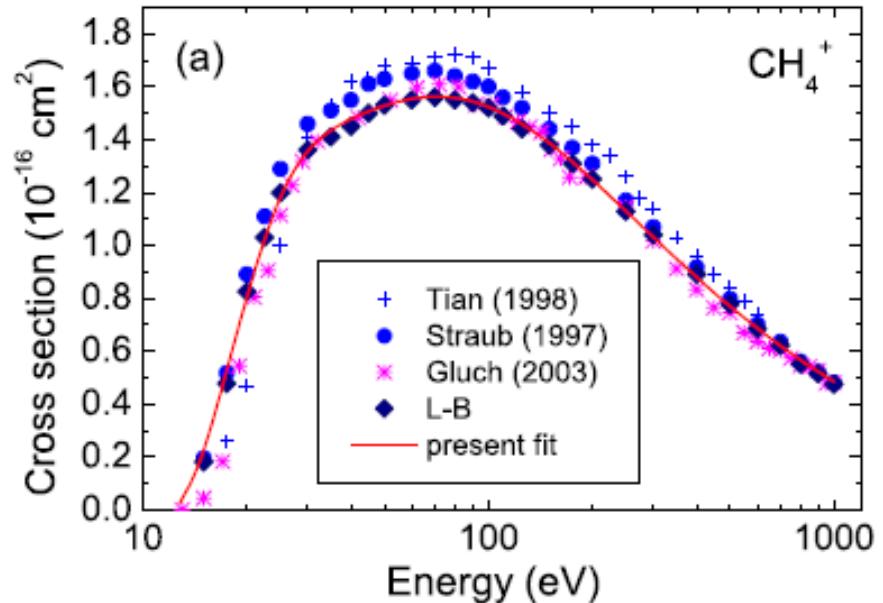


Total ionization in **serious (50%) disagreement** with relativistic BEB

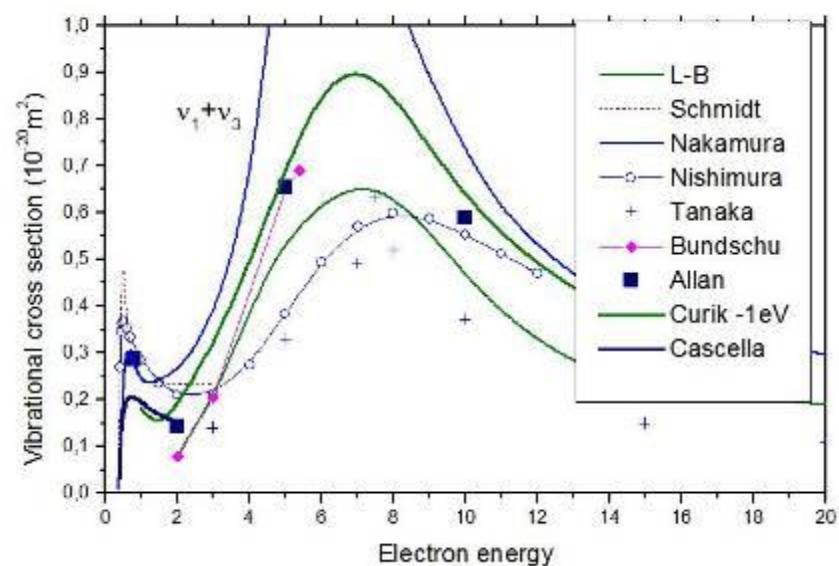
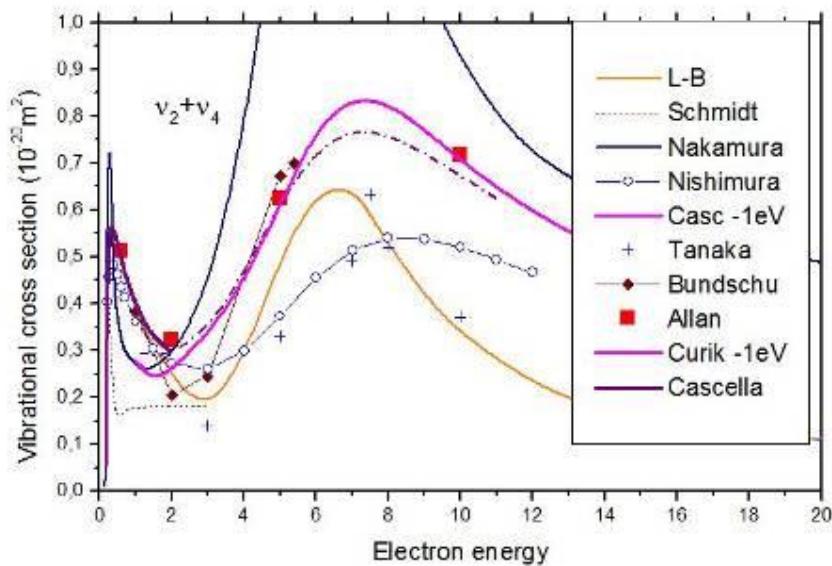
R. Basner, M. Schmidt, K. Becker, Int. J. Mass Spectr. 233 (2004) 25
W.M. Huo, Y.-K. Kim, Chemical Physics Letters 319 (2000) 576–586

Partial ionization: CH_4

Agreement within 15-20%;
unless some cases, like H^+ ions

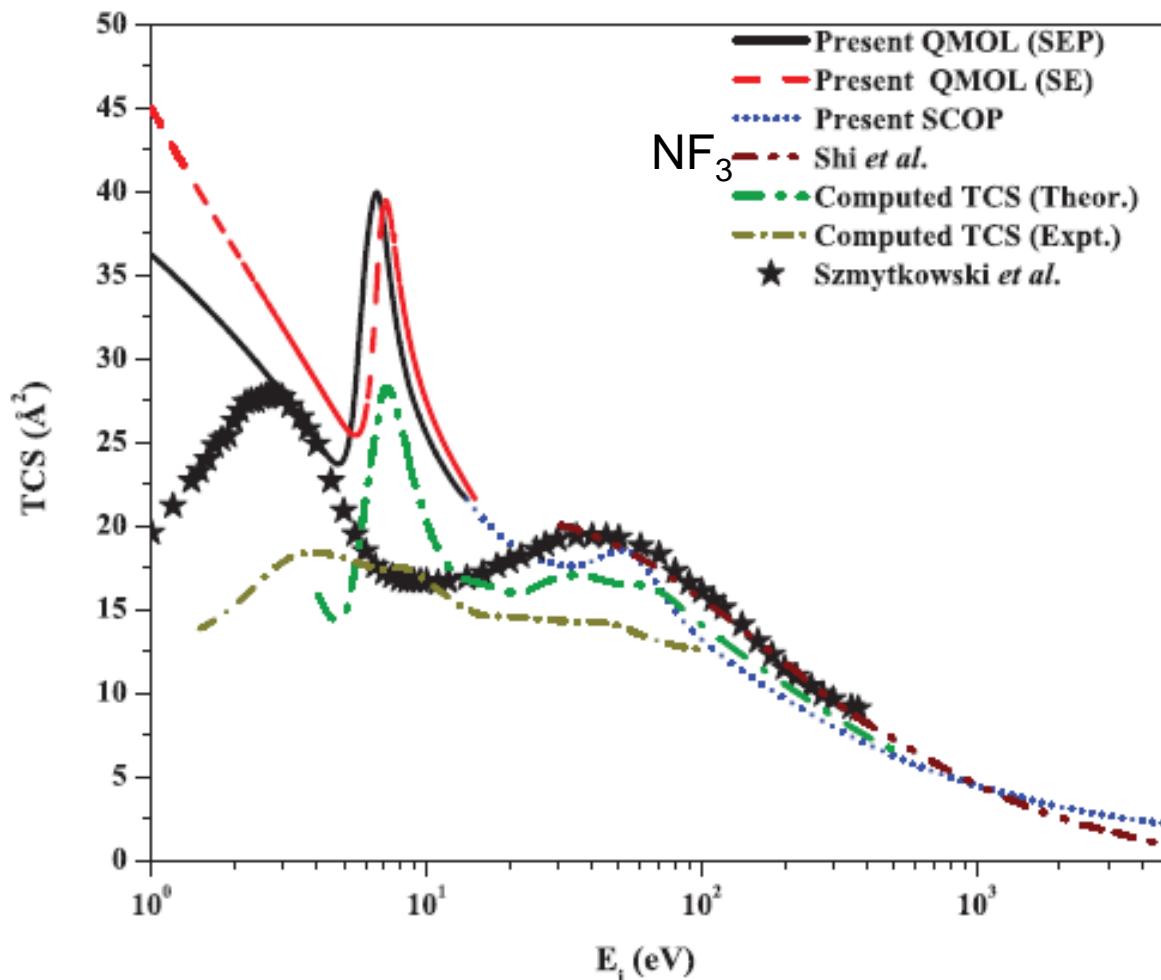


Vibrational: resonant scattering in CH₄



Serious (by few folds) disagreement between swarm-derived, beam-measured and theoretical values

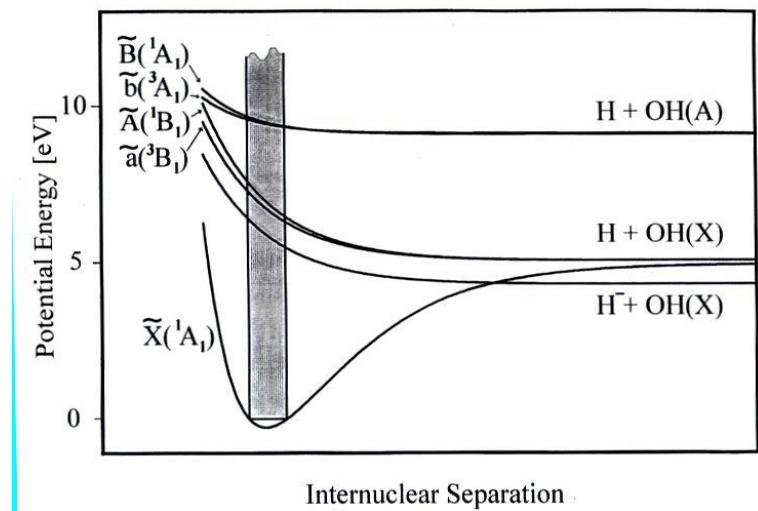
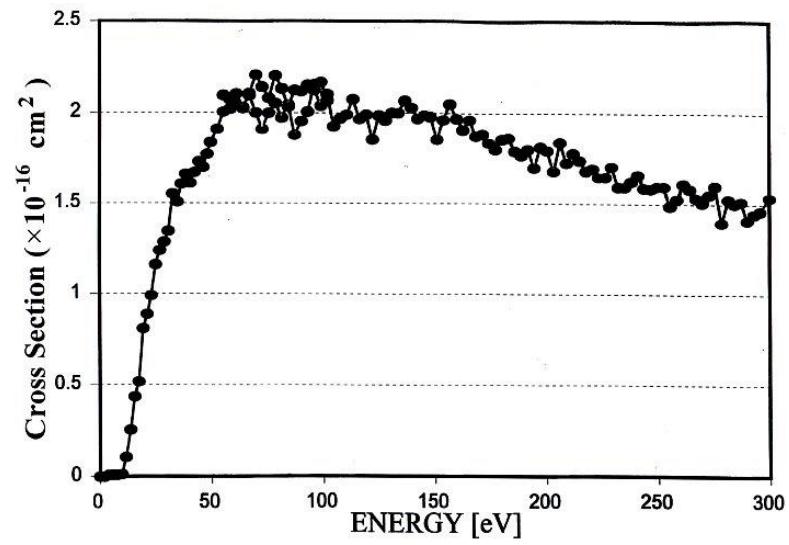
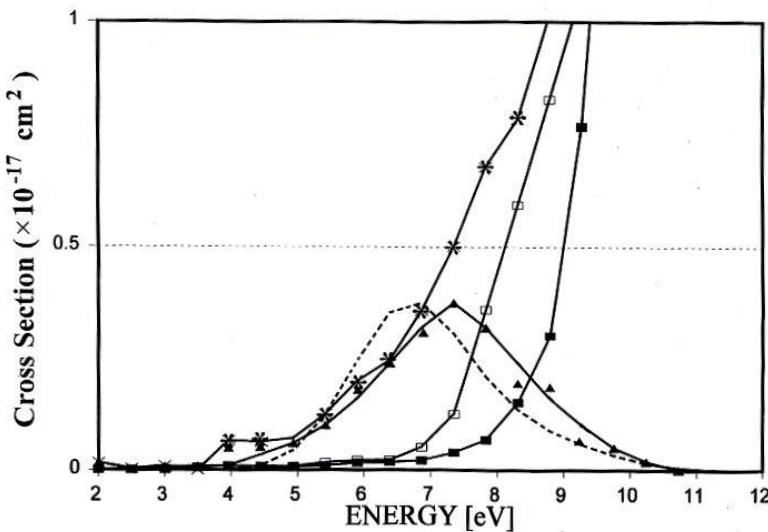
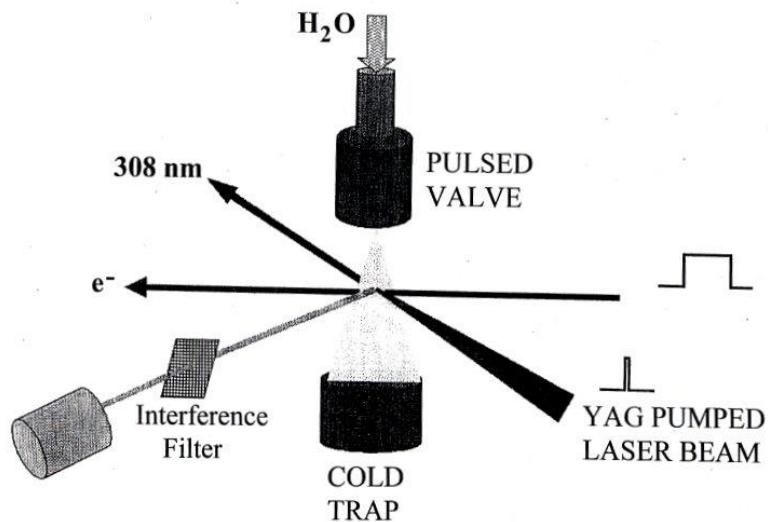
„Shape” resonances: experiment vs. theory (NF_3)



Calculations do not yield XS for resonant vibrational excitation (which is essentially unknown due to lack of experiments)

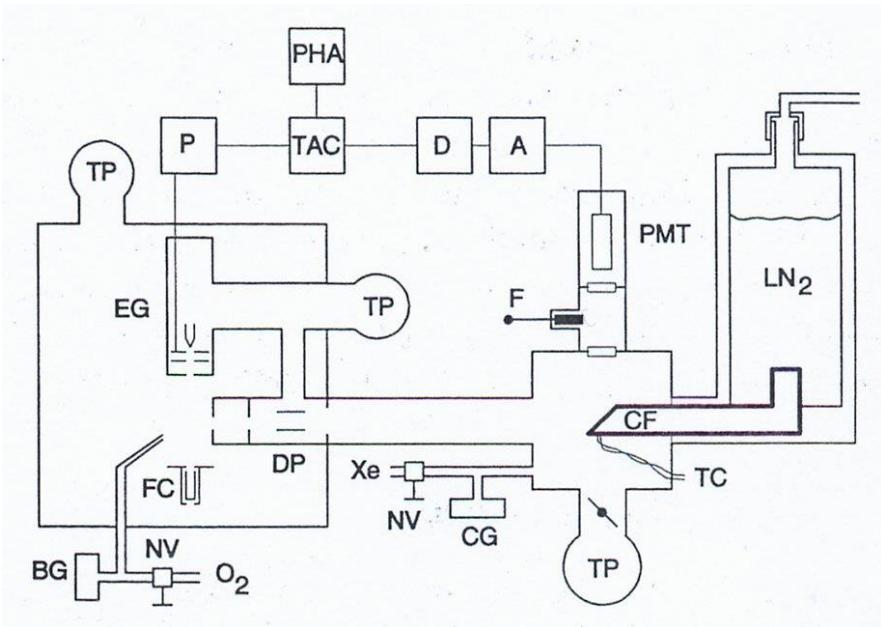
Dissociation into neutrals (H_2O)

Laser-induced fluorescence



Dissociation into neutrals (N_2O)

XeO^* excimer decay



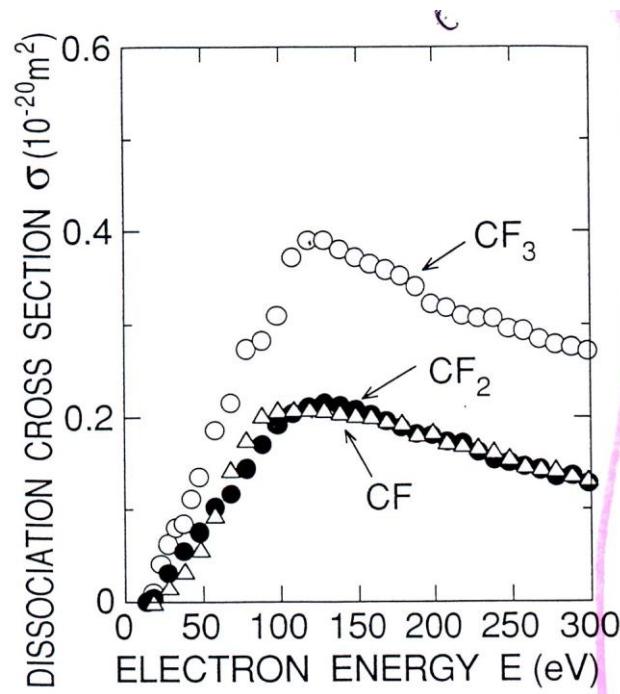
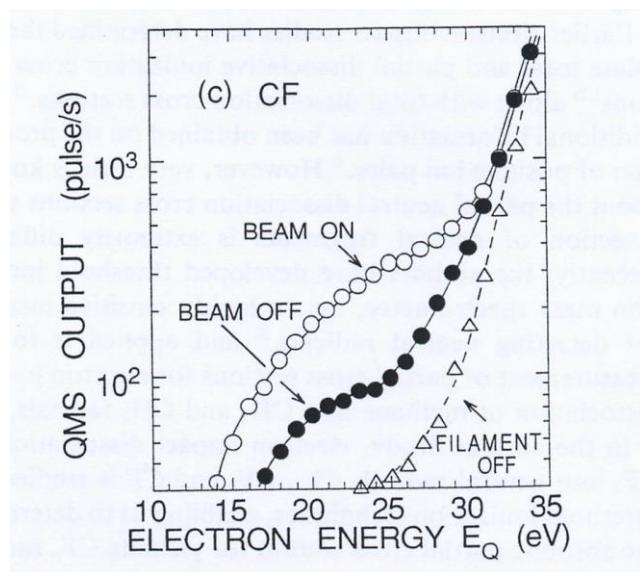
LeClair and McConkey JCP 99 (1993) 4566

TABLE I. Absolute cross sections for the production of $\text{O}(^1\text{S})$ following electron impact on $\text{O}(^3\text{P})$, $\text{O}_2(X^3\Sigma_g^-)$, and $\text{N}_2\text{O}(X^1\Sigma^+)$ in units of 10^{-18} cm^2 . The atomic oxygen data are taken from Ref. 57.

E (eV)	O	O_2	N_2O
4.4	0.54
4.8	1.30
5	1.60
6	2.57
7	3.02
8	3.22
9	3.28
10	3.27
12	3.15	...	5.12
14	2.97	...	9.52
16	2.79	0.35	13.8
20	2.44	0.92	18.1
24	...	1.26	20.5
28	...	1.47	21.7
32	...	1.61	22.2
36	...	1.73	22.4
40	1.37	1.82	22.4
45	1.21	1.92	22.5
50	1.07	1.97	22.4
60	...	2.04	22.2
70	0.69	2.07	21.7
80	...	2.08	21.1
90	...	2.06	20.6
100	0.38	2.04	20.1
120	...	1.98	18.9
140	...	1.90	18.0
160	...	1.82	17.1
180	...	1.75	16.3
200	0.08	1.67	15.6
250	...	1.53	13.9
300	...	1.39	12.8
350	...	1.26	11.8
400	...	1.16	11.0
450	...	1.08	10.3
500	...	1.02	9.60
600	...	0.92	8.63
700	...	0.82	7.91
800	...	0.75	7.39
900	...	0.69	6.88
1000	...	0.65	6.49

Dissociation into neutrals (CF_4)

Two electron beams: dissociation & ionization



Dissociation into neutrals (CF_4 , CH_3F ...)

„Volatile organotellurides”

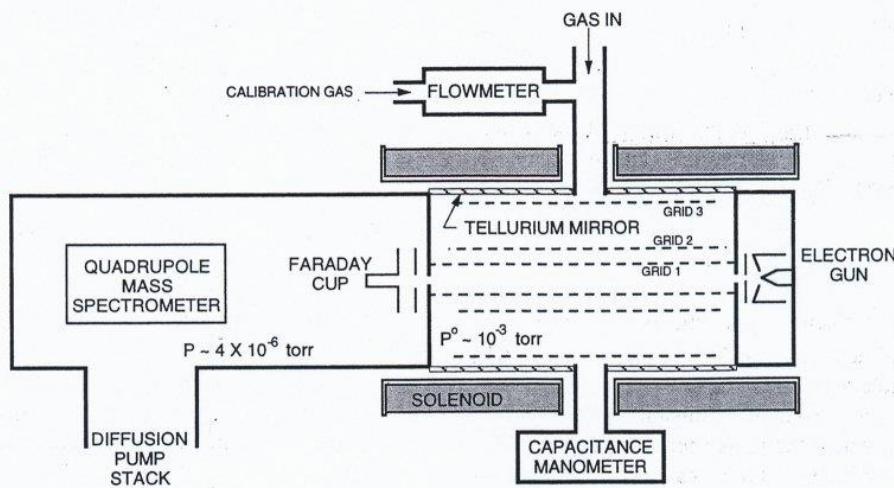


FIG. 1. Schematic diagram of the apparatus.

Motlagh and Moore JCP 109 (1988) 432

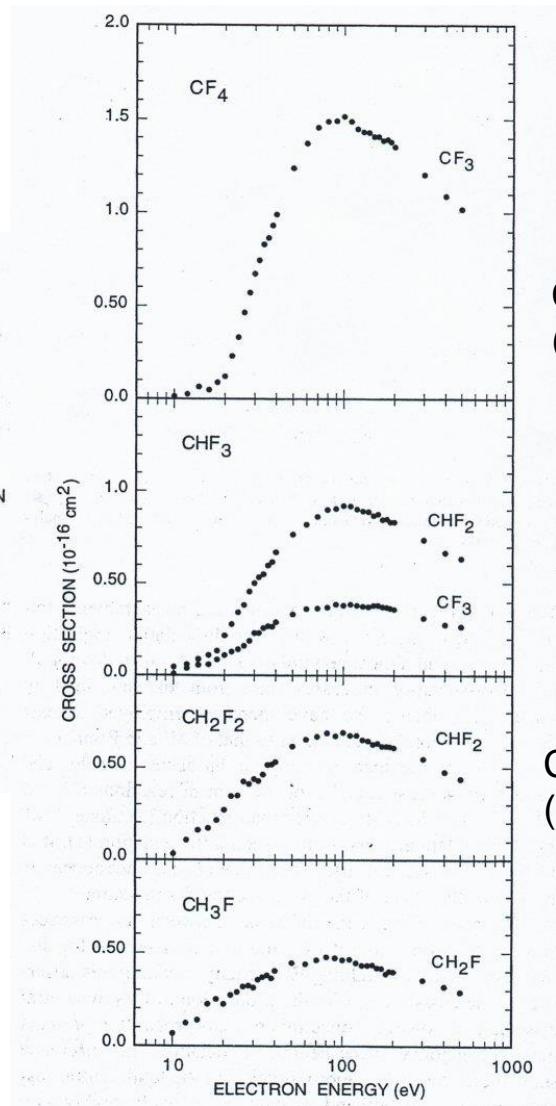
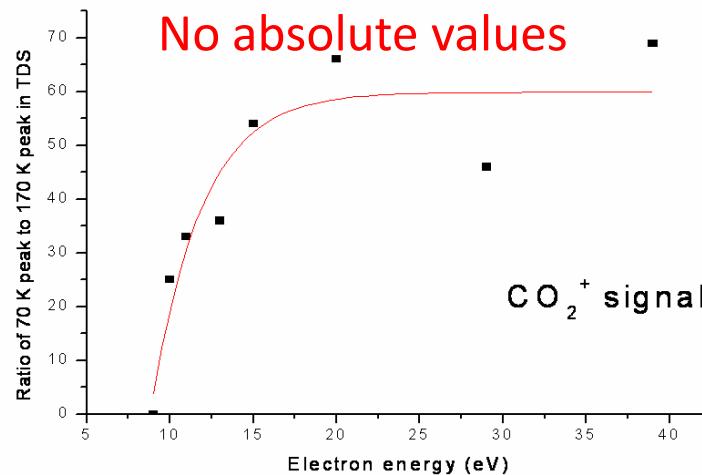
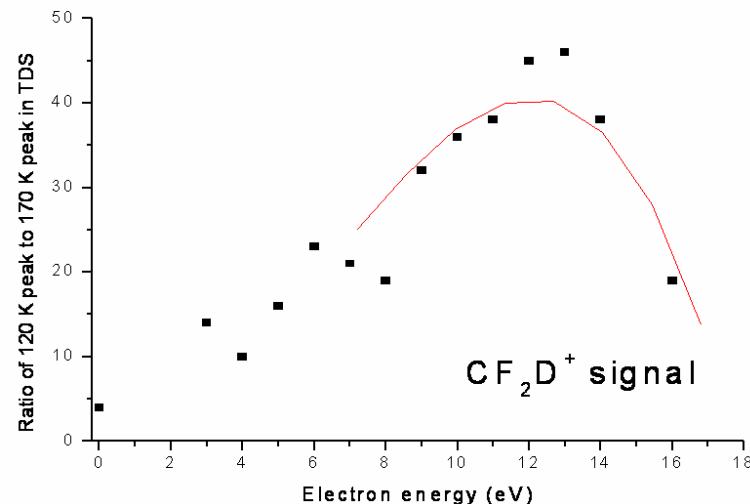
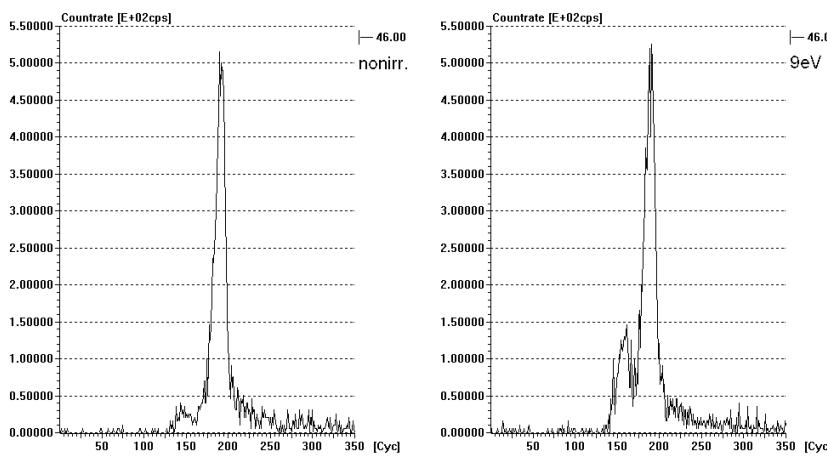
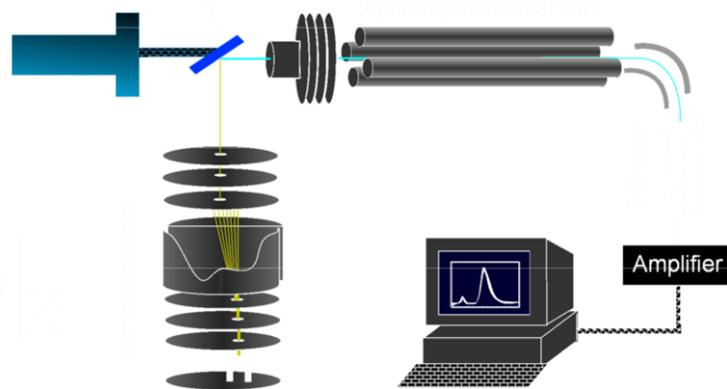


FIG. 5. Cross sections for the production of fluoromethyl radicals by neutral dissociation (n.d.) and dissociative ionization (d.i.) from electron impact on fluoromethanes.

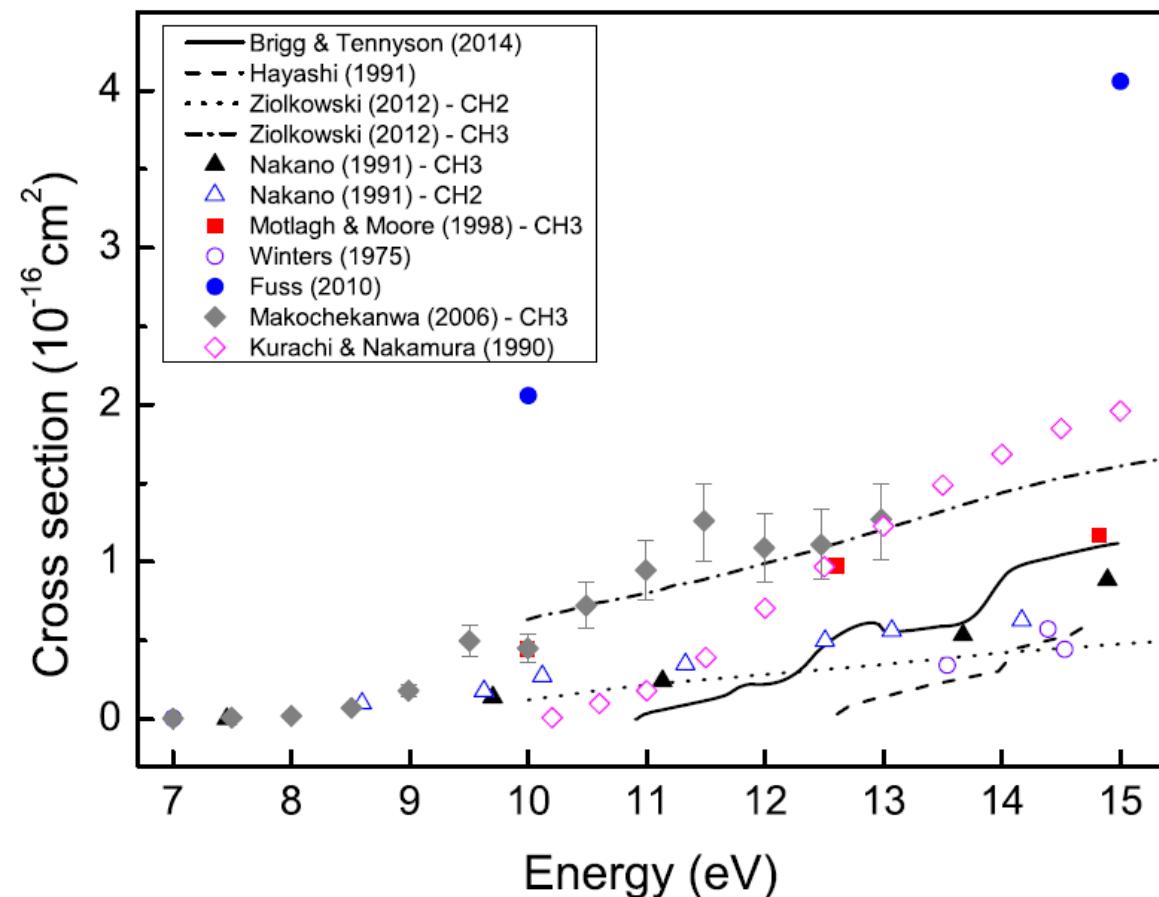
?

Dissociation into neutrals (CF_3COOH)

Cold deposition/ Electron
irradiation/ Thermal desorption



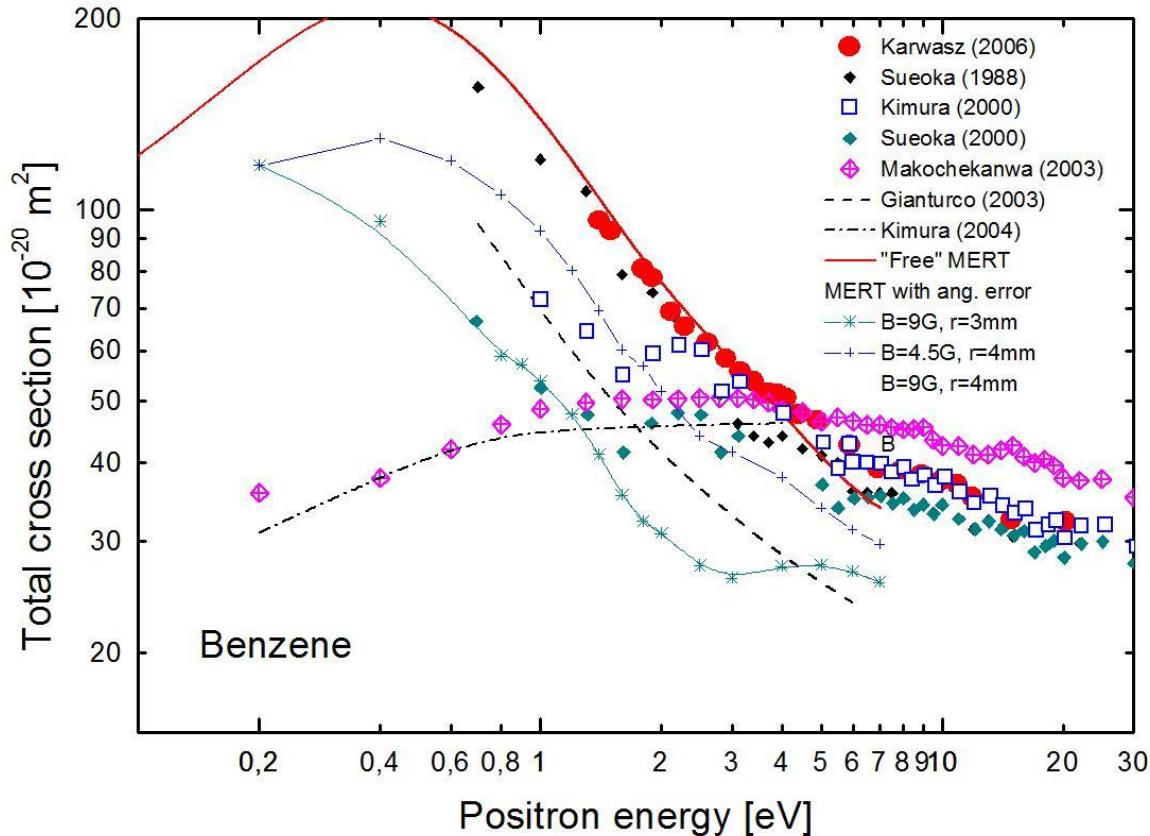
Dissociation into neutrals/ electronic excitation – theory & experiment (CH_4)



Experiments in serious disagreements;
Calculations Ziolkowski shifted by -3eV;
Briggs underestimated;

No recommended values were given

Total: Positron scattering (C_6H_6)



Modified effective range theory used to correct experimental data of Sueoka et al.

Kimura, Makochekanwa data come from Sueoka, but they published data obtained with a **higher guiding magnetic field**

Total: polar molecules

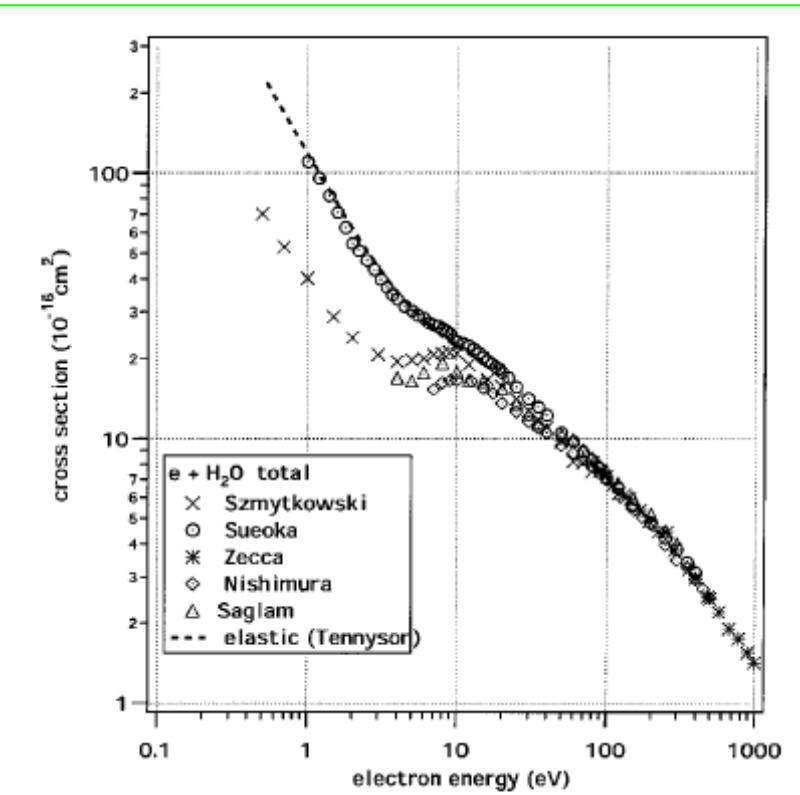
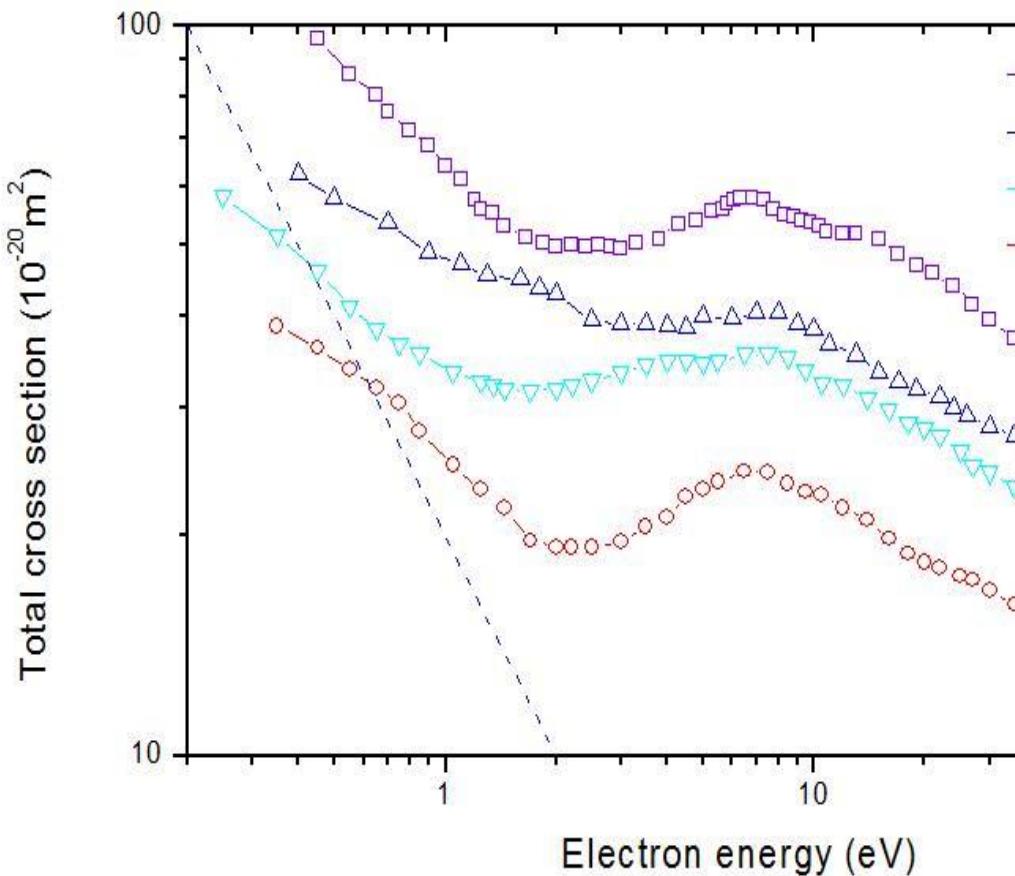
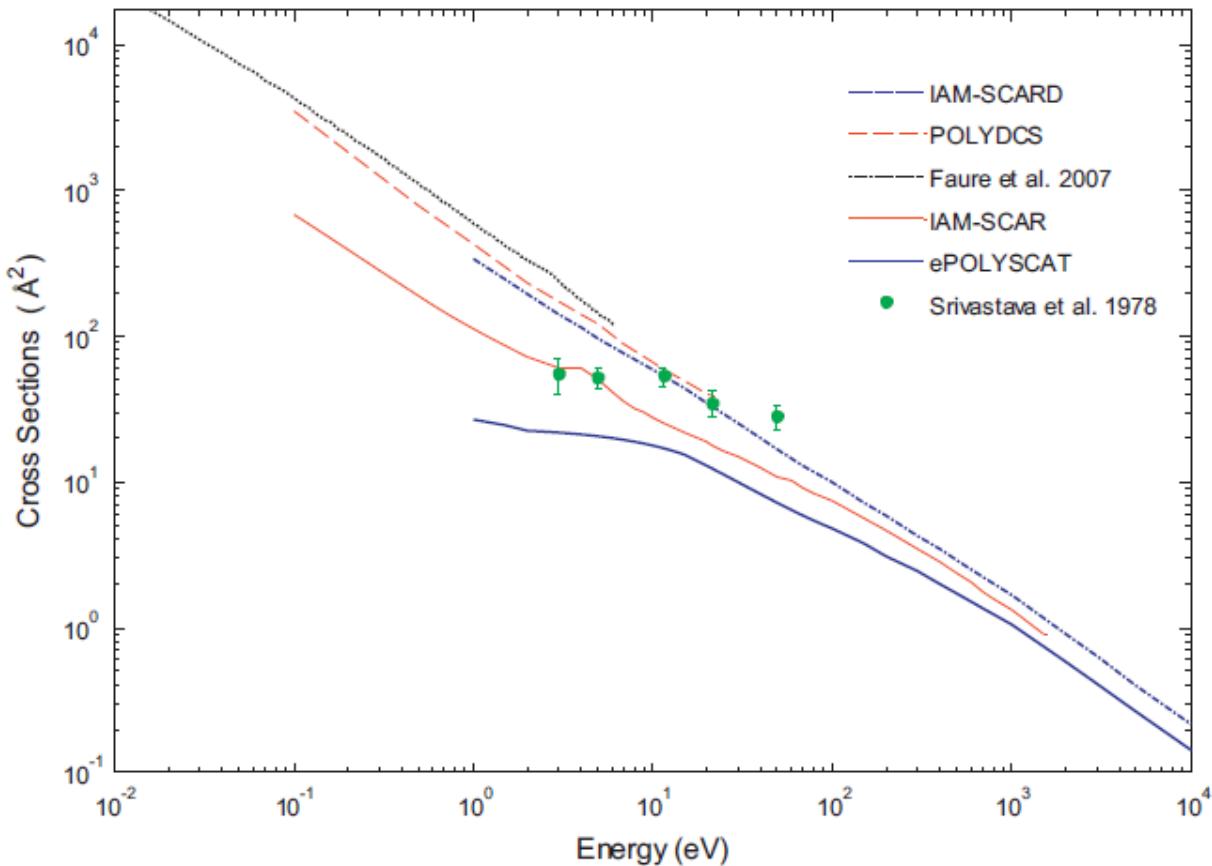


FIG. 2. Total scattering cross section, Q_T , of H_2O . A comparison is made of the experimental cross sections obtained by Szmytkowski (Ref. 21), Sueoka *et al.* (Ref. 26), Zecca *et al.* (Ref. 22), Nishimura and Yano (Ref. 23), and Saglam and Aktekin (Refs. 24 and 25). The theoretical elastic cross section obtained by Tennyson *et al.* (Ref. 28) is also shown for comparison.

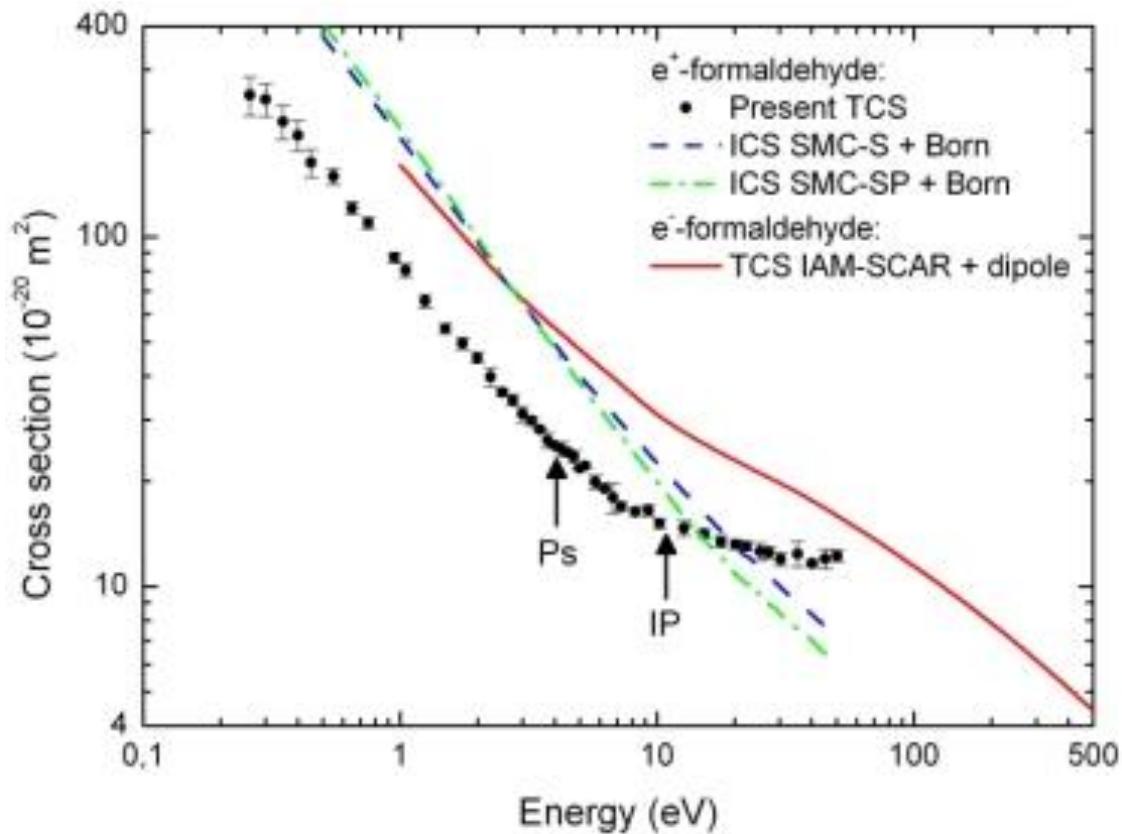
Total: polar molecules (HCN)

A.G. Sanz et al. / Applied Radiation and Isotopes 83 (2014) 57–67



As experimentalist
I would believe more
in theory than in
experiment

Polar molecules ($e^+/e^- + \text{HCOH}$)

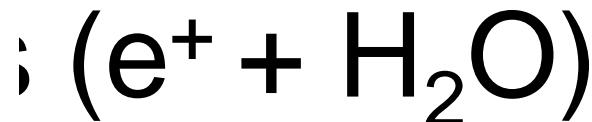
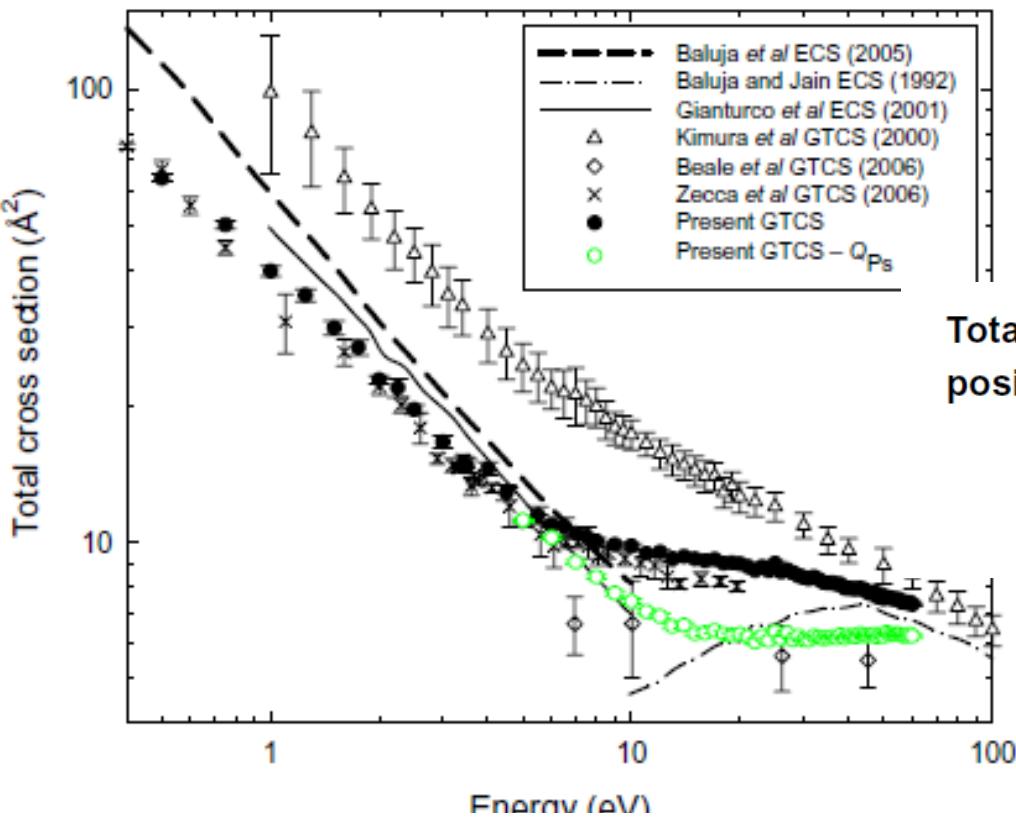


As experimentalist
I would believe more
in theory than in
experiment

Independent atom model-screened additivity rule / Schwinger multichannel

A Zecca, E Trainotti, L Chiari, G García, F Blanco, M H F Bettega, M T do N Varella, M A P Lima and M J Brunger

[Journal of Physics B: Atomic, Molecular and Optical Physics, Volume 44, Number 19](#)



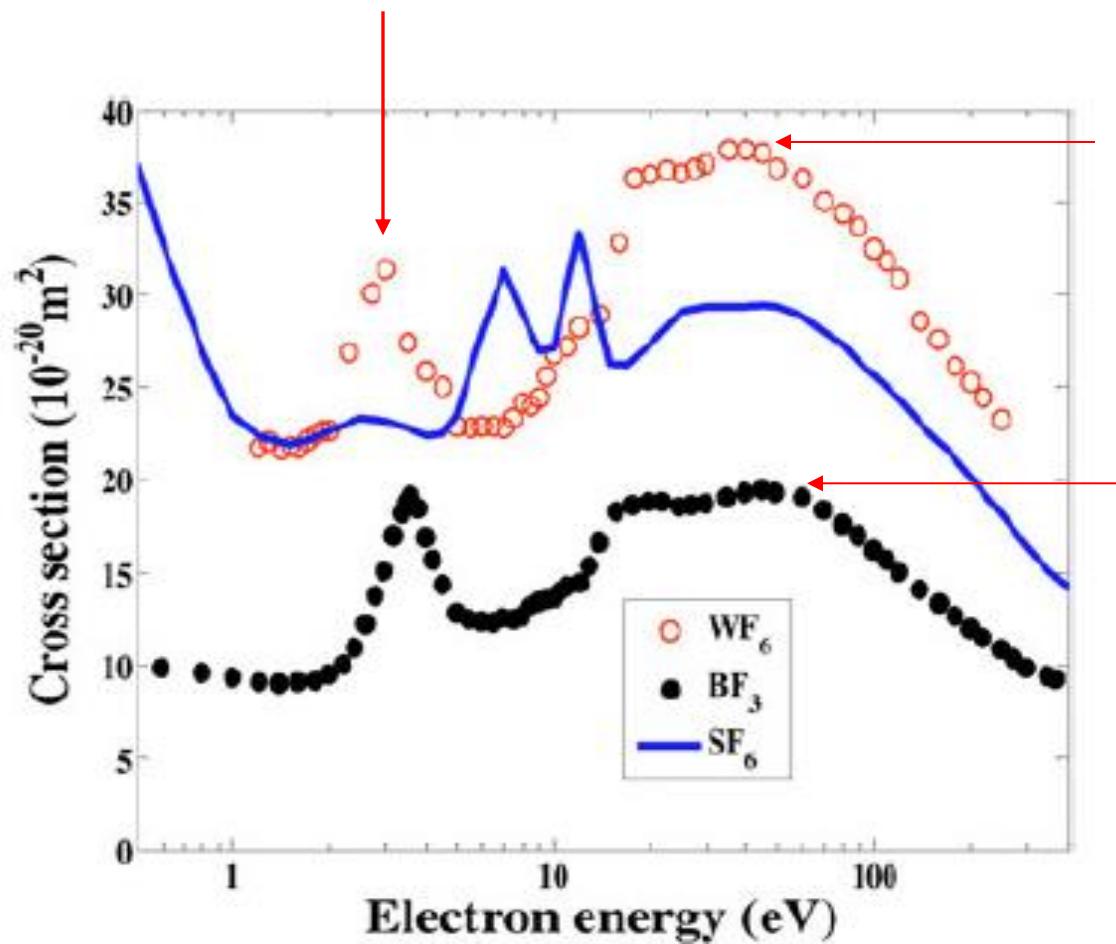
Total and positronium formation cross sections for positron scattering from H_2O and $HCOOH$

Casten Makochekanwa^{1,5}, Ana Bankovic², Wade Tattersall^{1,3}, Adric Jones¹, Peter Caradonna¹, Daniel S Slaughter¹, Kate Nixon⁴, Michael J Brunger⁴, Zoran Petrovic², James P Sullivan¹ and Stephen J Buckman¹

Table 2. H_2O positron impact GTCS (10^{-16} cm^2). Numbers in parentheses are the values after the forward scattering effect correction. Errors are as explained in the text.

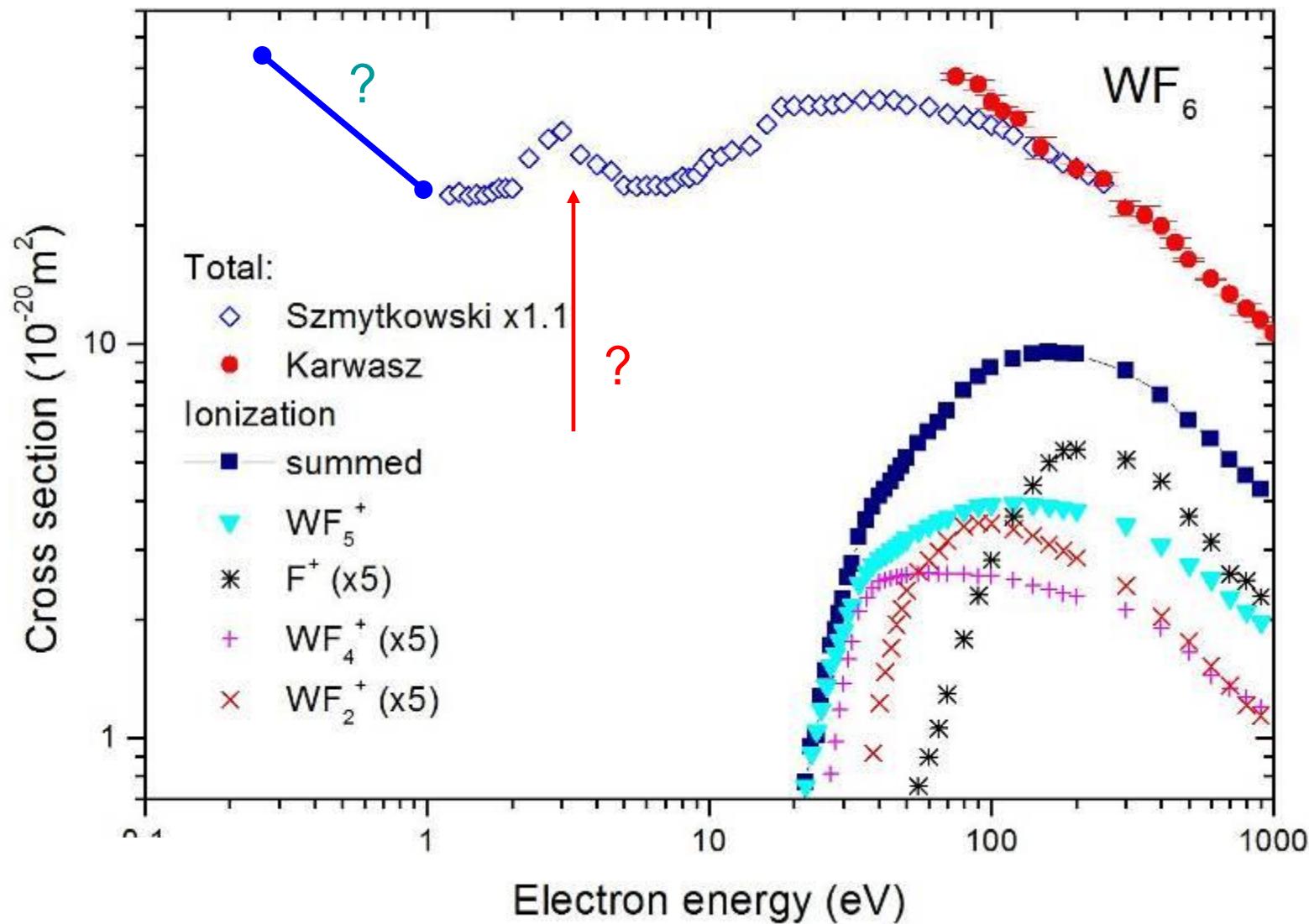
Energy (eV)	GTCS	Energy (eV)	GTCS
0.5	63.756(194.45) \pm 1.148(3.50)	25	8.985(11.38) \pm 0.119(0.15)
0.75	50.348(151.73) \pm 1.019(3.07)	26	8.598(10.81) \pm 0.120(0.15)
1	39.751(128.87) \pm 1.050(3.40)	27	8.694(10.86) \pm 0.125(0.16)
1.25	35.157(115.00) \pm 1.080(3.53)	28	8.569(10.64) \pm 0.136(0.17)
1.5	29.762(95.30) \pm 1.076(3.45)	29	8.432(10.41) \pm 0.125(0.15)

„Resonances” in total cross sections: WF_6

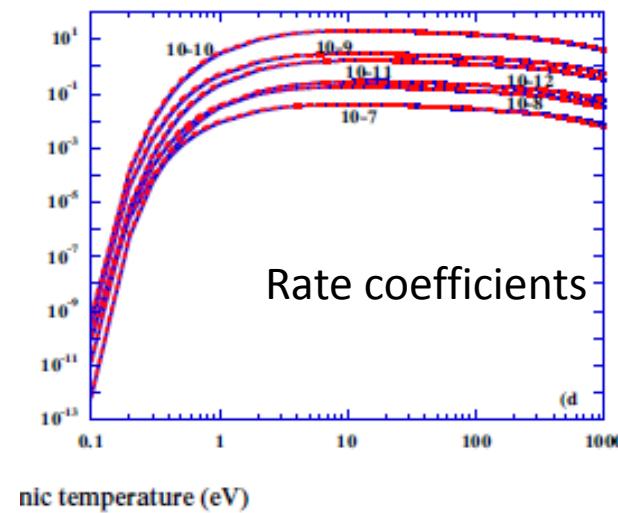
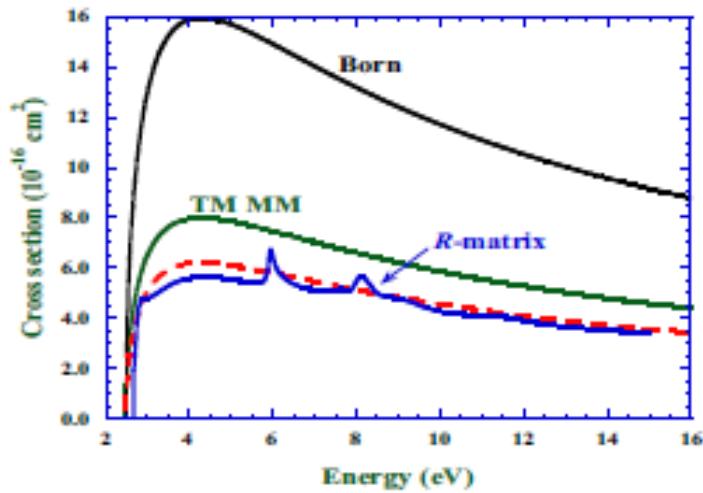
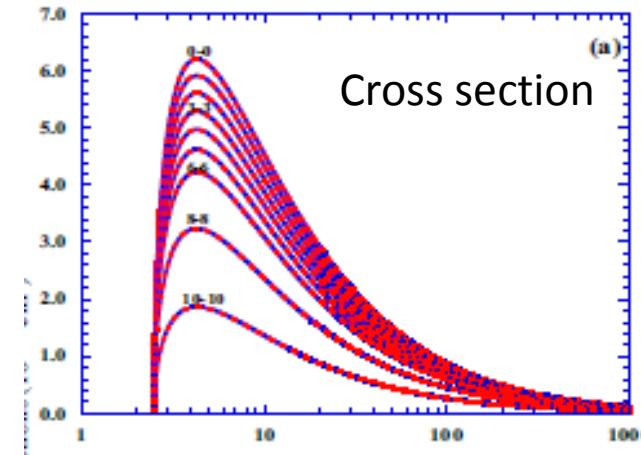
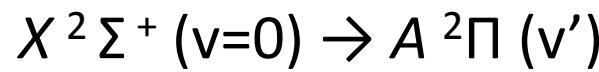
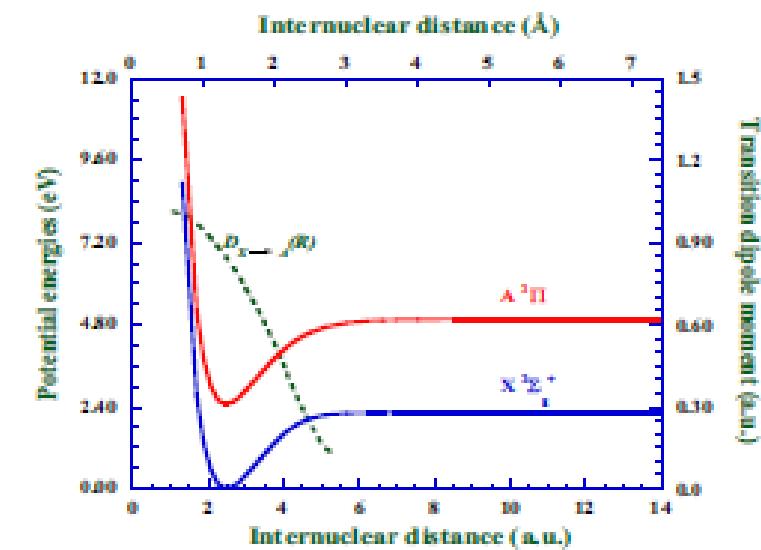


G. Karwasz, K. Fedus, FS&T (2013), experimental data: Szmytkowski and collaborators

WF_6 - few data



BeH: electronic and vibrational excitation



Beryllium

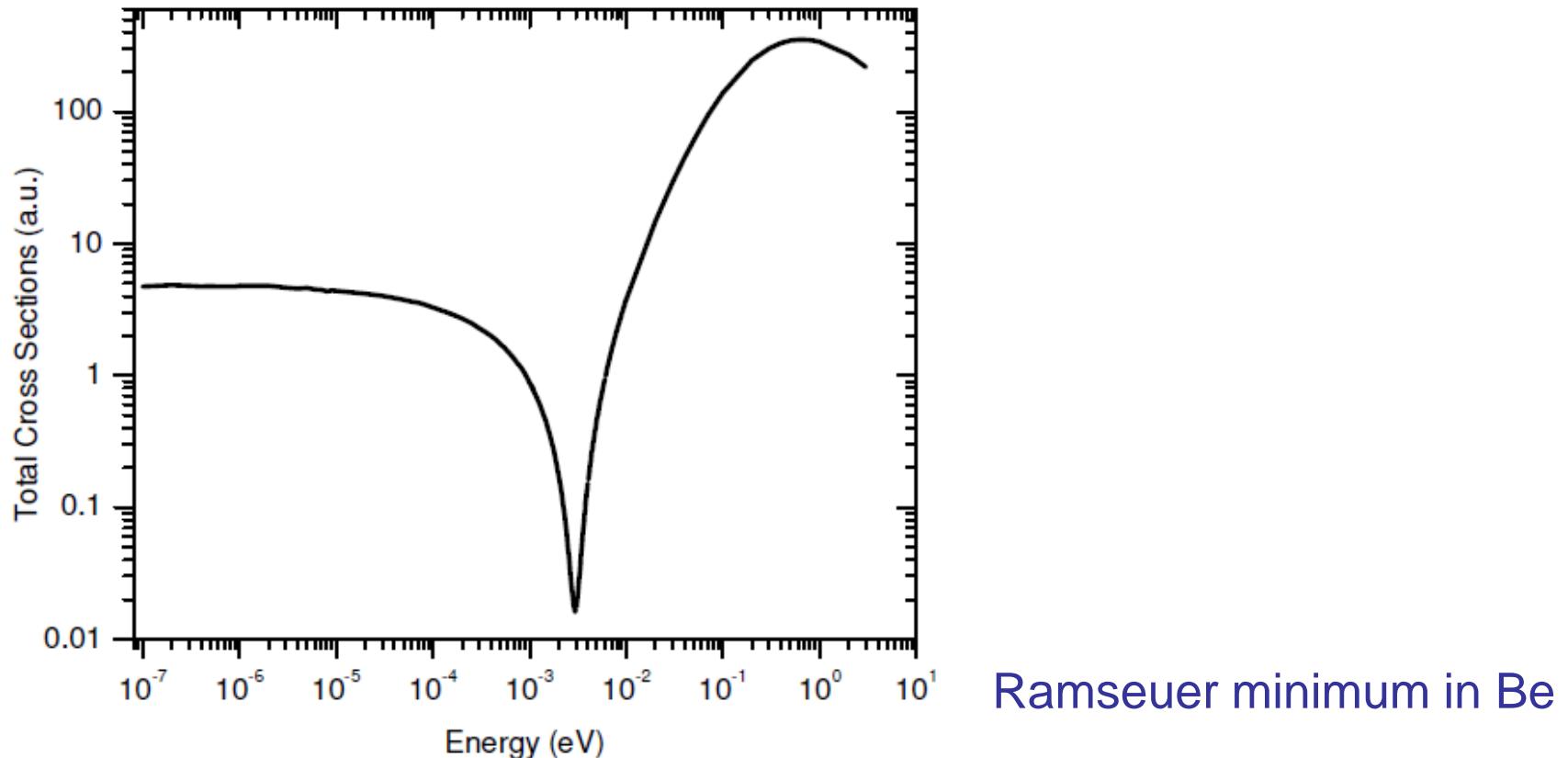


Figure 1. Total cross sections for low-energy electron scattering from atomic beryllium.

D. R. Reid, J. M. Wadehra, J.Phys. B 47 (2014)

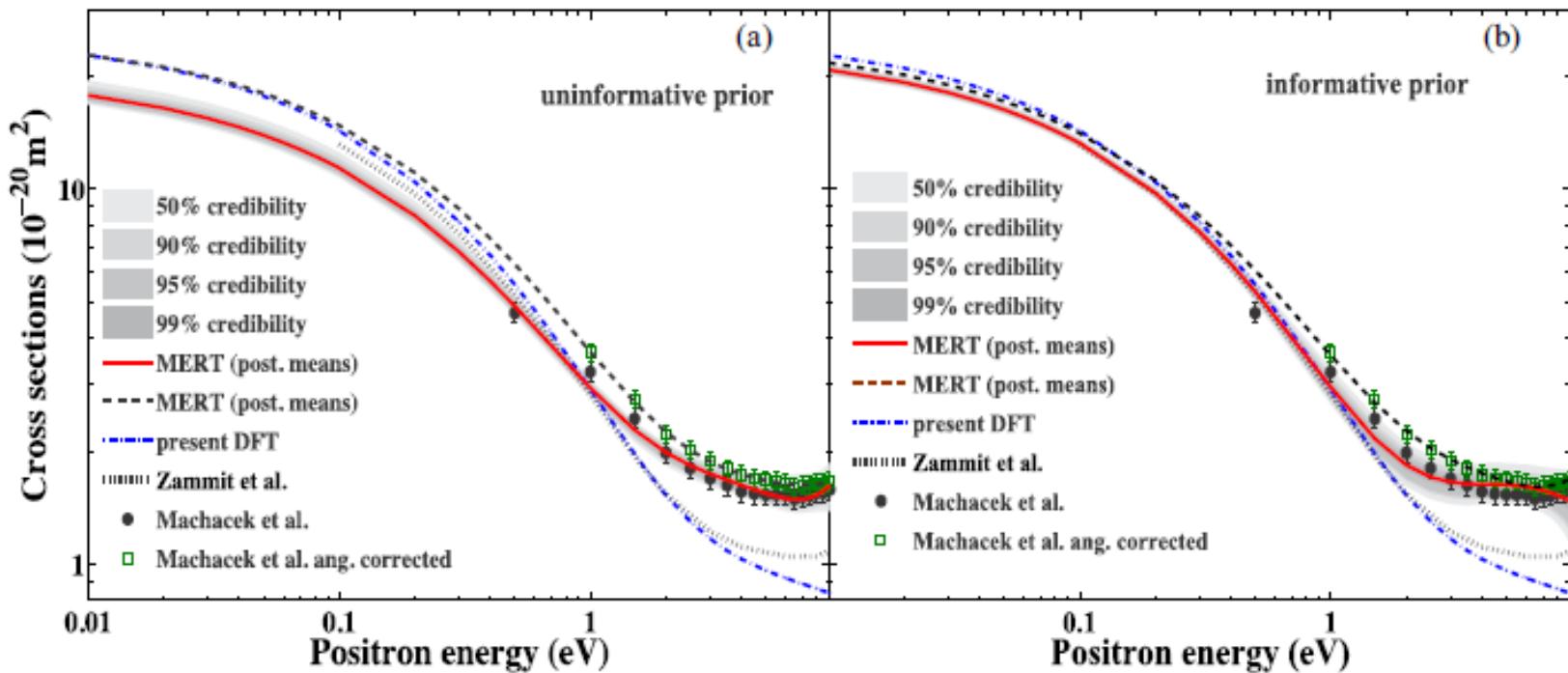
Positron + H₂: Bayesian analysis

PHYSICAL REVIEW A 91, 062701 (2015)

Positron scattering on molecular hydrogen: Analysis of experimental and theoretical uncertainties

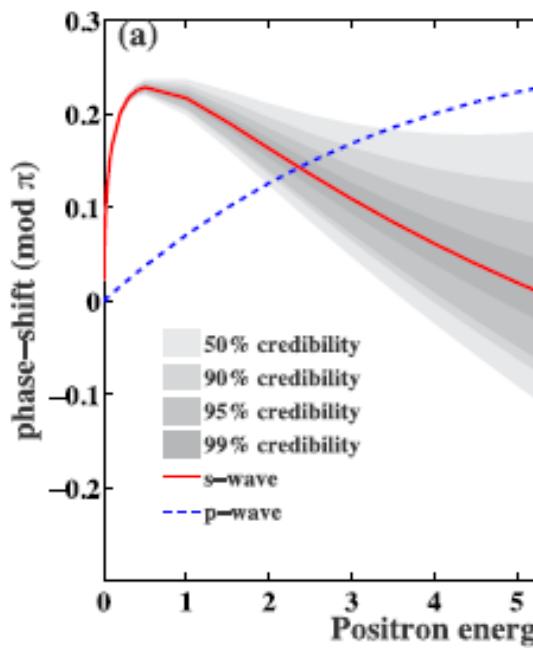
Kamil Fedus,^{1,*} Jan Franz,^{2,†} and Grzegorz P. Karwasz^{1,‡}

Total cross section



Positron + H₂: Bayesian analysis

Phase shifts



KAMIL FEDUS, JAN FRANZ, AND GRZEGORZ P. KARWASZ

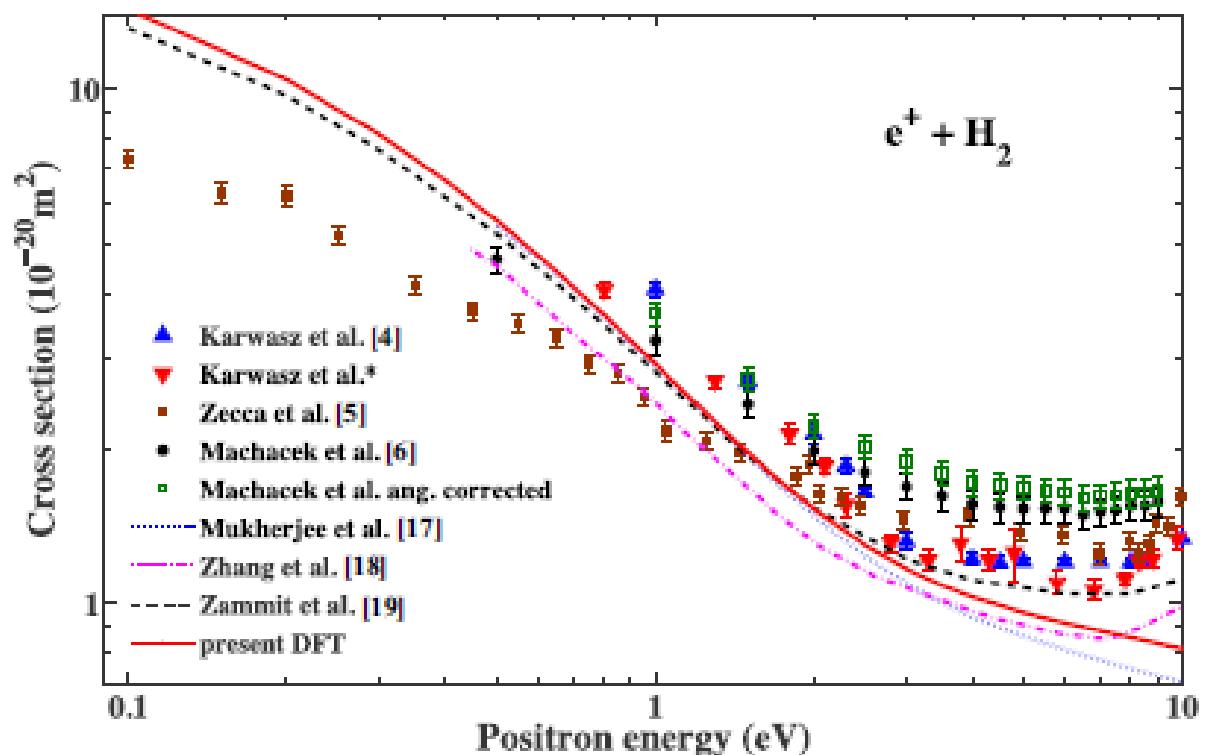
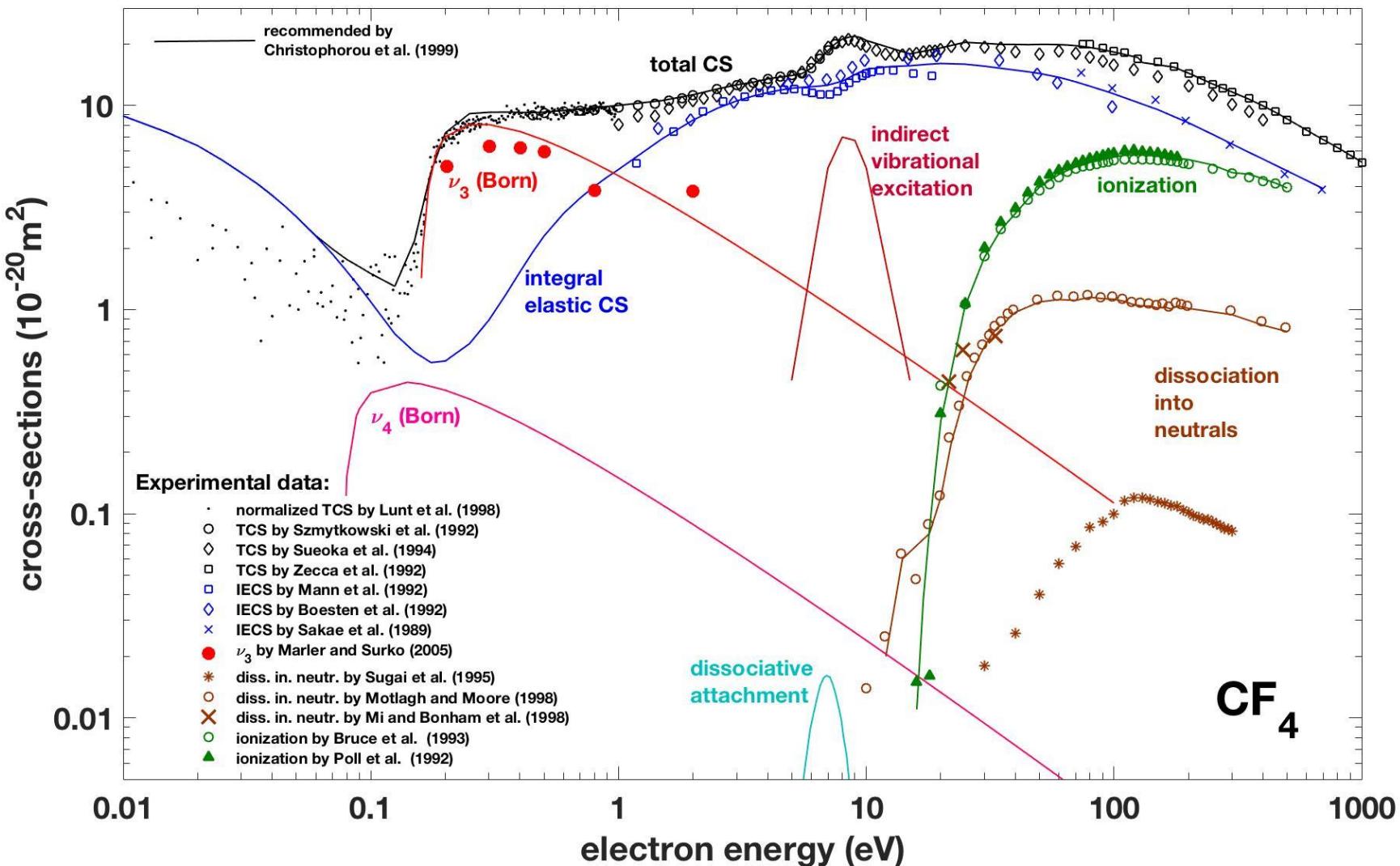


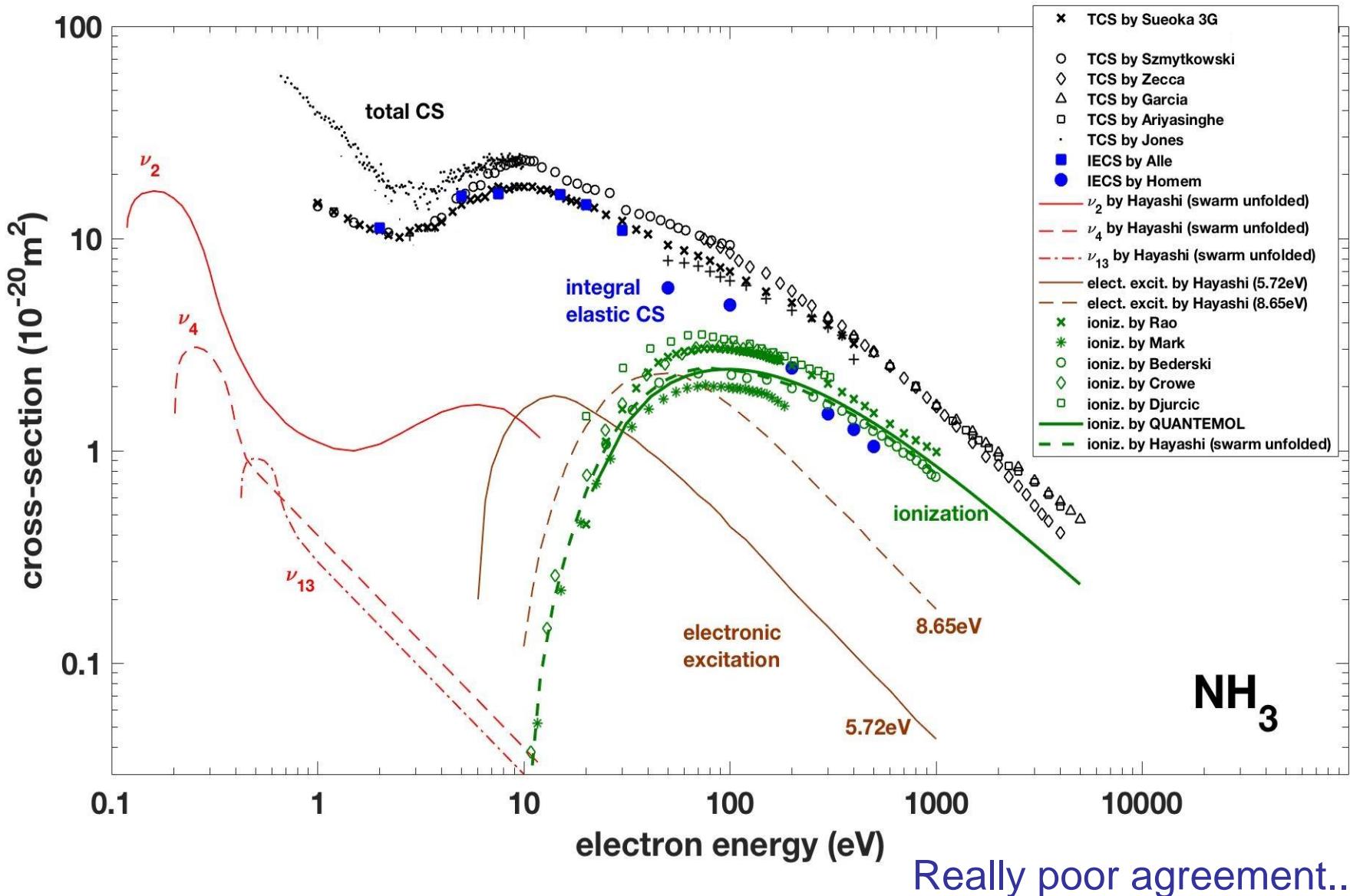
FIG. 3. (Color online) MERT-derived cross sections by Machacek *et al.* [6]: (a) direct phase shift only posterior mean values are given. The gray areas in the plot correspond to 50%, 90%, 95%, and 99% posterior regions due to uncertainties of MERT parameters.

Bayesian analysis does not help much when experiments are uncertain

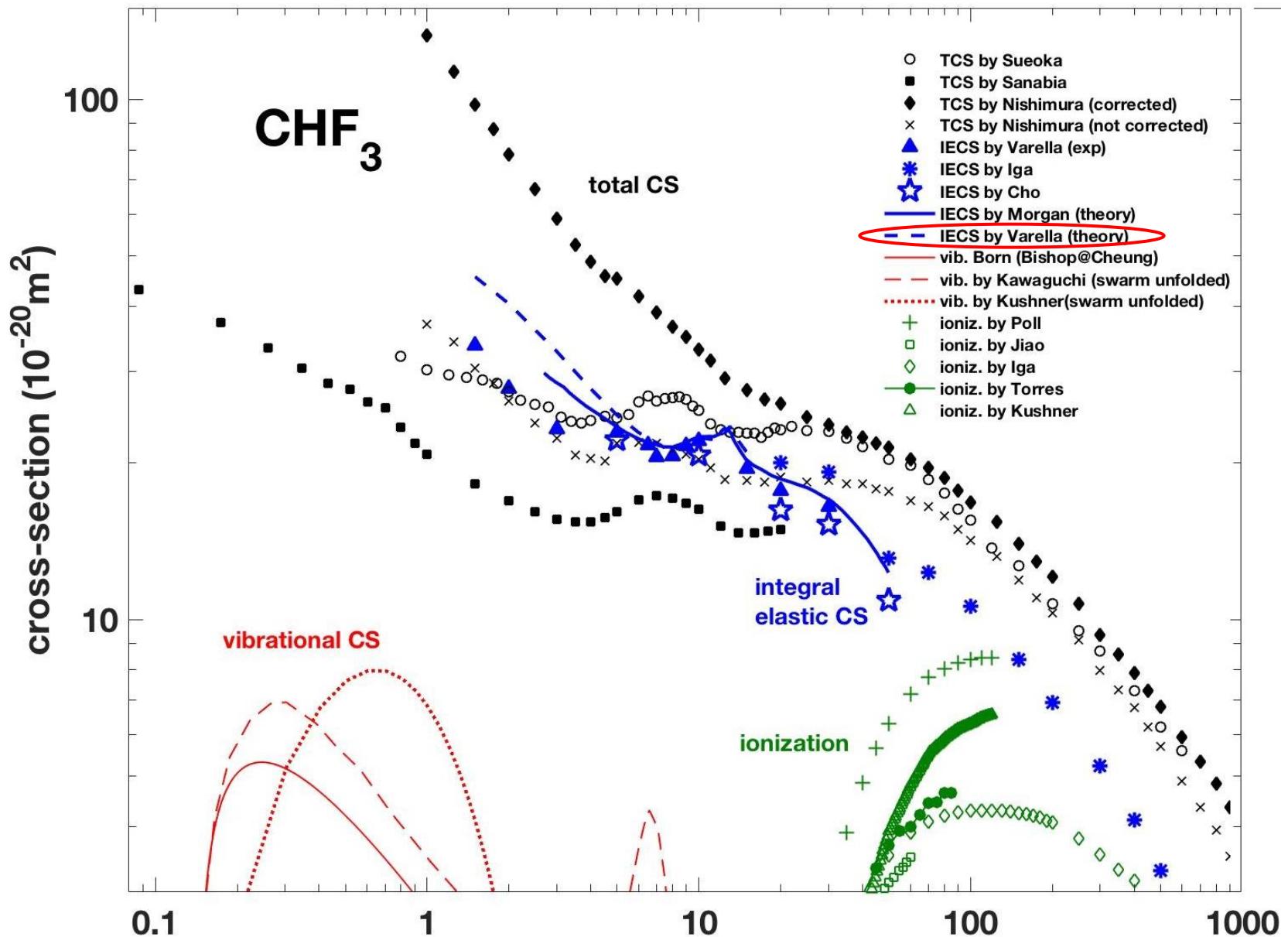
Check of congruence: CF_4 (\checkmark)



Check of congruence: NH₃ (X)



Check of congruence: CHF₃ ✕ ✕



Experimental uncertainties for electron scattering on molecules

- Total, in majority cases, within $\pm 5\%$
but no data for BeH, WH₂, few WF₆
- Ionization: total within $\pm 10\%$; in agreement with theories
but partial $\pm 15\%$
- Electronic excitation: good agreement between experiment and theory only of H₂
- Vibrational excitation: poorly understood at resonances
- Dissociation into neutrals desperately needed

Conclusions (II)

- Some targets possible for theory, other for experiments
- Solution: **commissioning measurements;**
- - NH₃ vibrational and electronic excitation (Fullerton California?)
- - BeH₂ elastic theoretical (Prague University?)
- - BeH₂ electronic excitation (?)
- - polar molecules (NH₃) at low energies (UNC Toruń?)
- - H vs defects in tungsten (positron beam: Trento University, TUV München, UNC Toruń)

**Thank for your attention,
and IAEA staff for welcome**