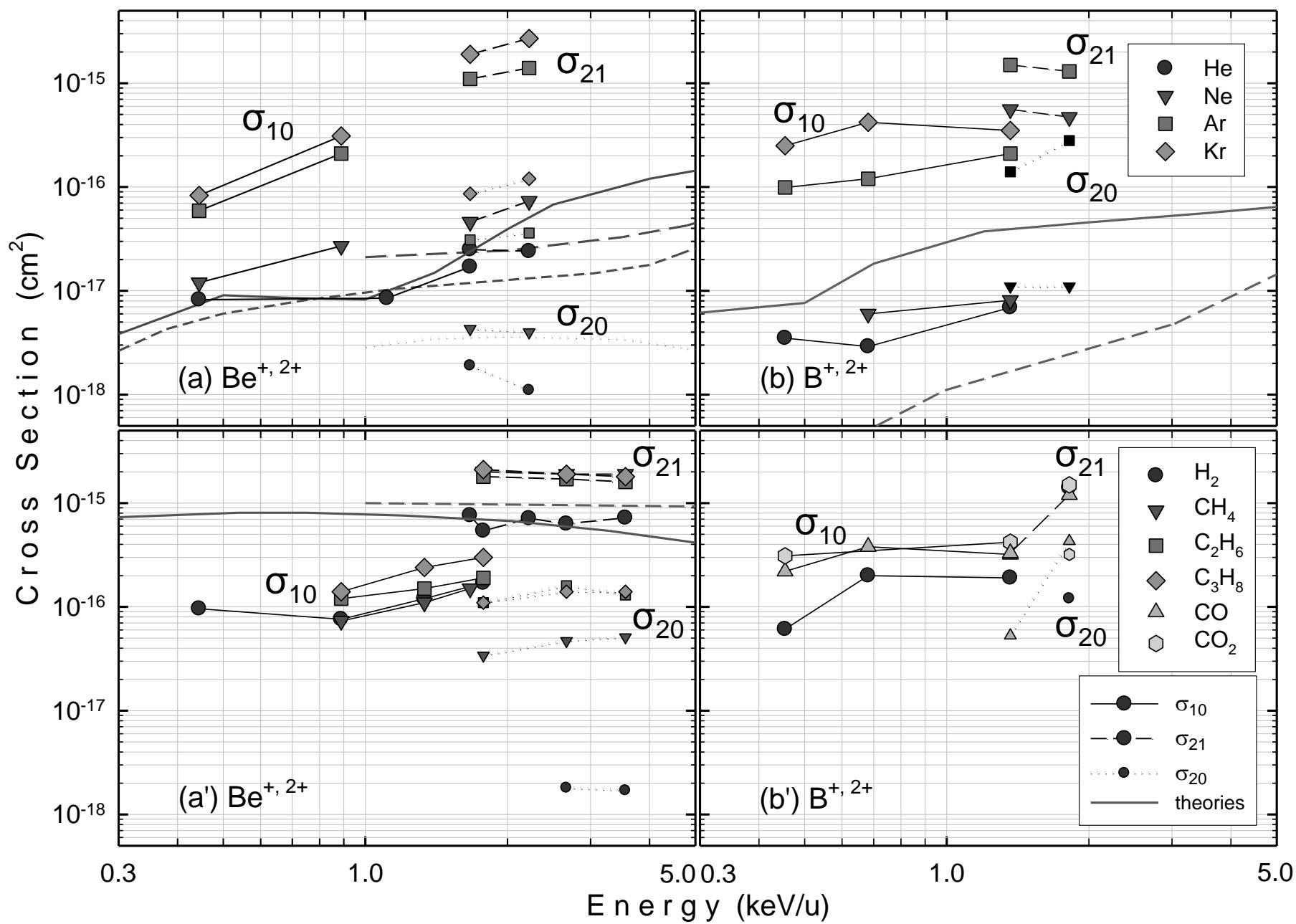


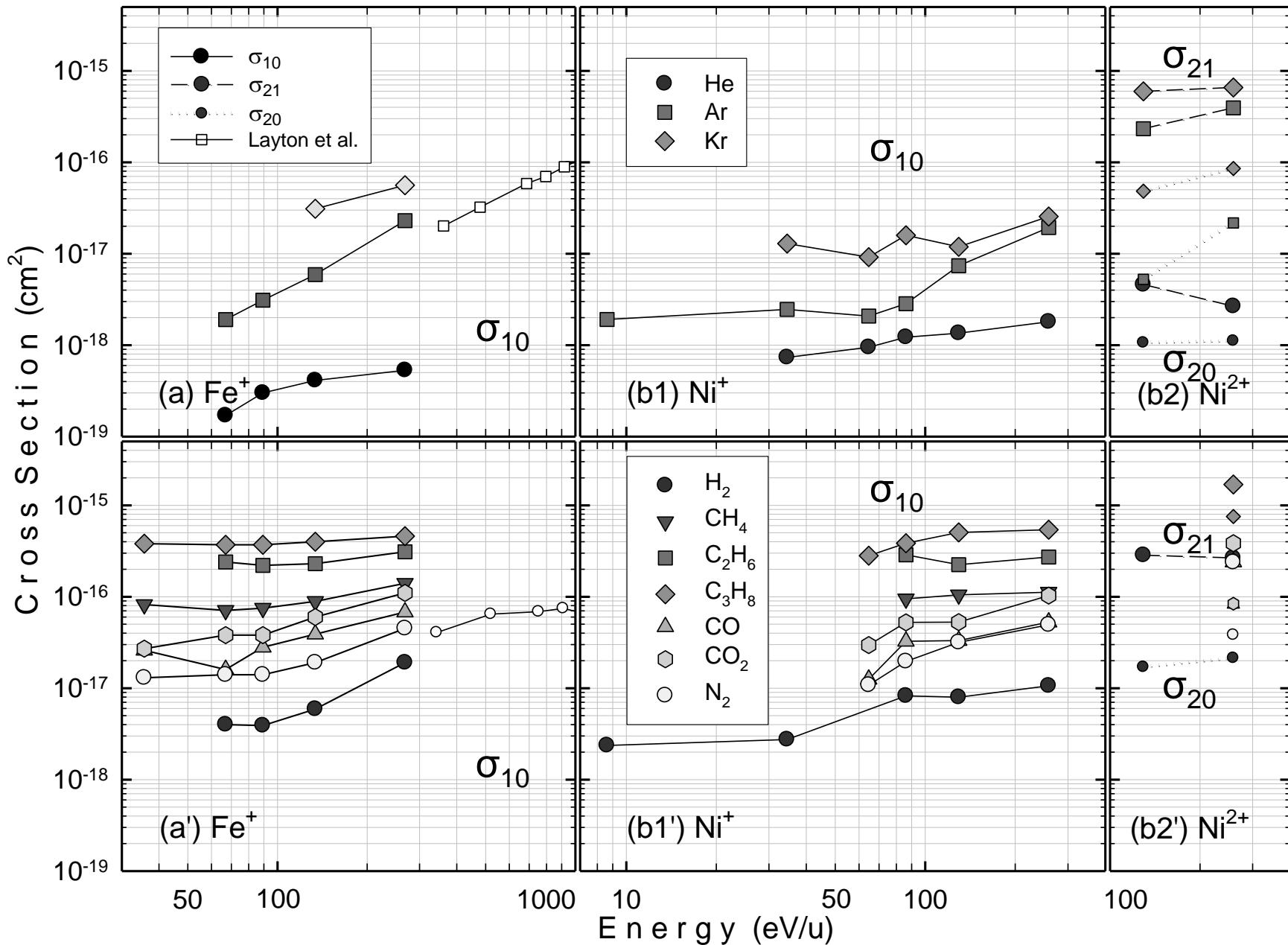
# First Step Benchmark of Inelastic Collision Cross Sections for Heavy Ions using Charge State Evolutions via Target Penetration

Alex M Imai, Viatcheslav P Shevelko

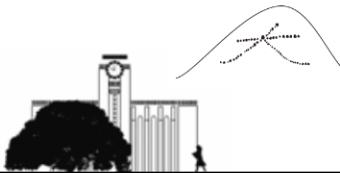
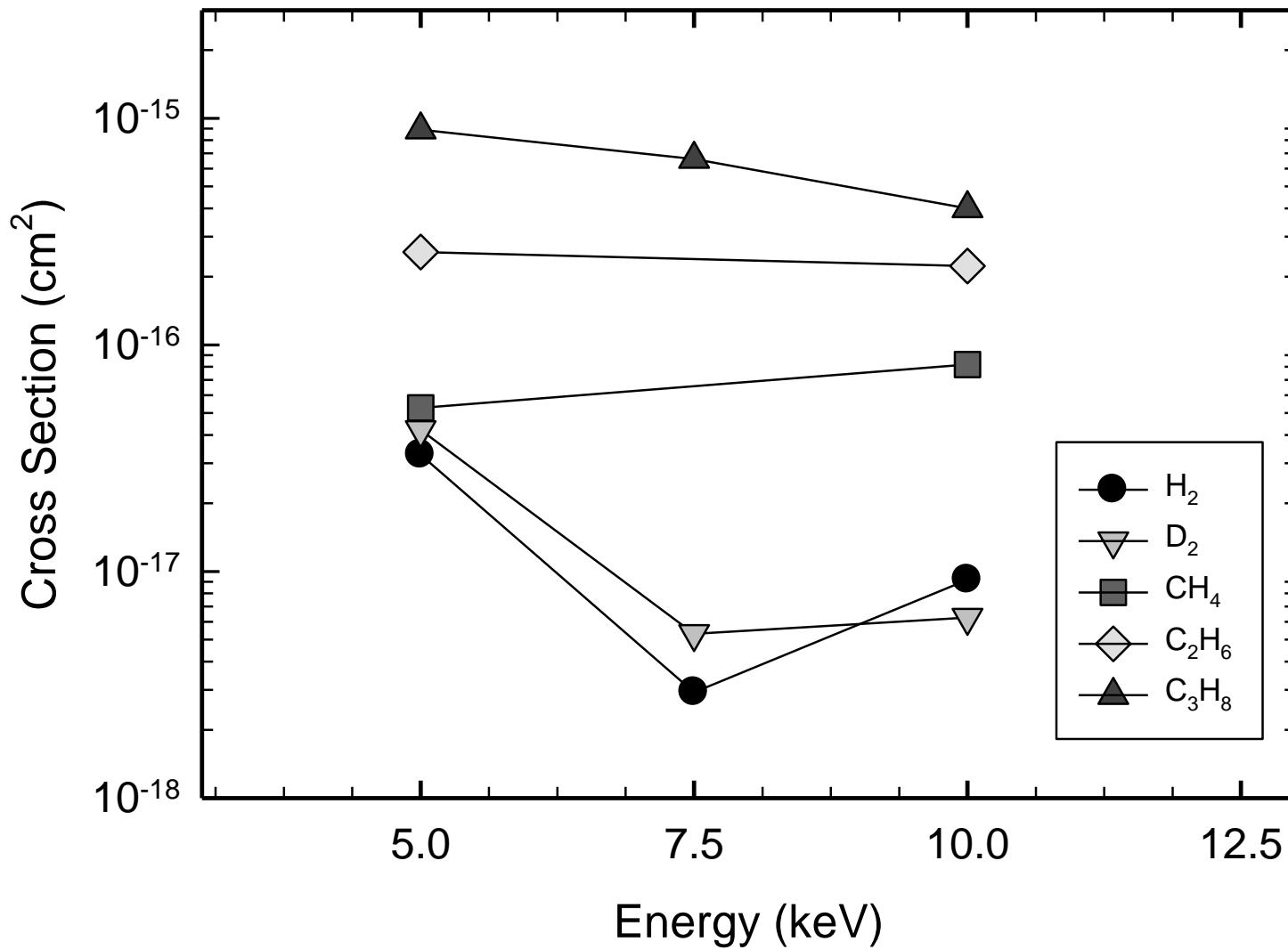
Department of Nuclear Engineering, Kyoto University  
P. N. Lebedev Physical Institute of Russian Academy of Sciences







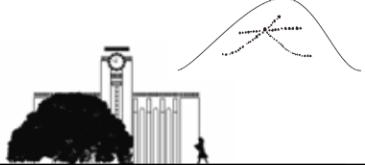
# Single-electron capture cross sections for W<sup>+</sup> ions



# Background

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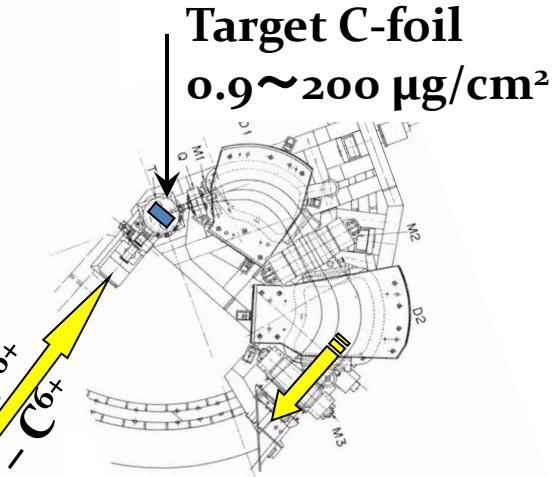
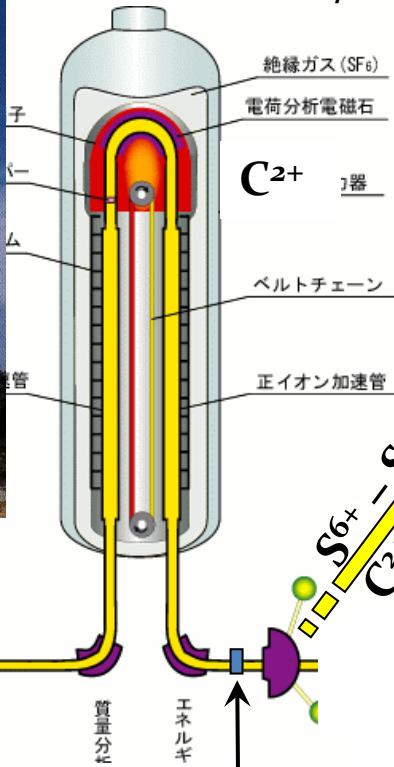
- You require not just accuracy of calculated cross sections but also their completeness.
- Experimentalists would like the evaluation of theoretical data to be done with experiments, but in many cases, there exist few experiments directly comparable to theories.
- Experimentalists are able to provide very accurate experimental results in some cases.



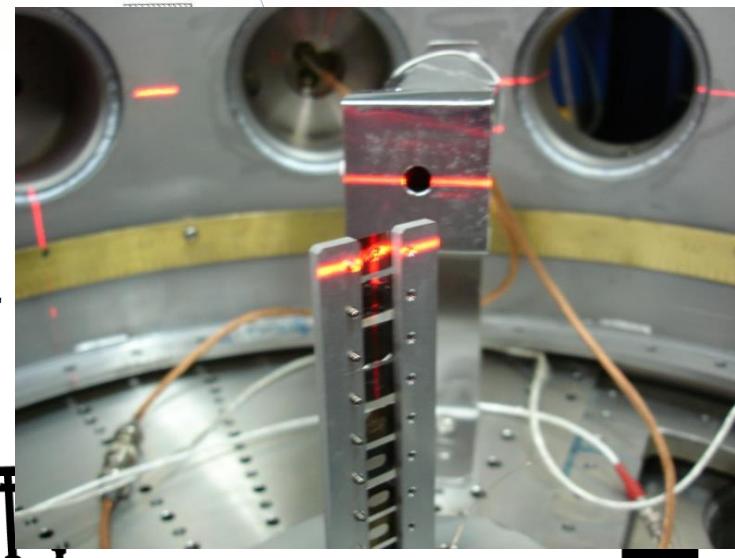
# Experimental apparatus in Japan Atomic Energy Agency



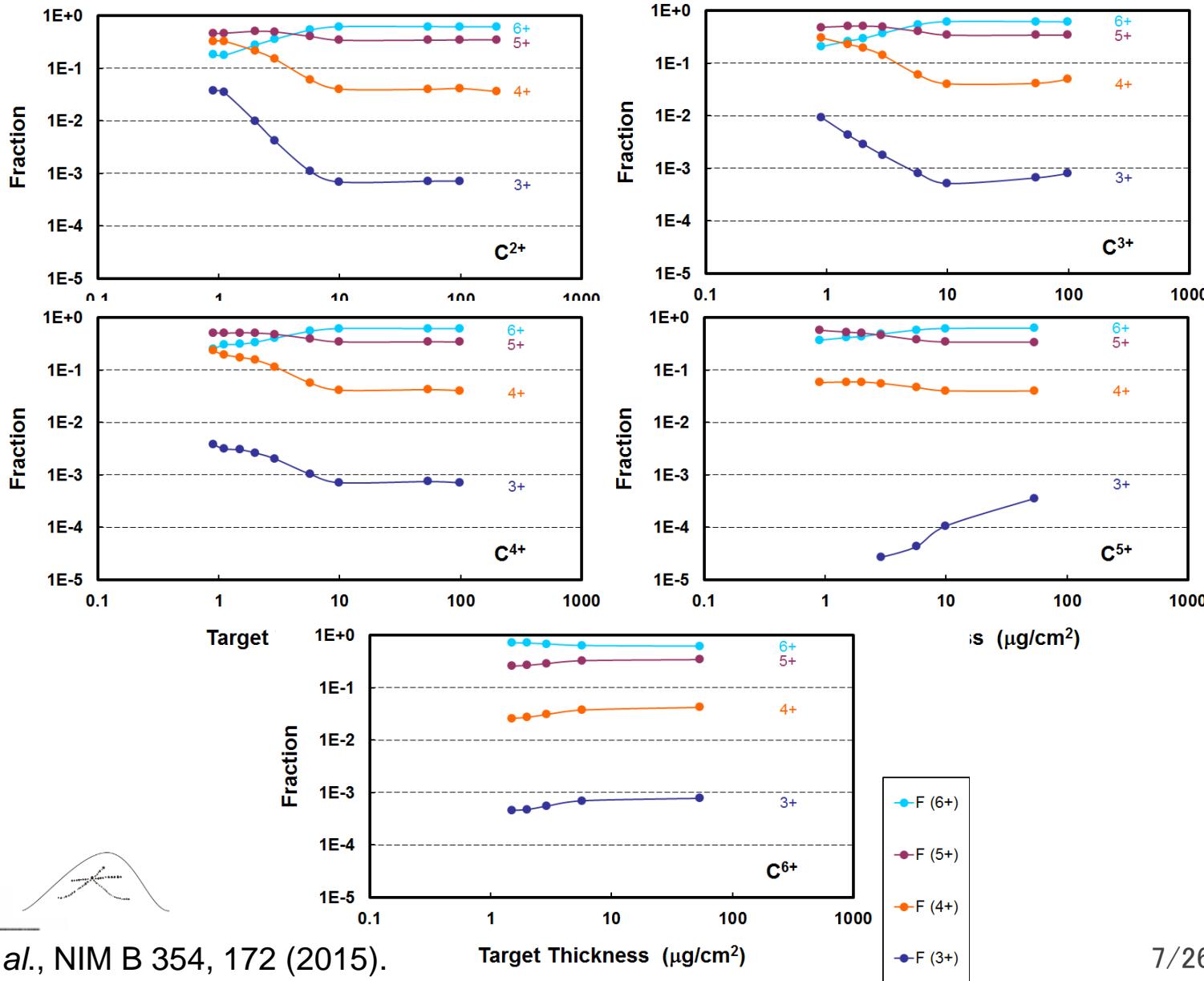
2.0 MeV/u  $C^{q+}$  ( $q=2\text{-}6$ ),  $S^{q+}$  ( $q=6\text{-}16$ ),  
1.0 MeV/u  $W^{q+}$  ( $q=13, 15, 28, 29, 30, 38$ )



$S^-$ ,  $W^-$   
—  
Post-stripper  
C-foil  $\sim 20 \mu g/cm^2$

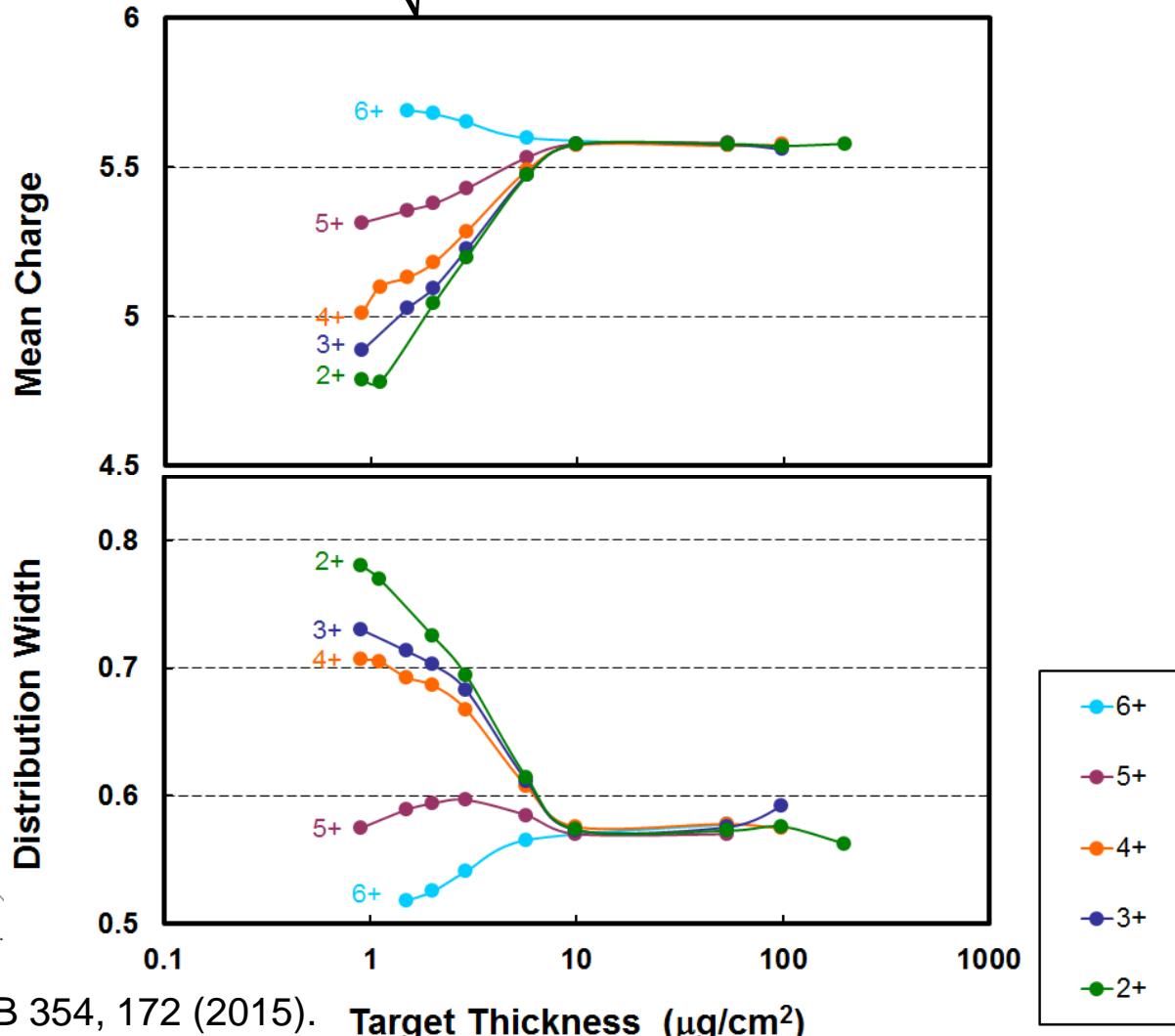


# Equilibrium and pre-equilibrium charge-state distributions of 2.0 MeV/u C ions after C-foils



# Equilibrium and pre-equilibrium charge-state distributions of 2.0 MeV/u C ions after C-foils

$$\bar{q} = \sum_q q y_q, \quad d = \sqrt{\sum_q (q - \bar{q})^2 y_q}, \quad s = \frac{\sum_q (q - \bar{q})^3 y_q}{d^3}$$



# Computer codes for charge-state evolutions



ETACHA:

a program for calculating charge states at GANIL energies, (10 – 80 MeV/u)

J.-P. Rozet, C. Stéphan, D. Vernhet, NIM B 107, 67 (1996).



Matrix Method:

Charge evolution of swift-heavy-ion beams explored by matrix method,

O. Osman, P. Sigmund, NIM B 269, 813 (2011).

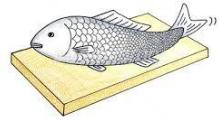
ETACHA3, **ETACHA4**: Extension of charge state distribution calculations for ion-solid collisions towards low velocities and many-electron ions,  
E. Lamour, P. D. Fainstein, M. Galassi, C. Prigent, C. A. Ramirez,  
R. D. Rivarola, J.-P. Rozet, M. Trassinelli, D. Vernhet, PRA 92, 042703 (2015).



BEAR (Balance Equations for Atomic Reactions)  
**V. P. Shevelko**, N. Winckler, I. Yu. Tolstikhina,  
NIM B 377, 77 (2016).



# Set of cross sections on the cutting-board

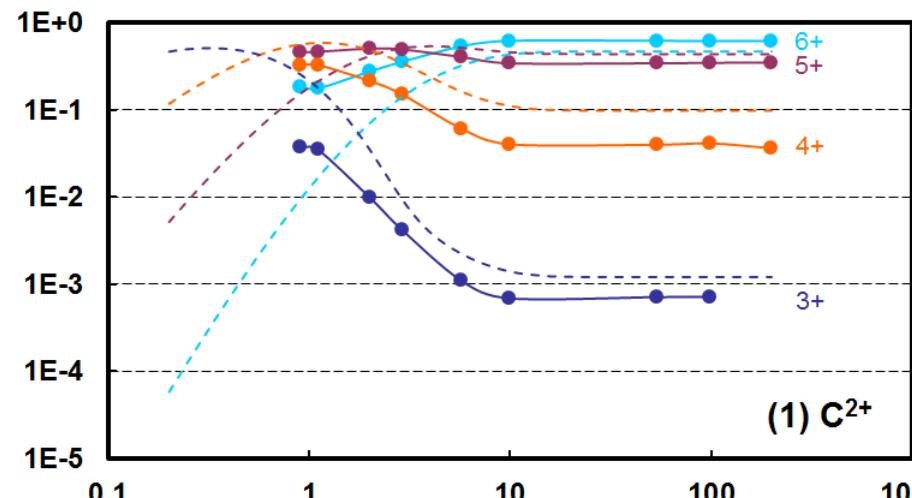


Case	Cross Sections	References	Accuracy
(1) - (3)	e-cap. OBK e-loss relativistic Born ex. relativistic Born	JPB37,201(2004) JETP119,1(2014) NIMB184,295(2001)	50% 30-50% 30-50%
(4)	$\frac{dy_i}{dx} = \sum_{i \neq j} y_j(x) \sigma_{ji} - \sum_{i \neq j} y_i(x) \sigma_{ij}$	$\sum_i y_j = 1$	Scaling used partly
ETACHA	REF. Bethe-Salpeter	1957	

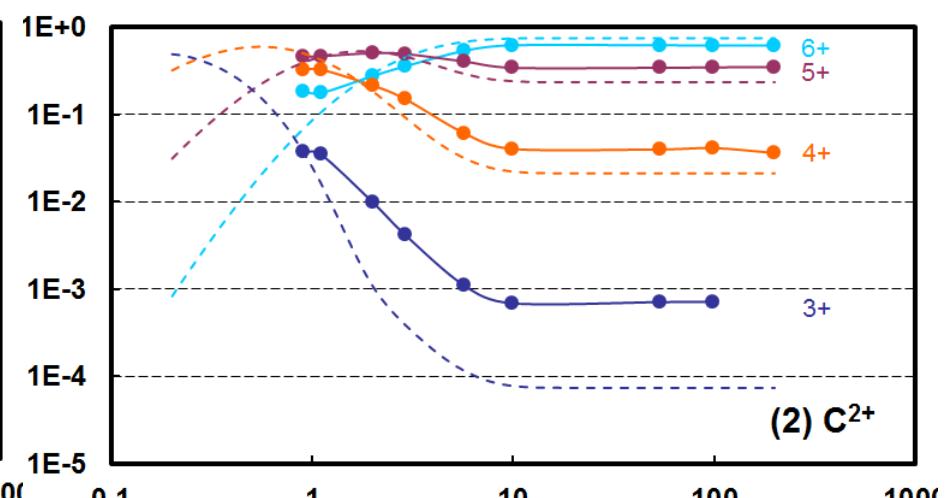
Case	Calculation	Yields $Y_i$	Density Effect
(1)		Charge-State $7(C^0 - C^{6+})$	Not involved.
(2)	Present		High $n$ states are ionized. JPB38,2675(2005)
(3)		CS + $n=1,2$ -state $18(C^0 - C^{6+})$	High $n$ states are ionized.
(4)	ETACHA4 PRA92,042703(2015)	CS + $n$ -substate many( $C^0 - C^{6+}$ )	Shorter collision intervals are involved in the RE.



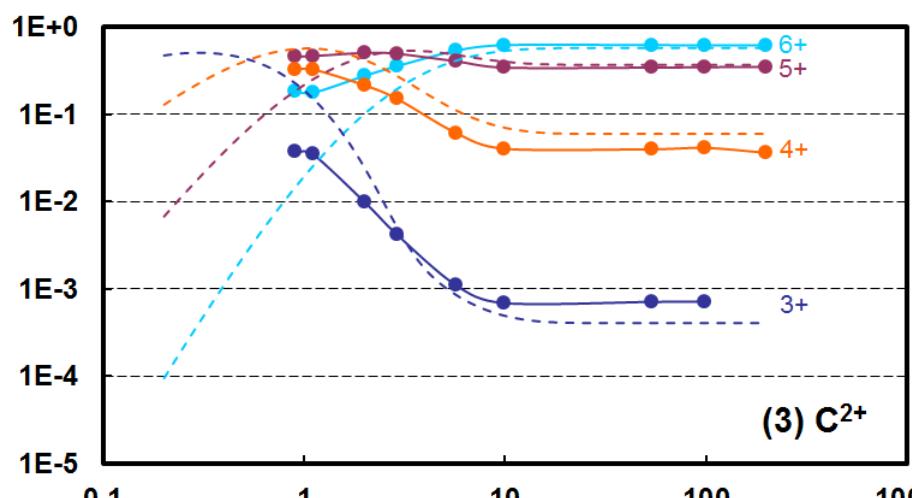
# Model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils



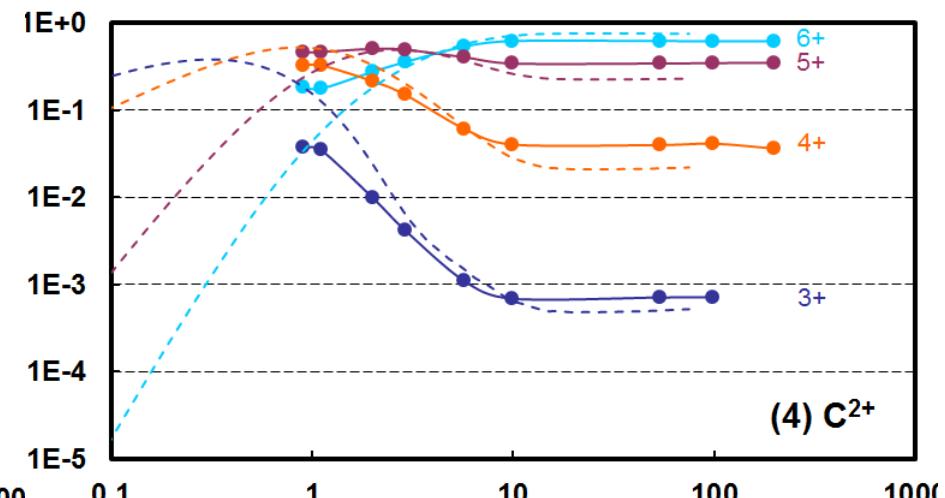
(1) C<sup>2+</sup>



(2) C<sup>2+</sup>



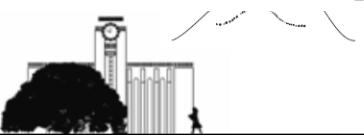
(3) C<sup>2+</sup>



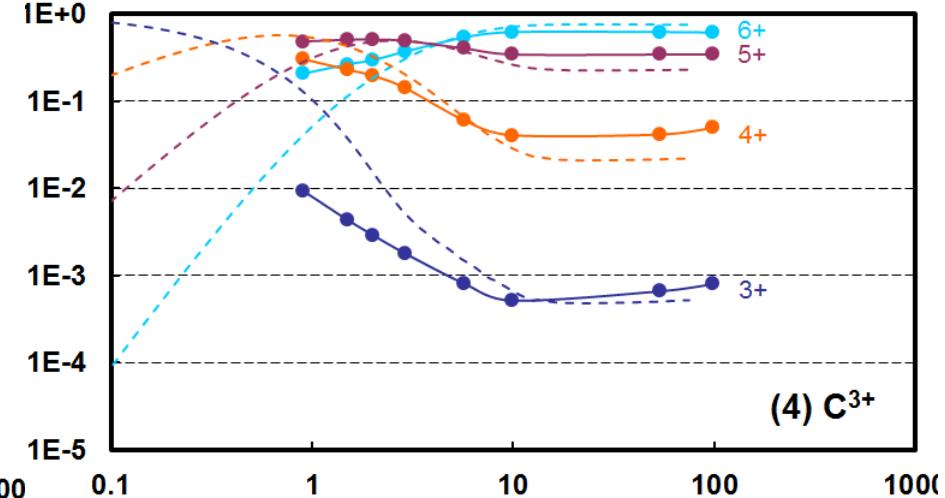
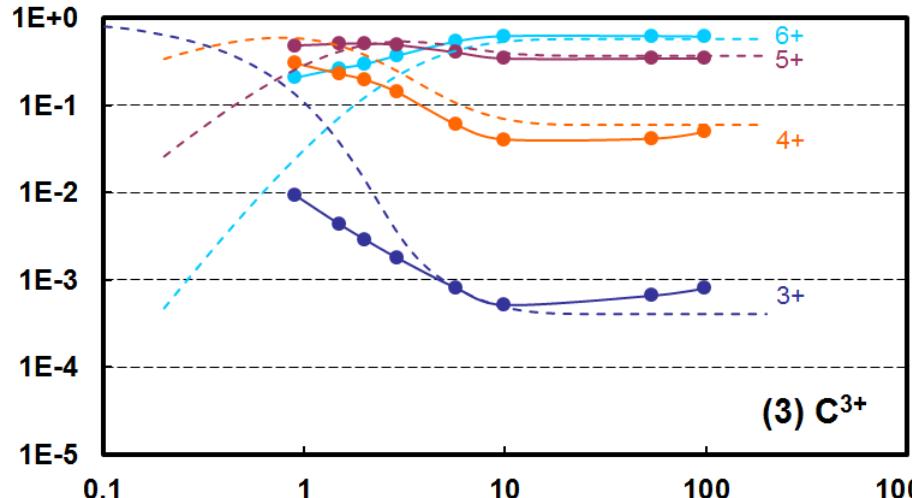
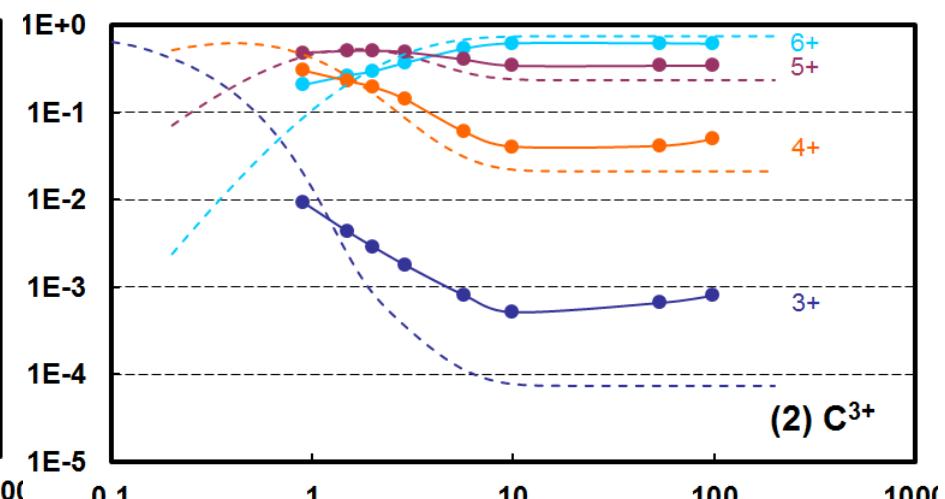
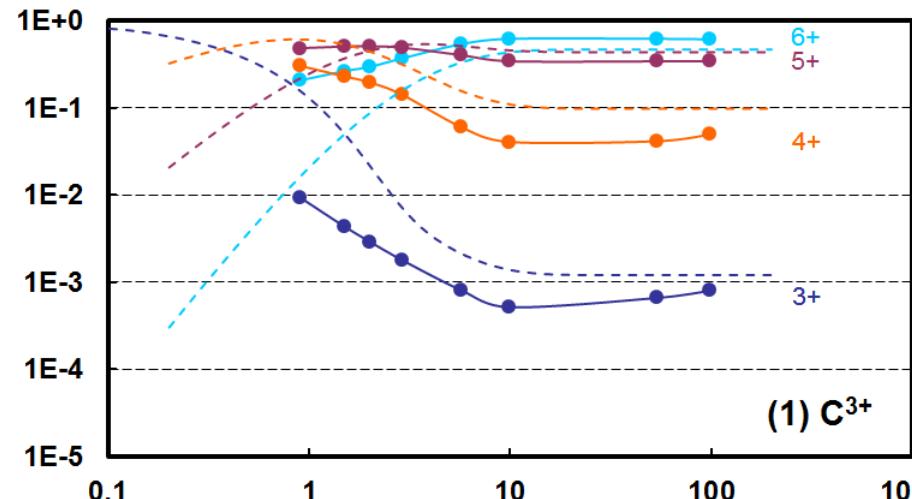
(4) C<sup>2+</sup>

Target Thickness ( $\mu\text{g}/\text{cm}^2$ )

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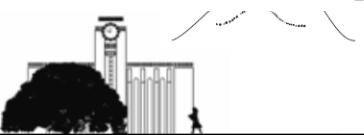


# Model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

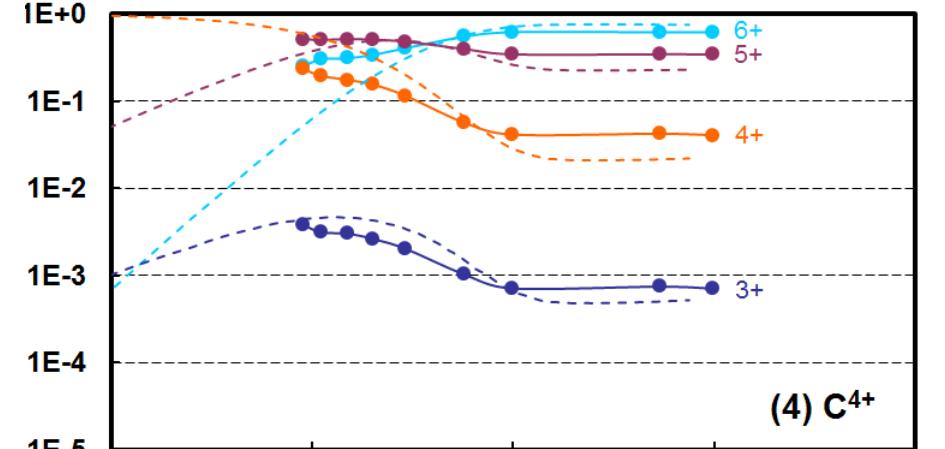
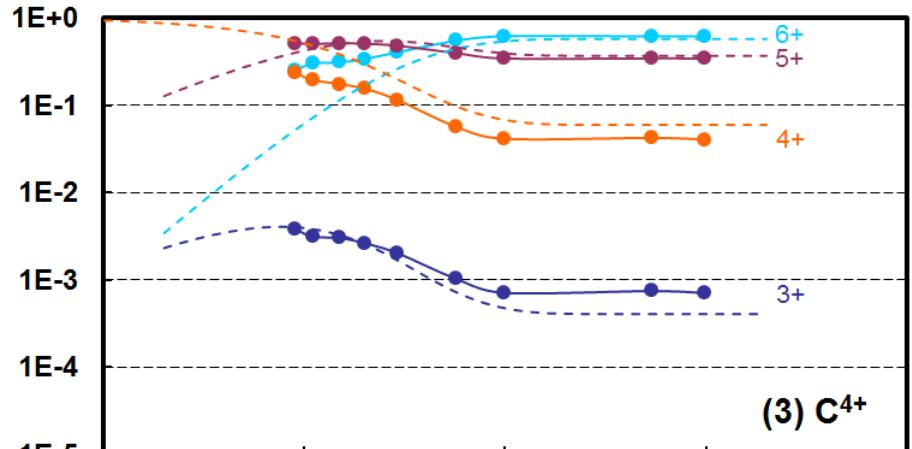
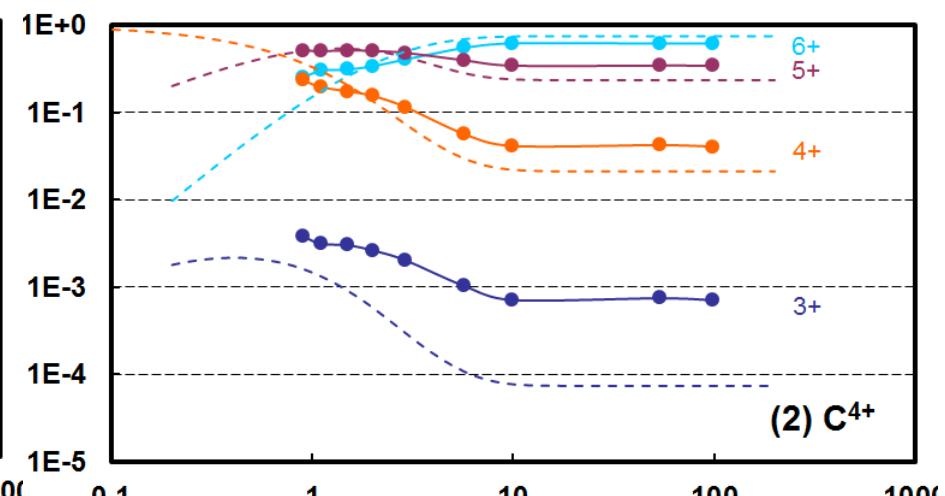
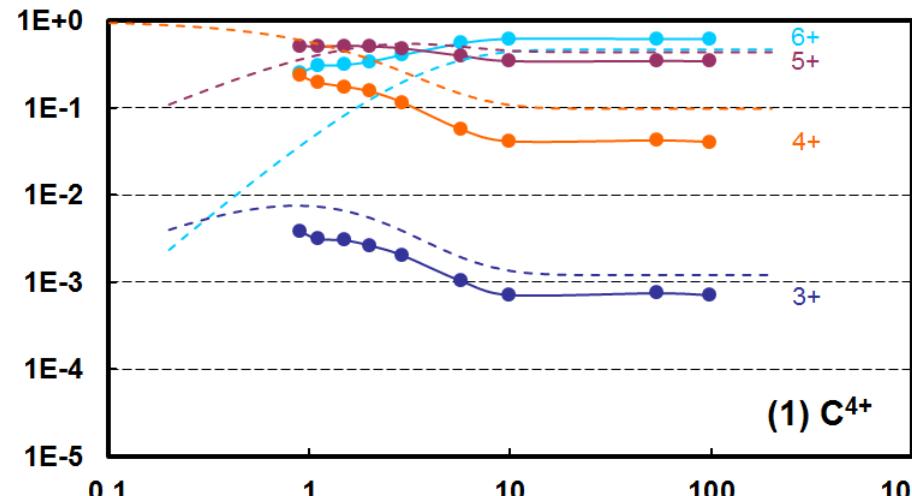


Target Thickness ( $\mu\text{g}/\text{cm}^2$ )

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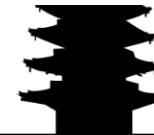
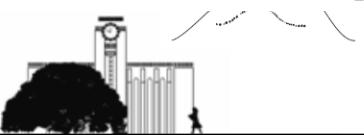


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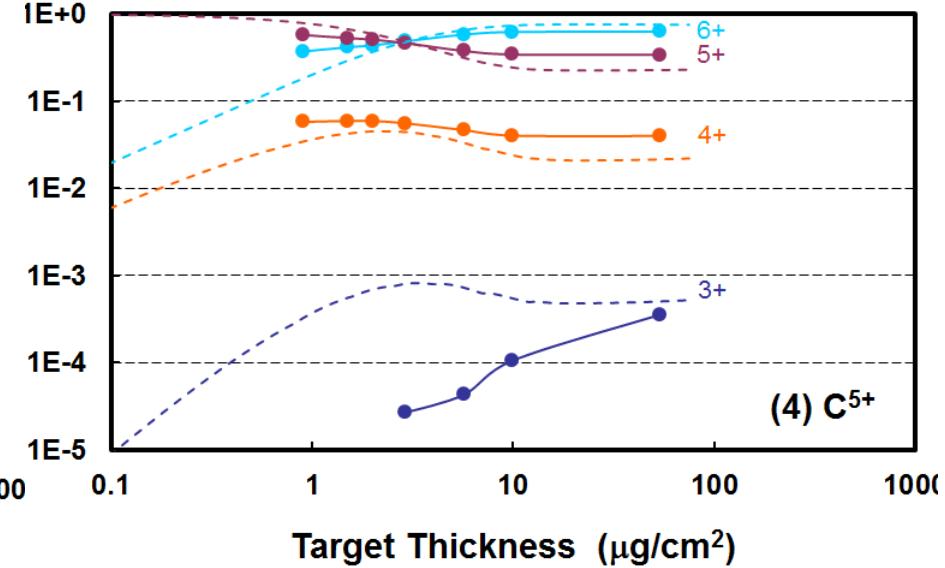
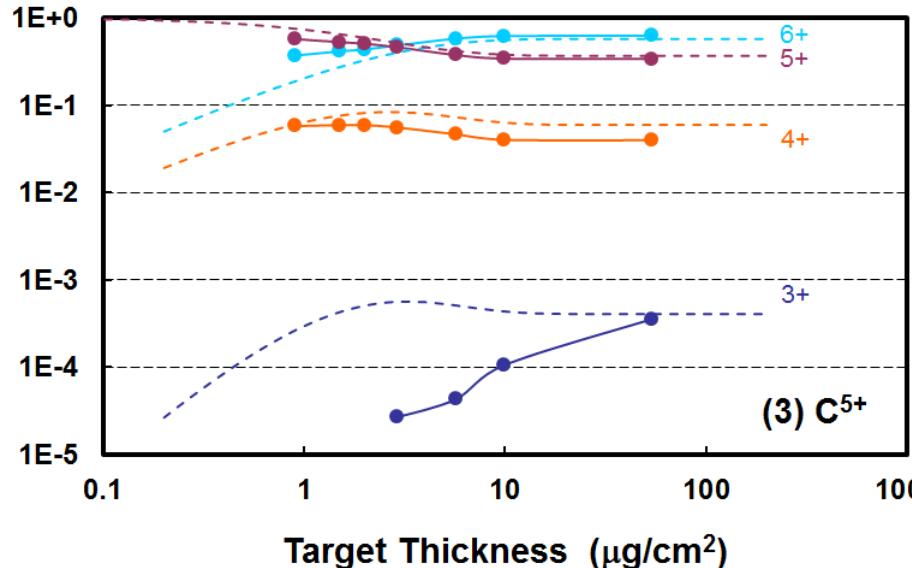
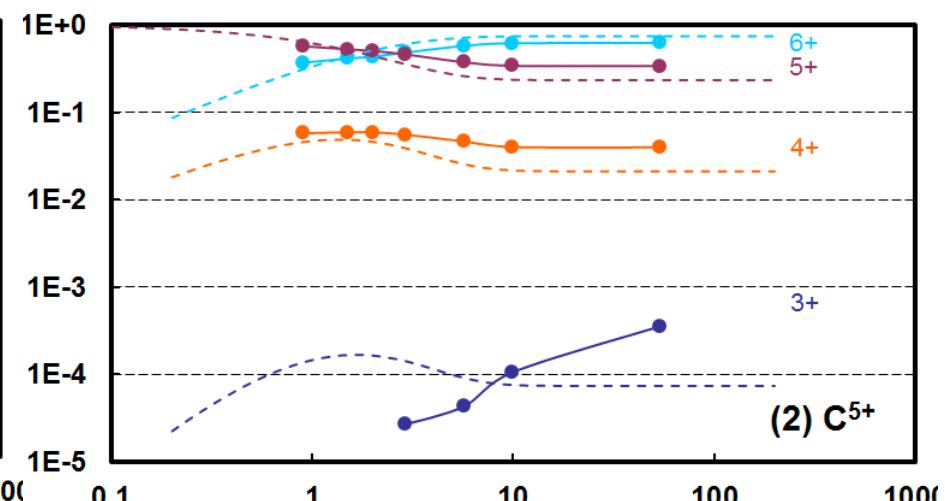
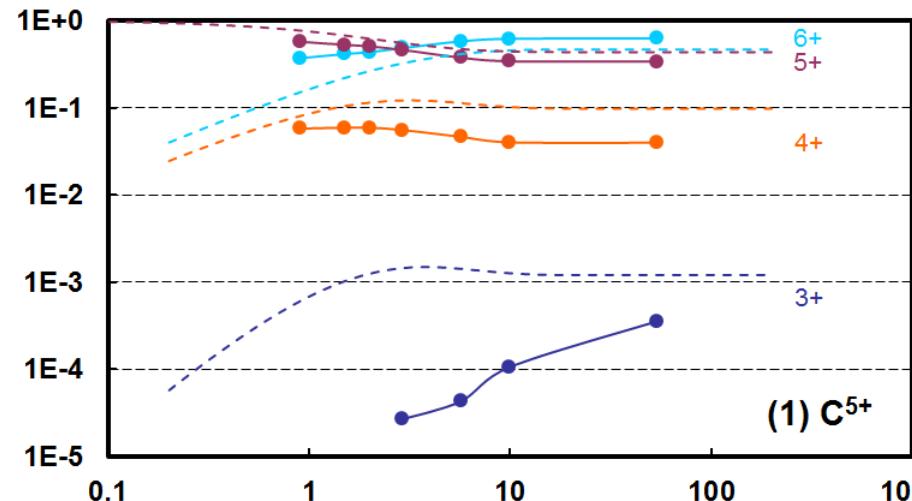


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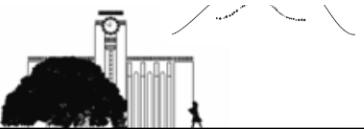


# Model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

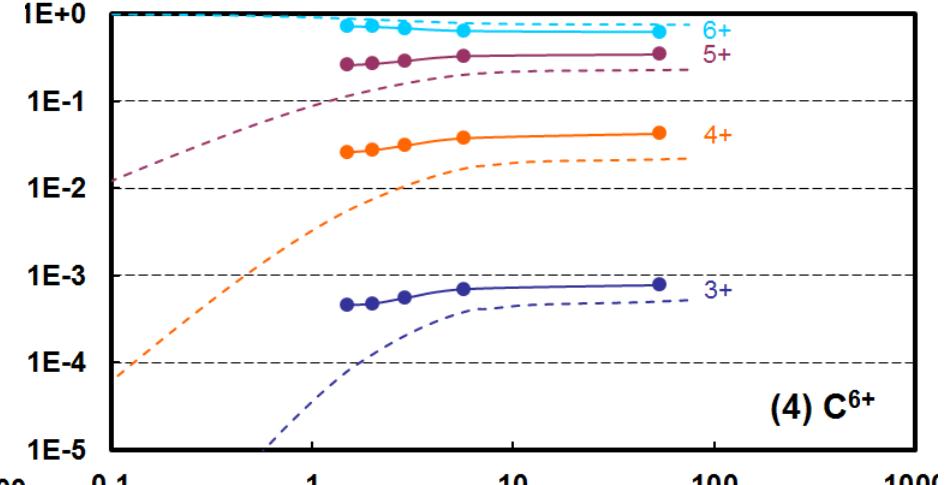
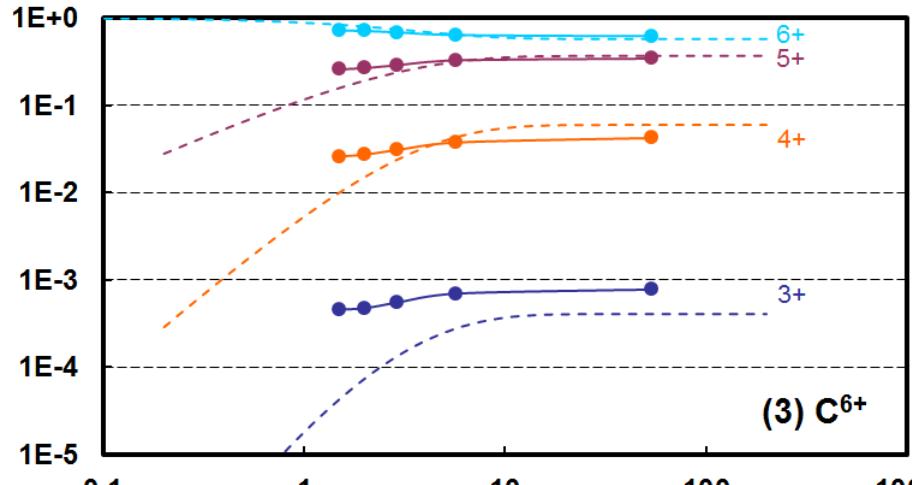
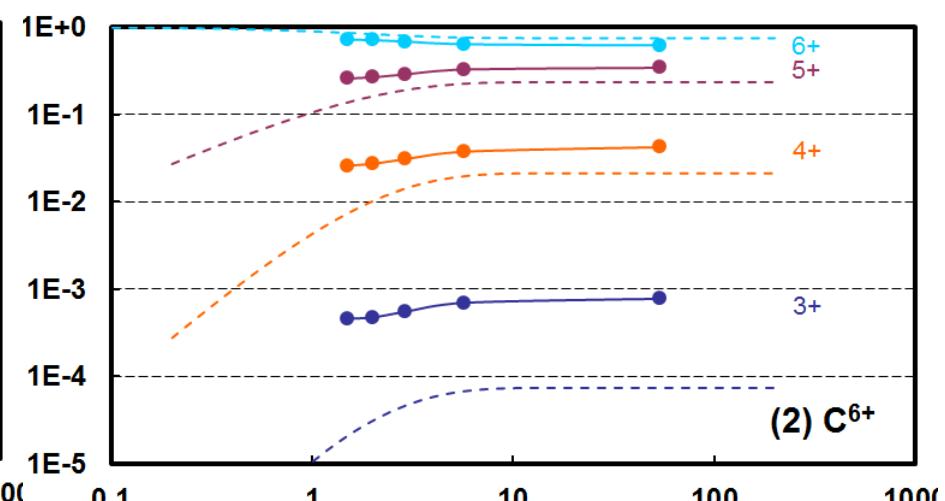
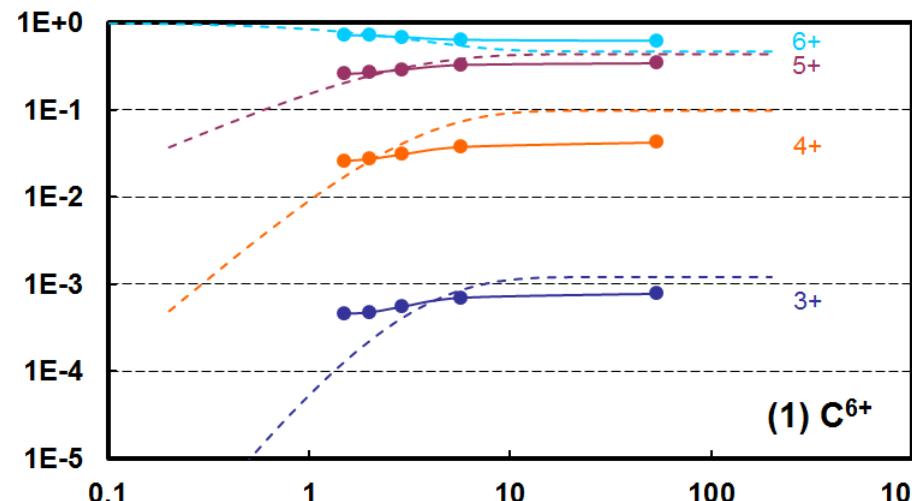


Target Thickness (μg/cm<sup>2</sup>)

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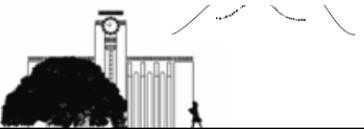


# Model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

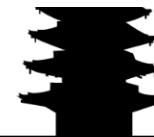
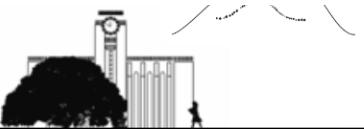
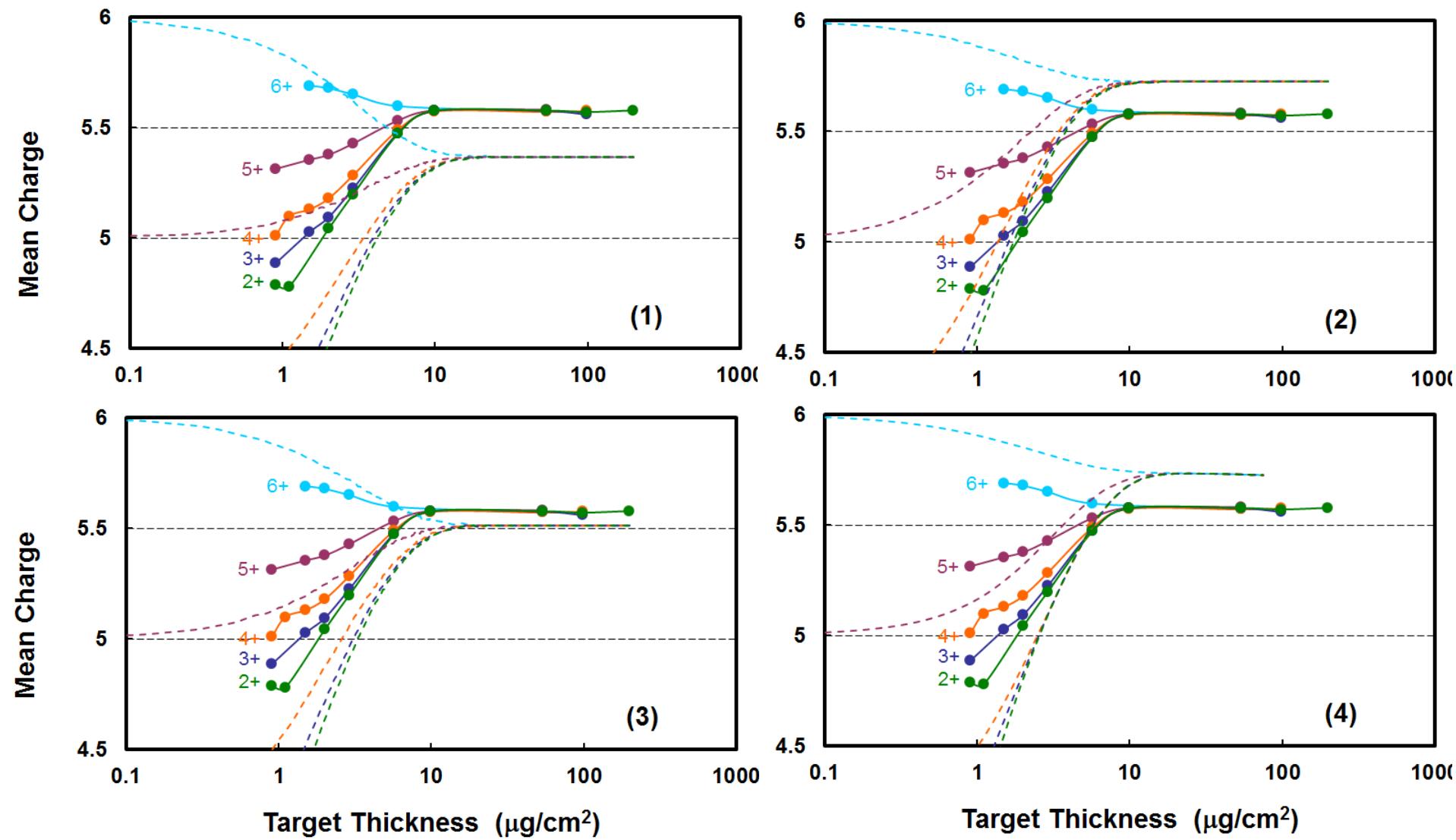


Target Thickness ( $\mu\text{g}/\text{cm}^2$ )

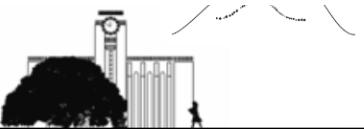
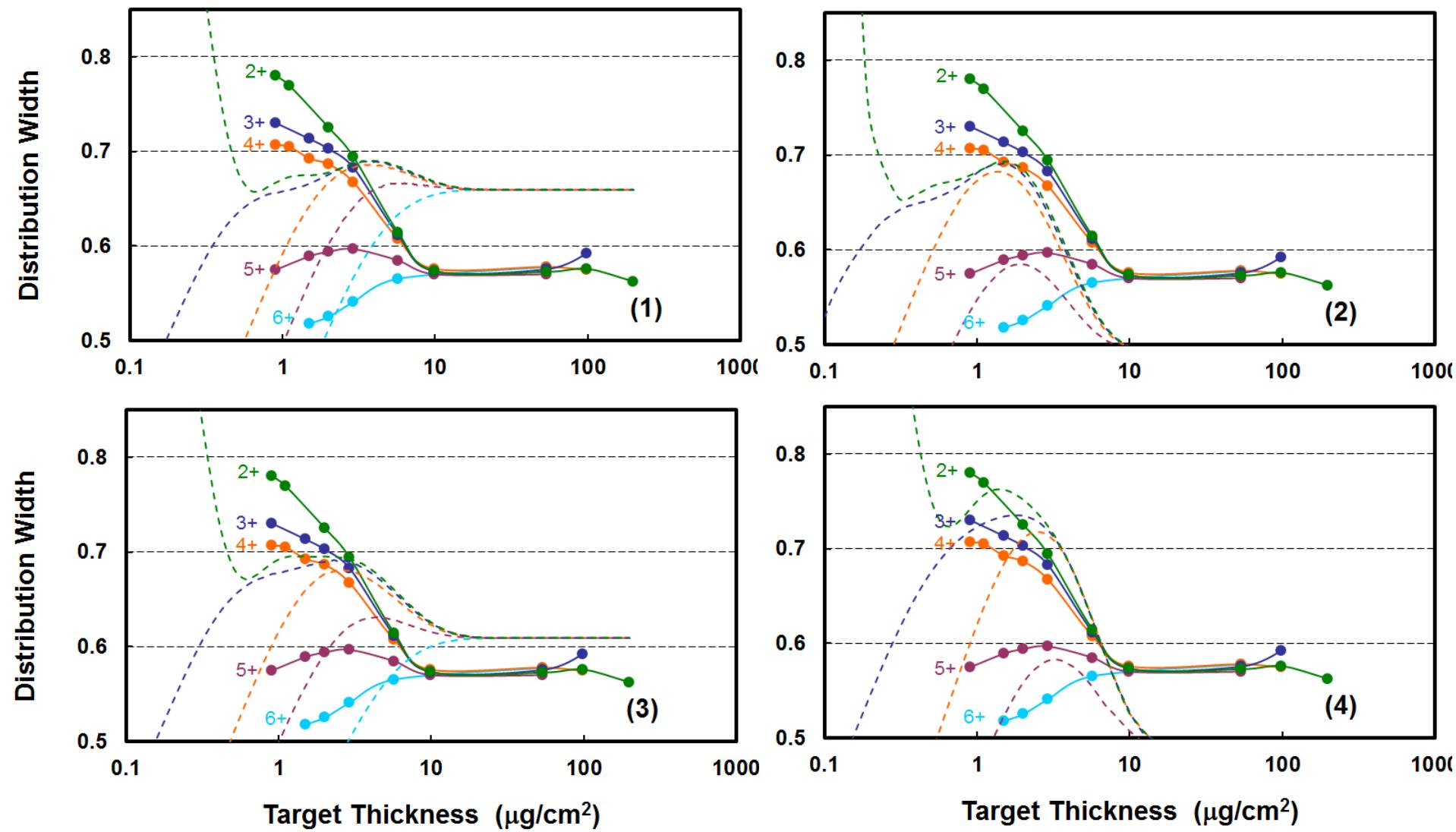
Target Thickness ( $\mu\text{g}/\text{cm}^2$ )



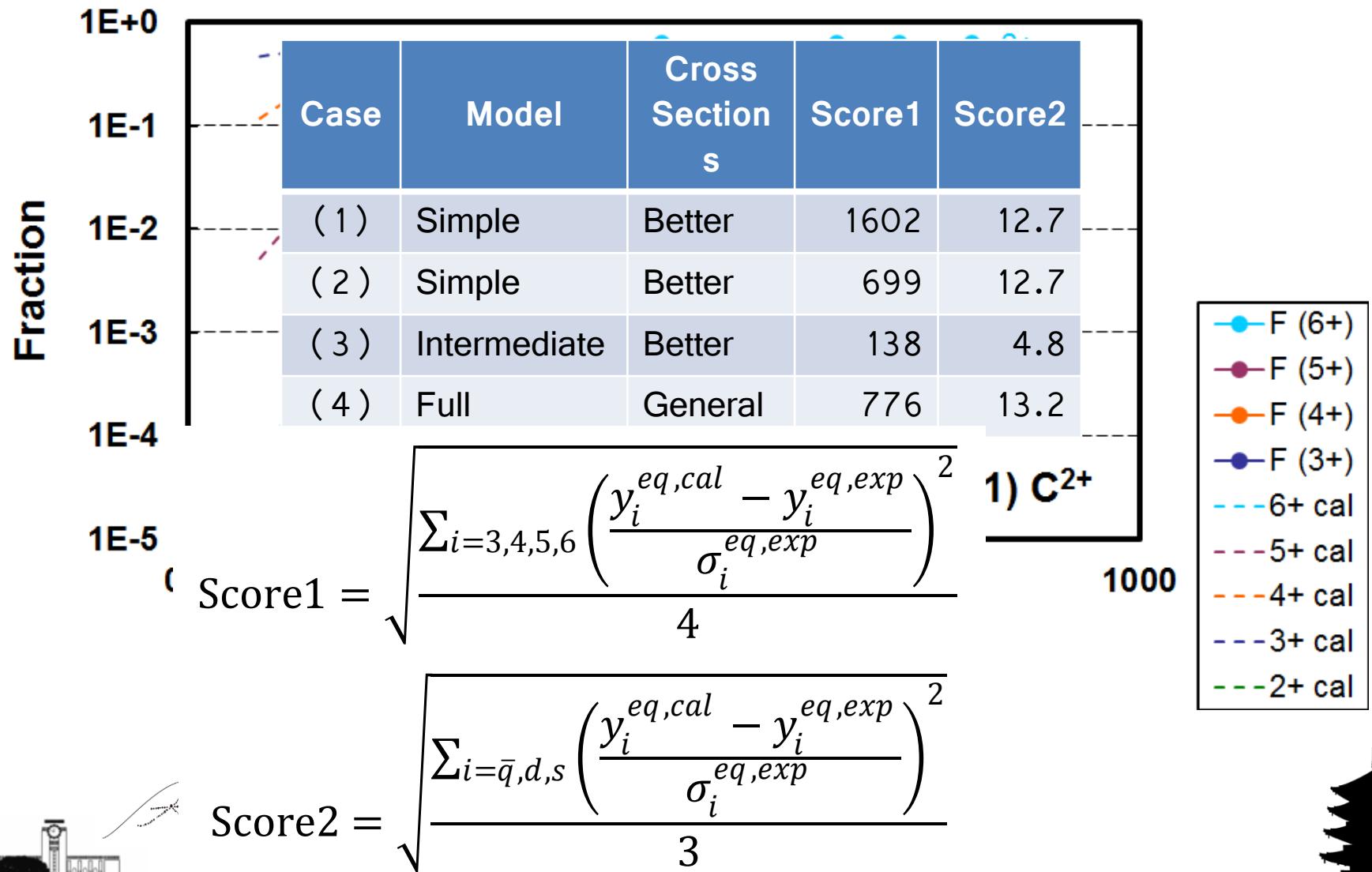
# Model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils



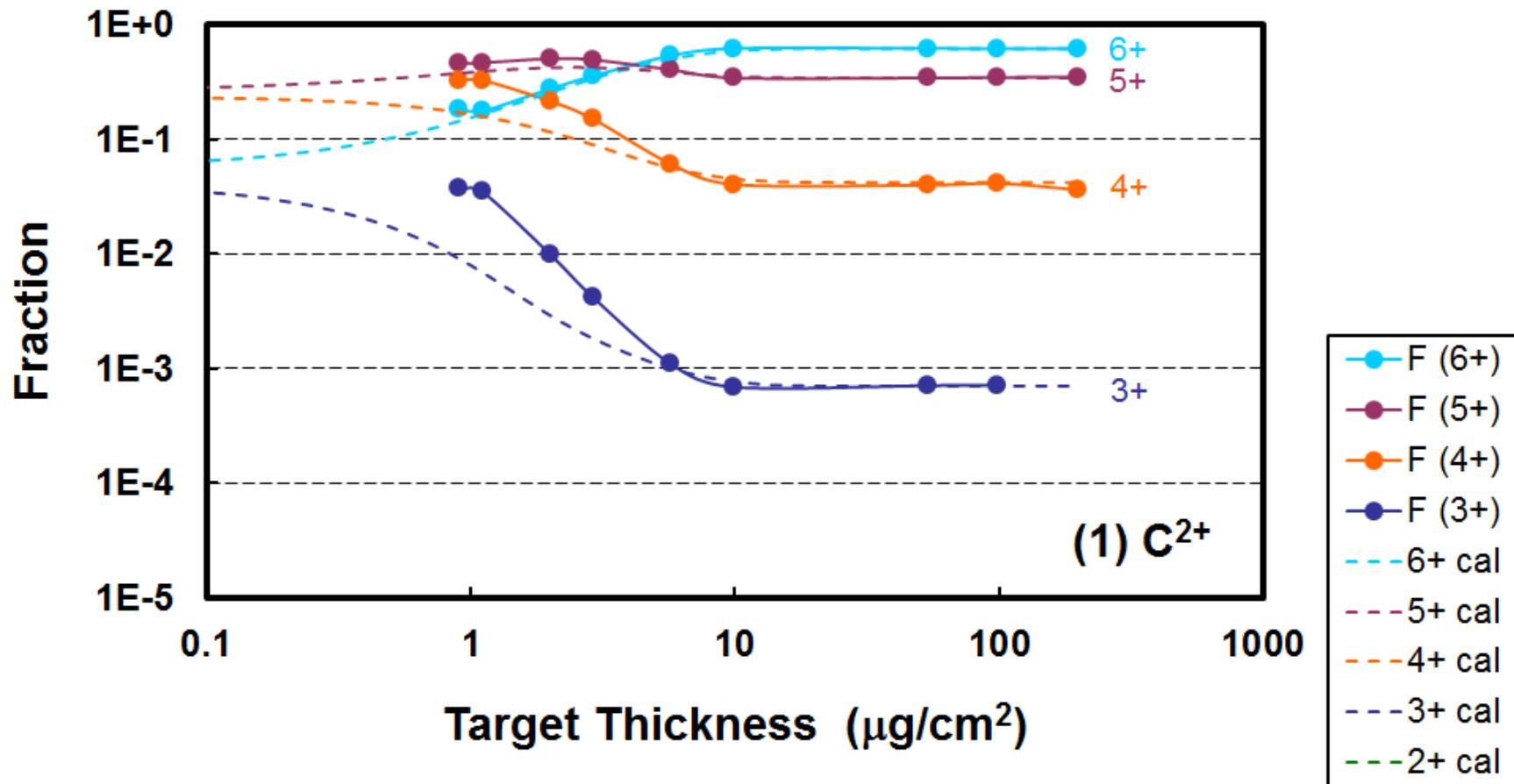
# Model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils



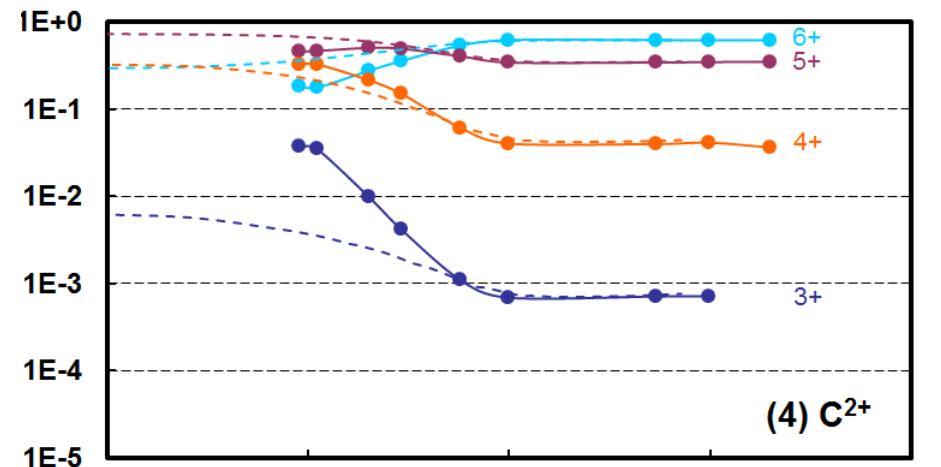
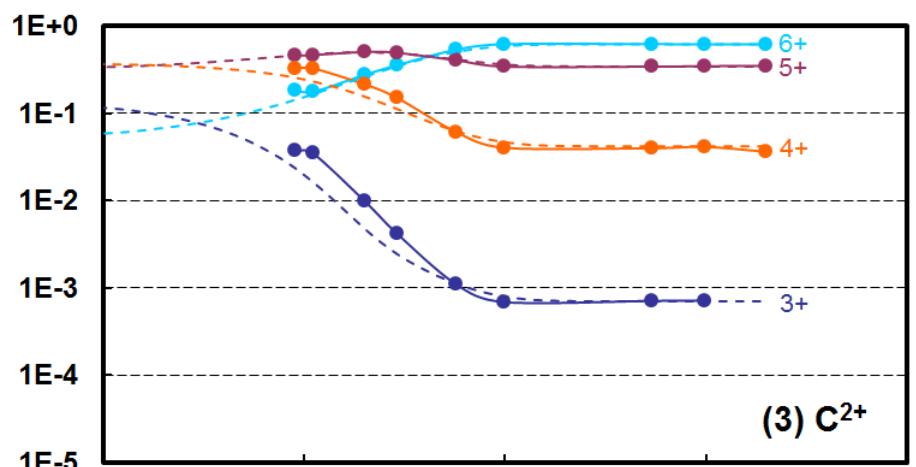
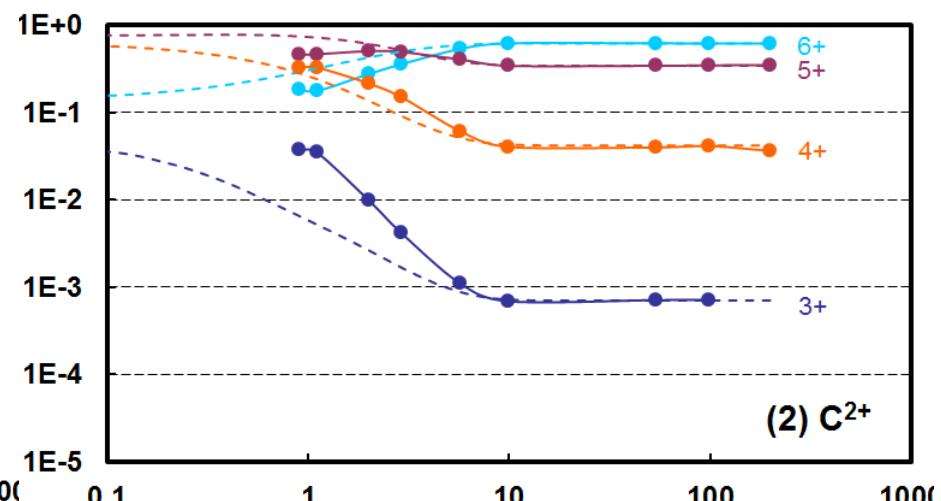
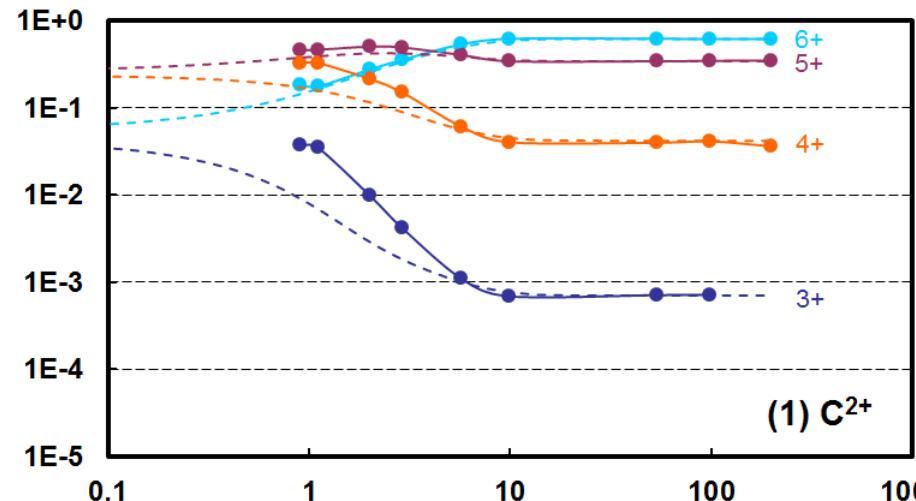
# Scores for reproducibility of the **equilibrium charge-state distributions** of 2.0 MeV/u C ions after C-foils



# Shifted model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

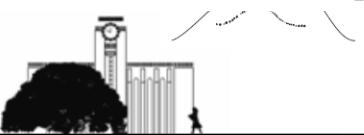


# Shifted model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

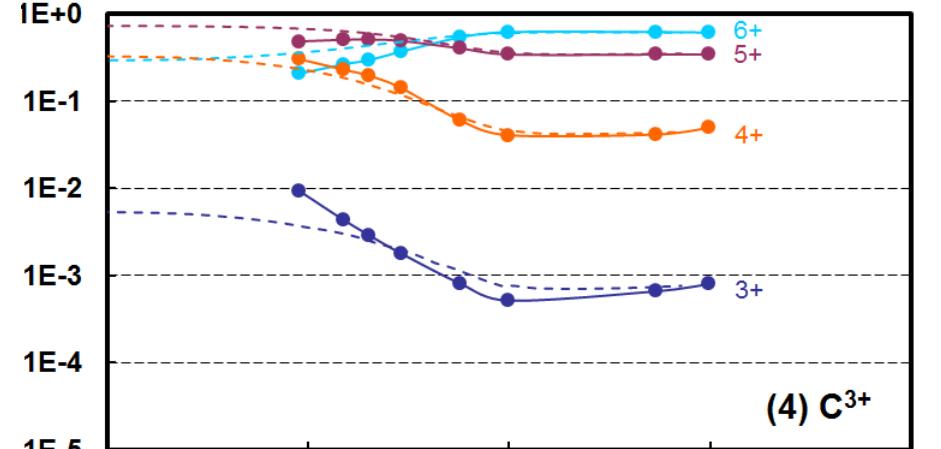
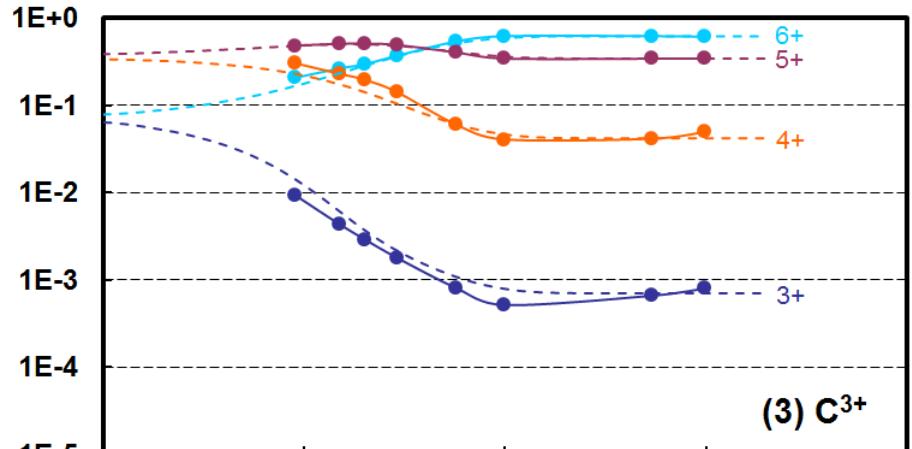
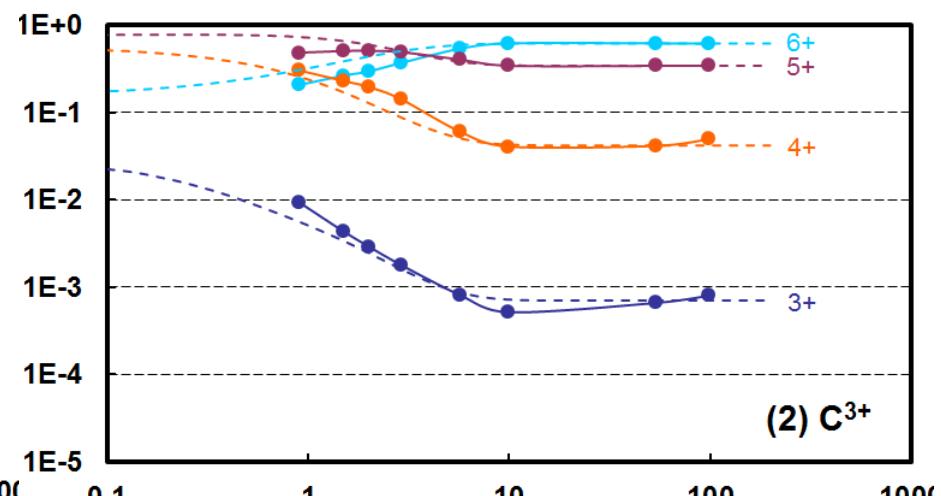
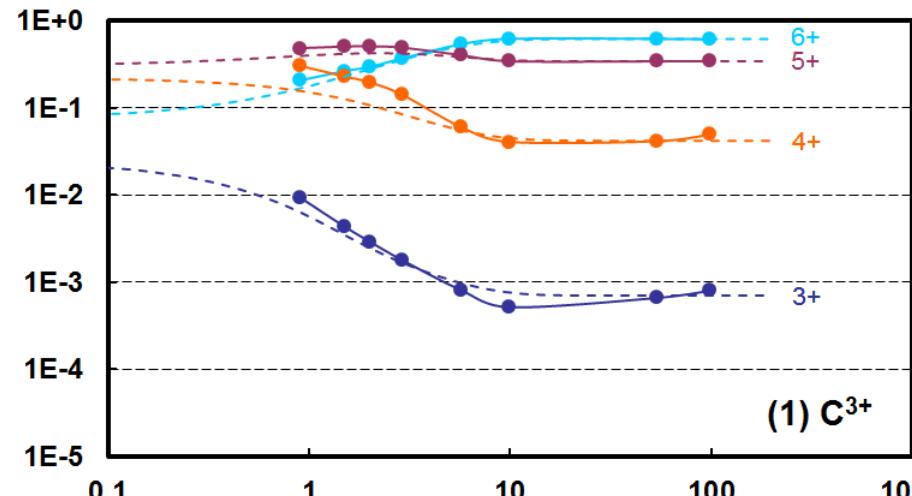


Target Thickness ( $\mu\text{g}/\text{cm}^2$ )

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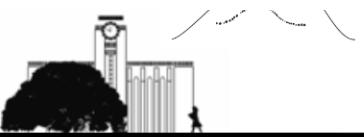


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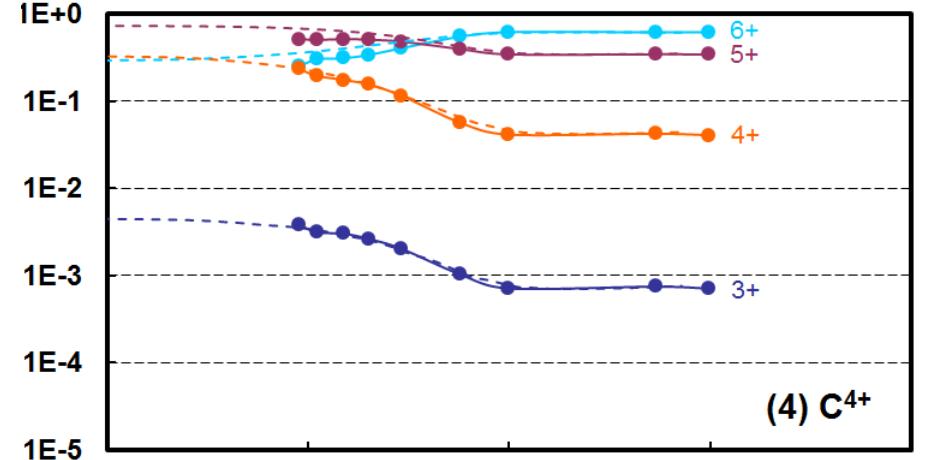
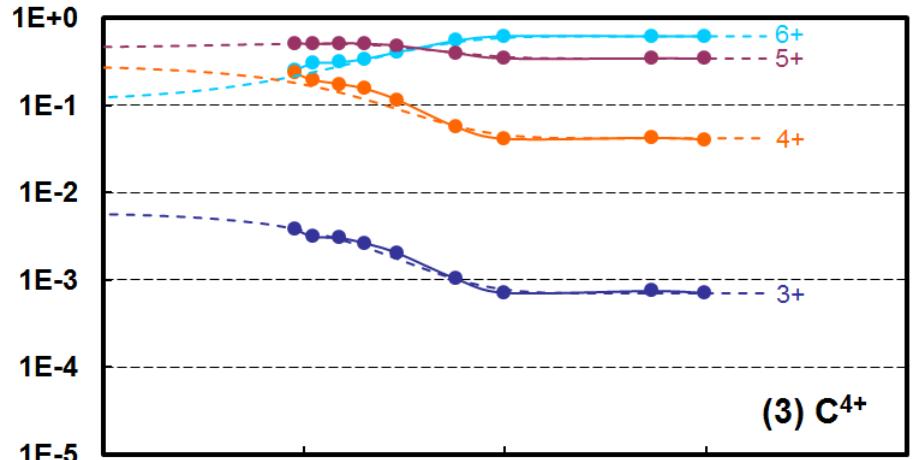
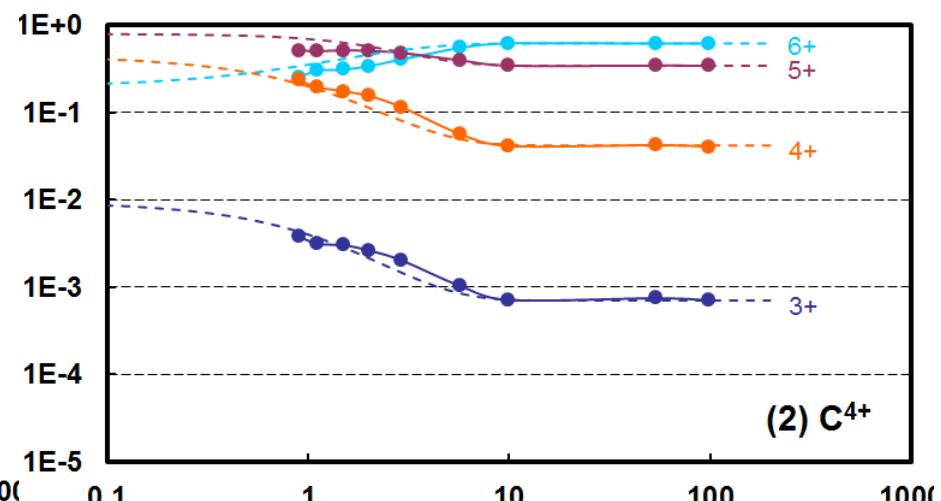
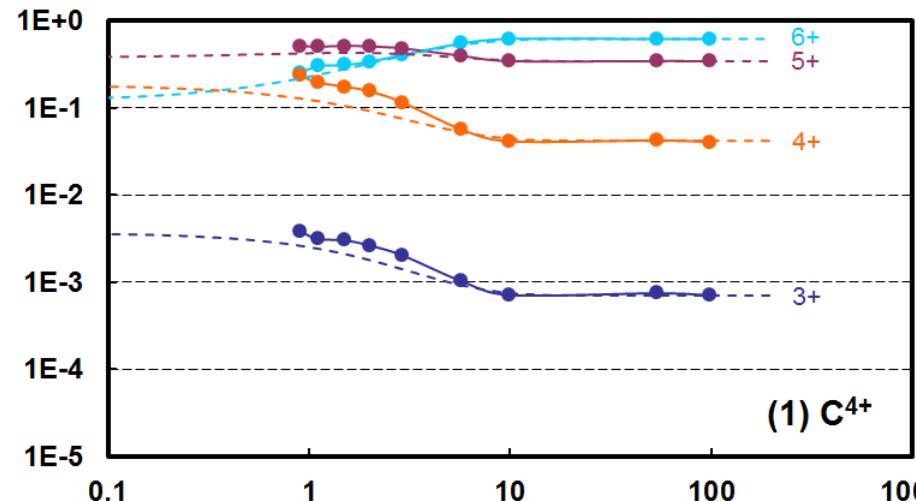


Target Thickness ( $\mu\text{g}/\text{cm}^2$ )

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# Shifted model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

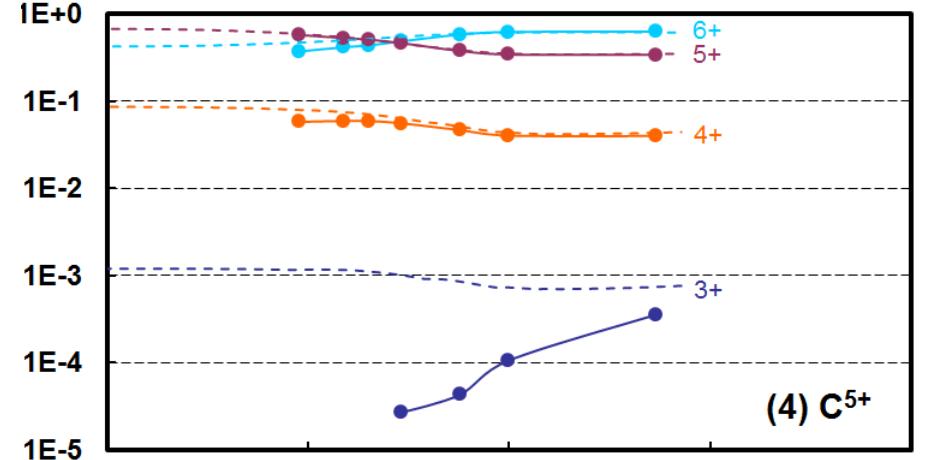
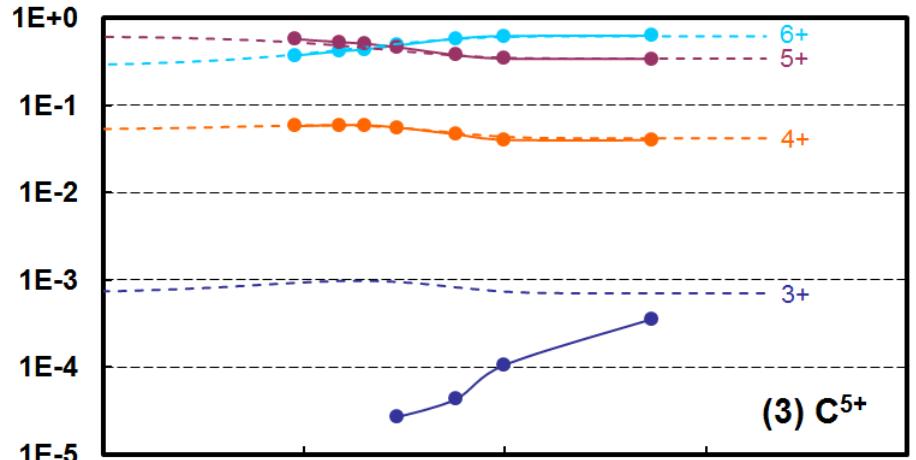
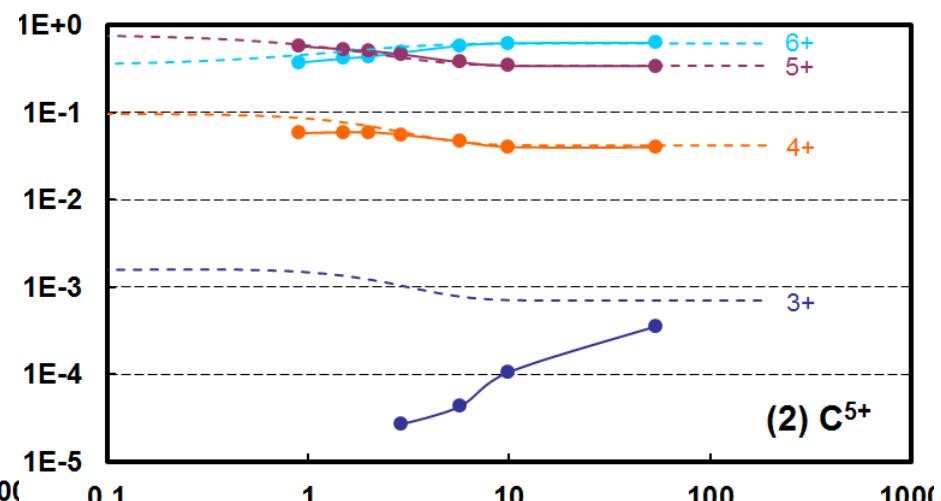
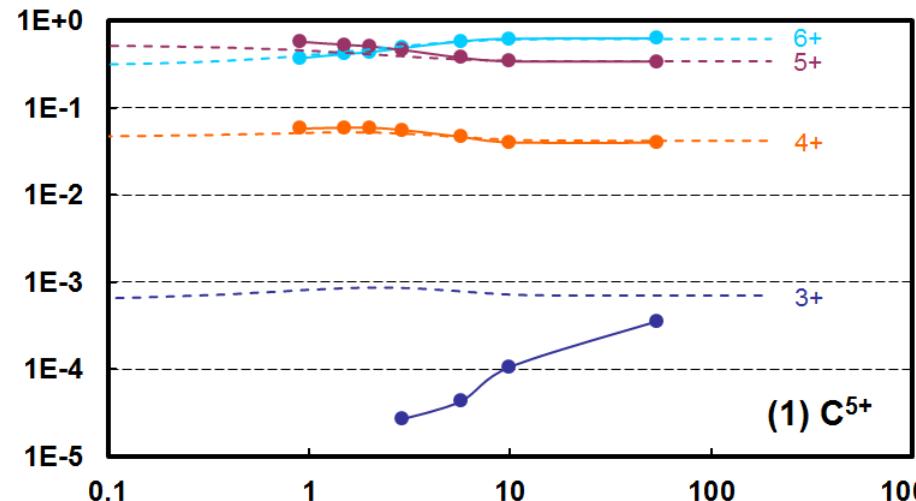


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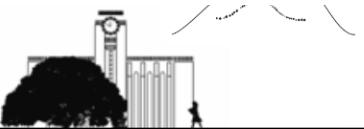


# Shifted model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

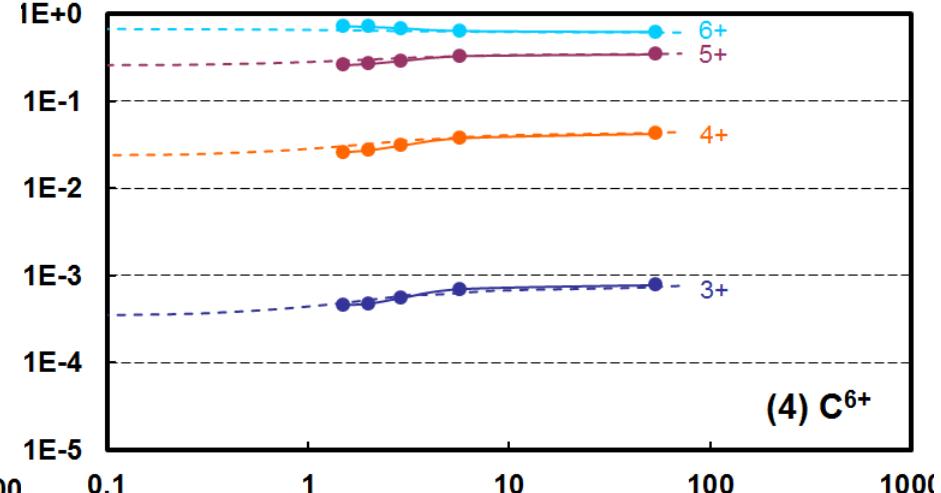
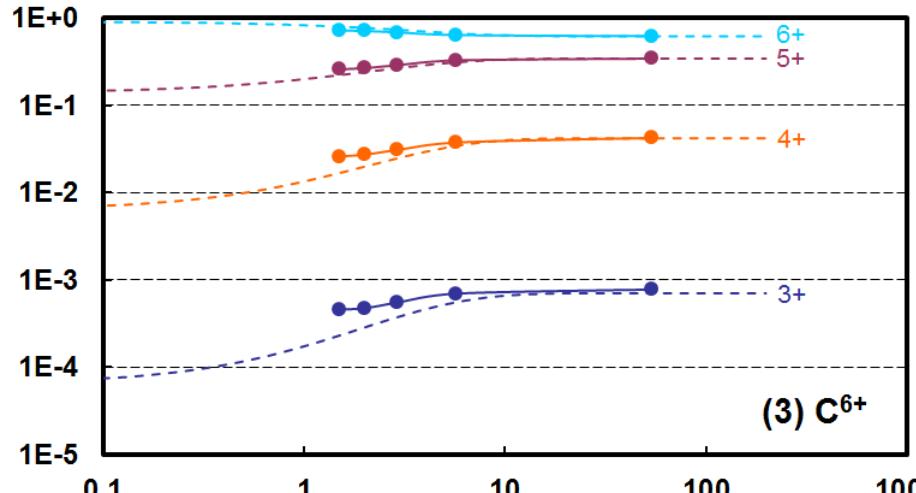
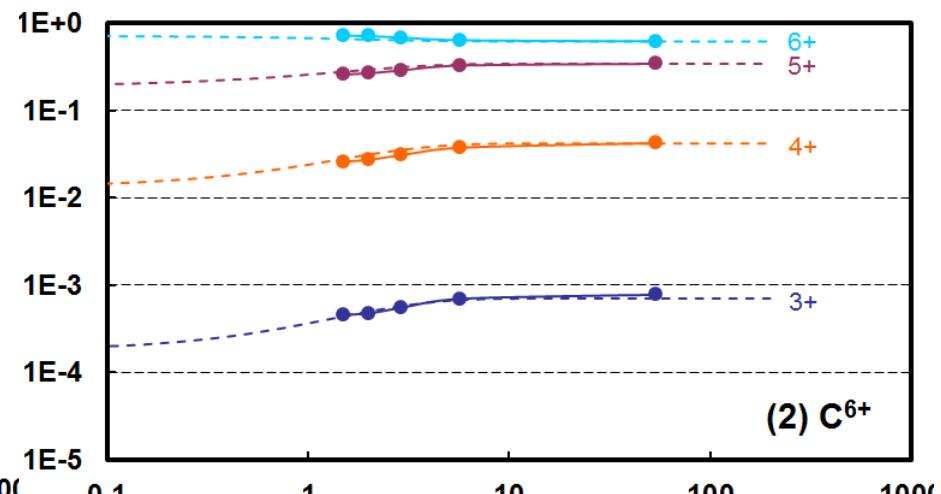
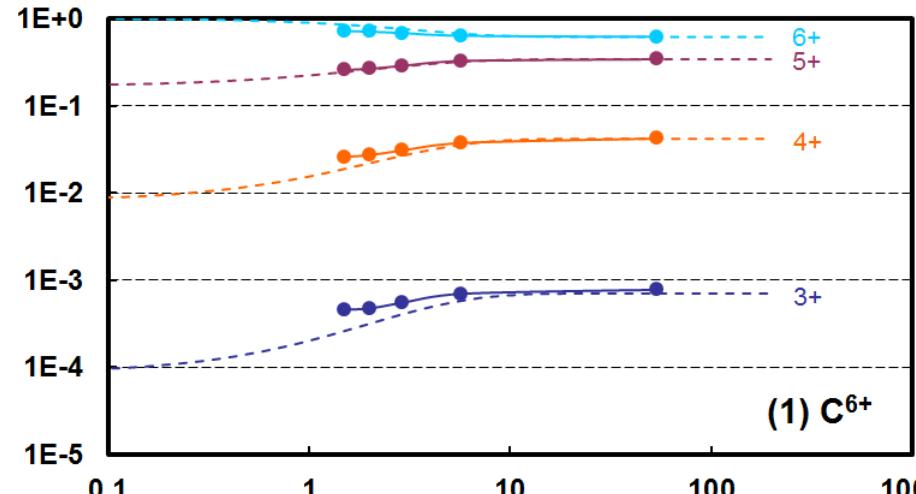


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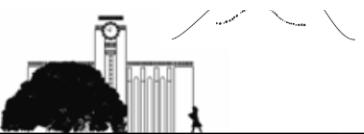


# Shifted model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils



Target Thickness ( $\mu\text{g}/\text{cm}^2$ )

Target Thickness ( $\mu\text{g}/\text{cm}^2$ )

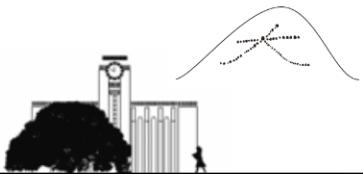


# Scores for reproducibility of the **pre-equilibrium charge-state distributions** of 2.0 MeV/u C ions after C-foils

$$Score = \sqrt{\frac{\sum_i (y_i^{pre-eq,cal} - y_i^{pre-eq,exp})^2}{N}}$$

$N = 97$

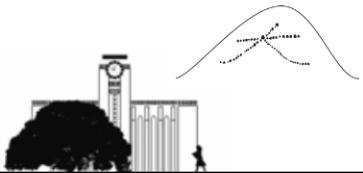
Case	Model	Cross Sections	Score	Score1	Score2
(1)	Simple	Better	0.0570	1602	12.7
(2)	Simple	Better	0.0792	699	12.7
(3)	Intermediate	Better	0.0282	138	4.8
(4)	Full	General	0.0747	776	13.2



# Summary and outlook

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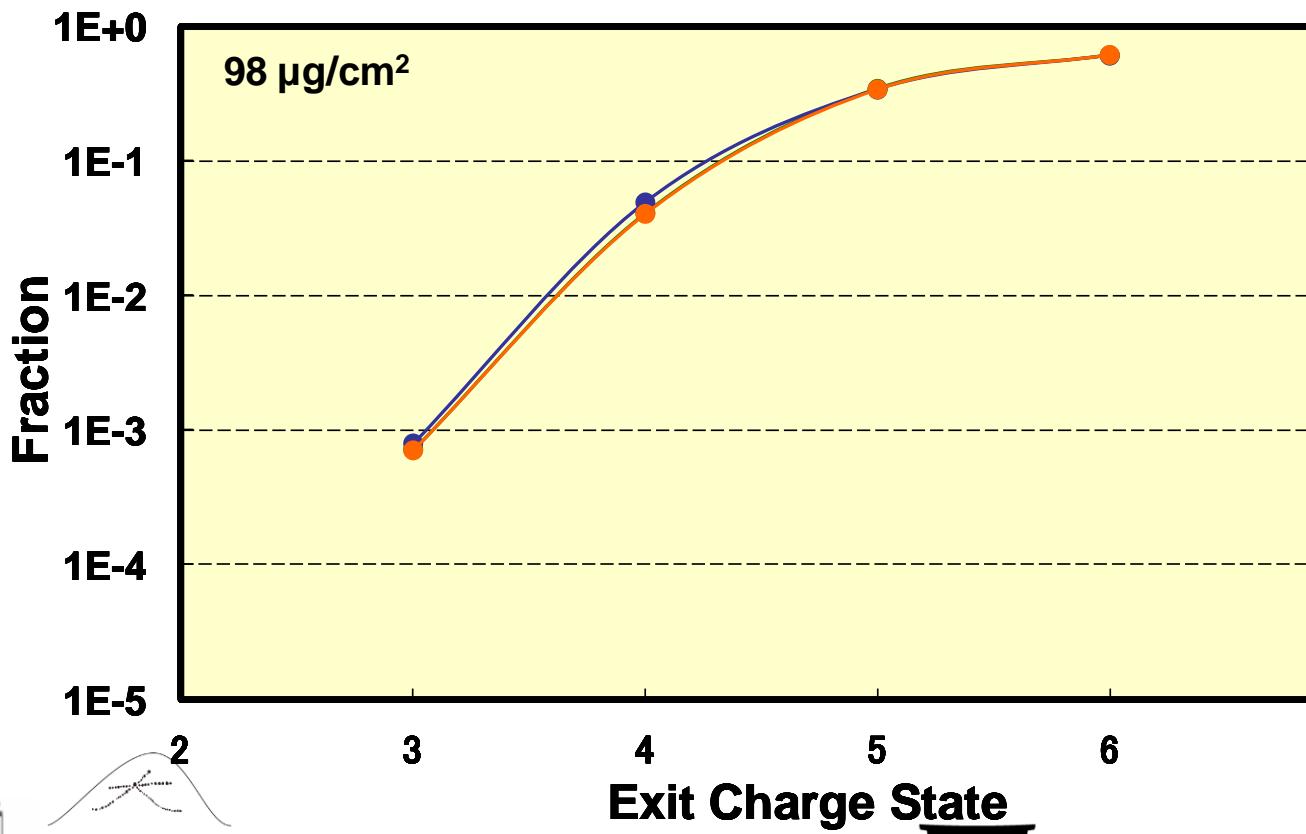
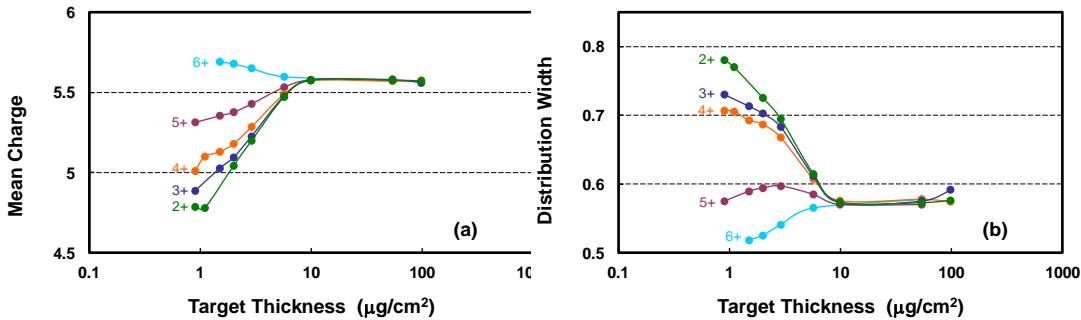
- You require not just accuracy of calculated cross sections but also their completeness.
- Experimentalists would like the evaluation of theoretical data to be done with experiments, but in many cases, there exist few experiments directly comparable to theories.
- Experimentalists are able to provide very accurate experimental results in some cases.
- It would be possible to evaluate set of calculated cross sections (e-capture, loss, excitation, de-excitation) using charge state evolution data.
- It would be also possible to reduce the collision energy by using dense gas targets.



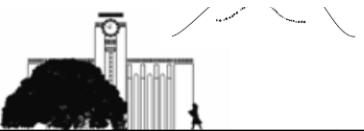
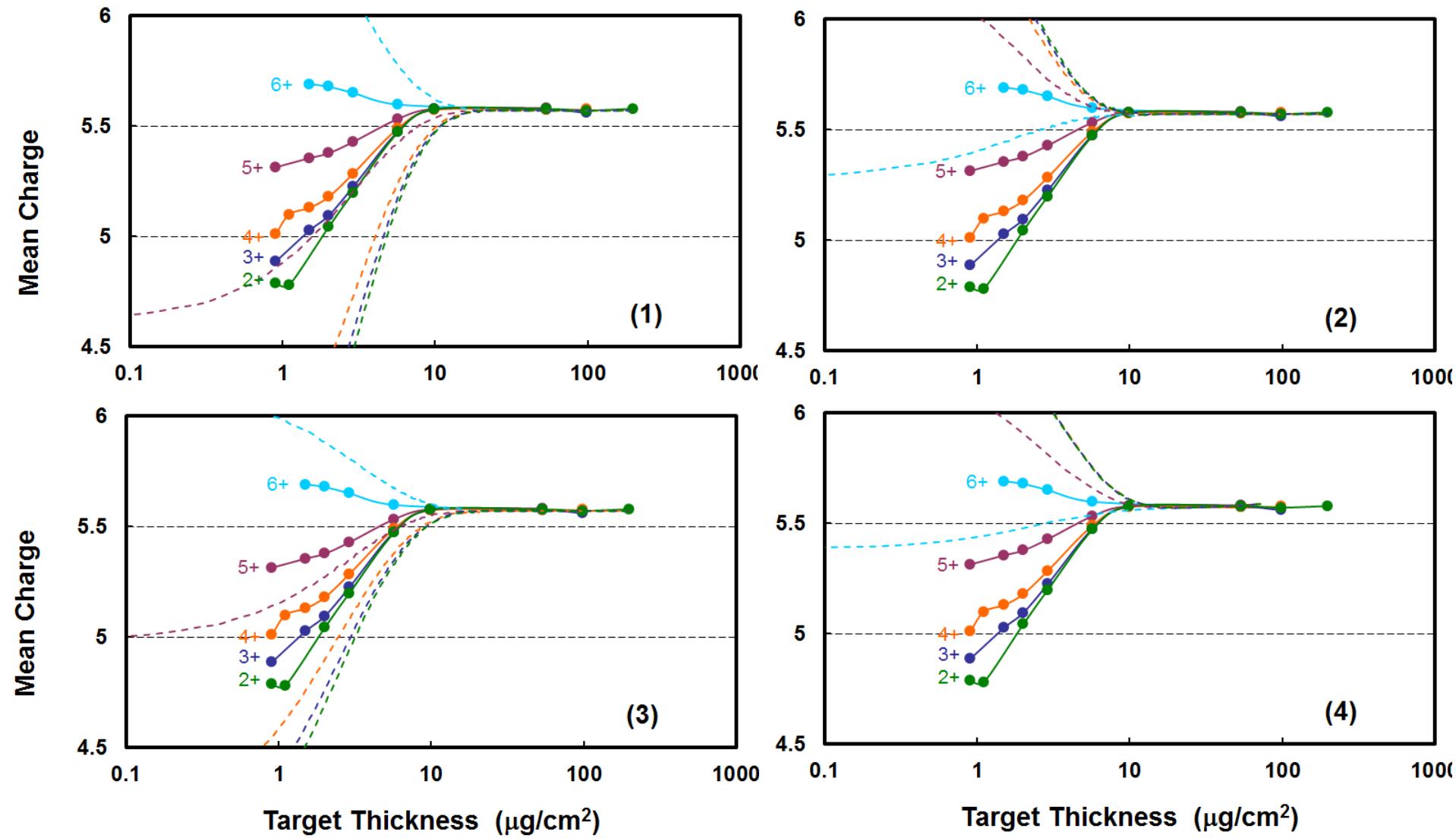
# Vielen Dank und Frohe Weihnachten !



# Charge-state distributions of 2.0 MeV/u $C^{q+}$ ions after C-foils



# Shifted model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils



# Shifted model calculations using sets of cross sections for charge-state distributions of 2.0 MeV/u C ions after C-foils

