

**“a procedure to explore uncertainty and reliability  
in theoretical cross section data for electron and  
positron scattering”**



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# Outline

- Need for cross section data
- Theoretical methodology & Sample Results
  - ❖ Electron Scattering
  - ❖ Positron Scattering
- Uncertainty estimation
  - ❖ Benchmarking Data
  - ❖ Consistency check
  - ❖ Convergence check
  - ❖ Sensitivity to input parameters
  - ❖ Further plan
- IAMDB

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# Theory: Electron scattering\*

## □ Low Energy Formalism based on R-matrix

- ❖ Computes differential, momentum transfer and total cross section in the energy range 0.1eV to 10-15 eV
- ❖ The dissociative electron attachment process is qualitatively investigated

## □ Spherical Complex Optical Potential (SCOP) Method

- ❖ Computes elastic ,inelastic and total cross sections for energies above IP up to 105 keV

## □ Complex Scattering Potential-ionization contribution (CSP-ic) Method

- ❖ Computes ionization cross section from inelastic cross section calculated through SCOP method



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# Theory: Positron scattering\*

## □ Modified SCOP & CSP-ic Methods

- ❖ Computes ionization cross section from inelastic cross section calculated through SCOP method.

## □ Difference between electron and positron interaction:

- ❖ Positrons are distinguishable from electrons, hence no exchange.
- ❖ The static interaction is repulsive, and
- ❖ The polarization interaction is attractive in nature.
- ❖ **Positronium Formation and Positron annihilation**



# Theory: Positron scattering\*

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\* Singh et al., *J. Phys. Chem. A* **120** (2016) 5685.

# Theory: Positron scattering\*

## □ Modified SCOP & CSP-ic Methods

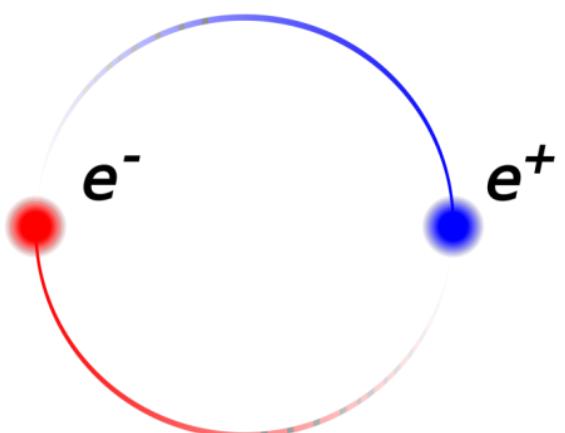
- ❖ Computes ionization cross section from inelastic cross section calculated through SCOP method.

## □ Difference between electron and positron interaction:

- ❖ No exchange.
- ❖ The static interaction is repulsive, and
- ❖ The polarization interaction is attractive in nature.

### ❖ Positronium Formation

- ❖ Positronium formation involves the capture of an incident positron by one of the target electrons, to form a "bound state".
- ❖ Positronium formation threshold is 6.8 eV below from ionization threshold of the target.



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# Results: Electron scattering

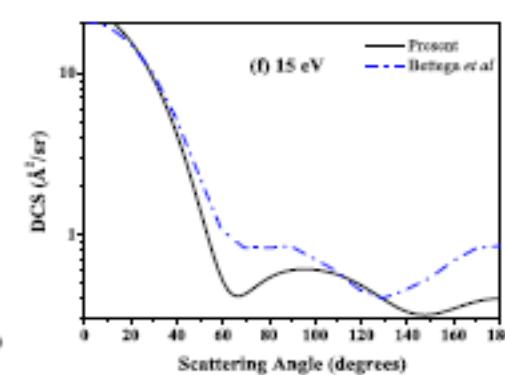
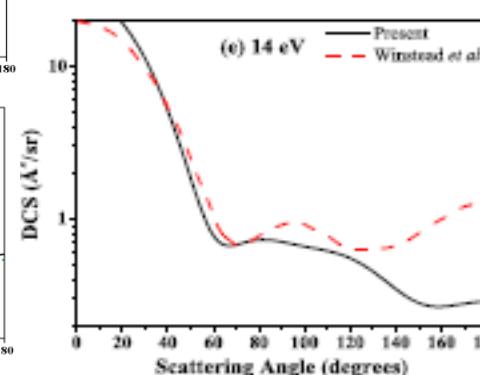
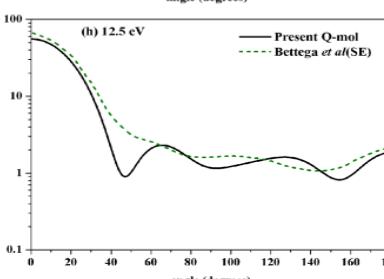
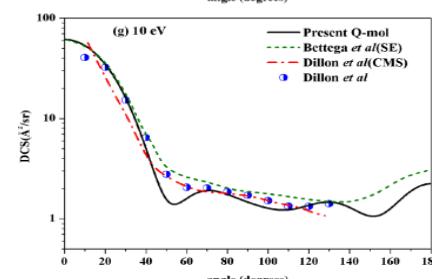
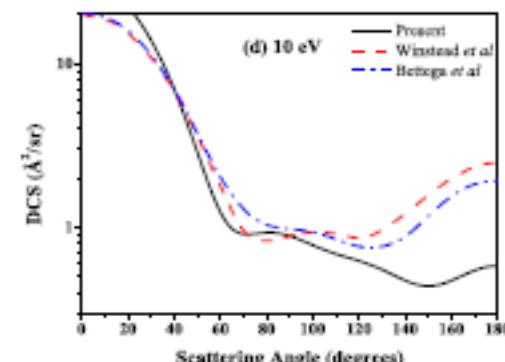
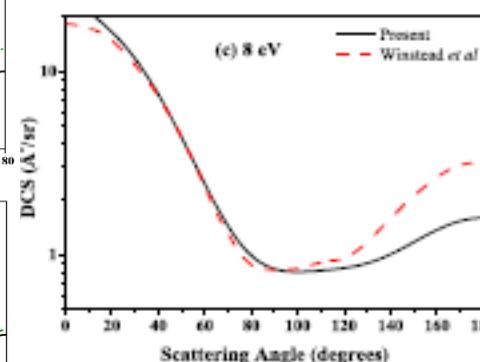
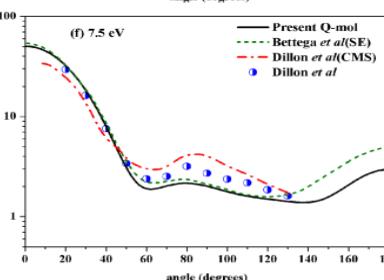
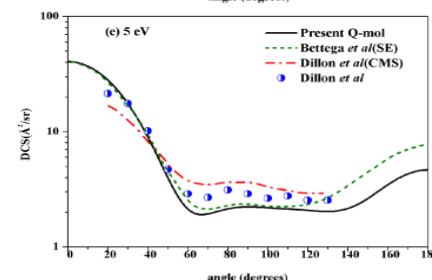
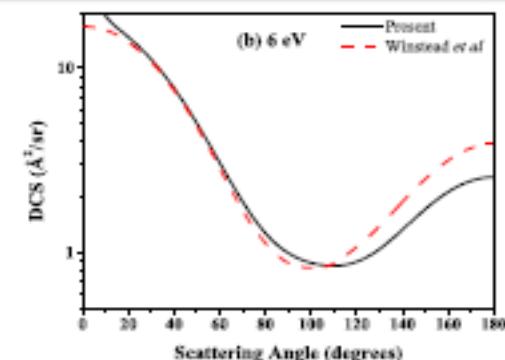
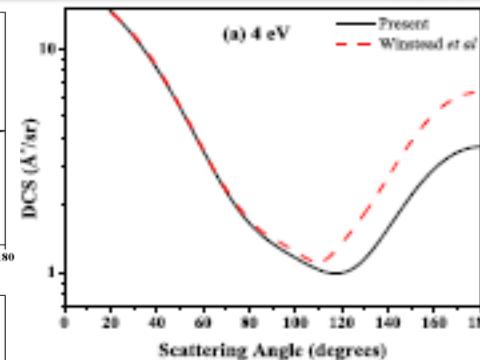
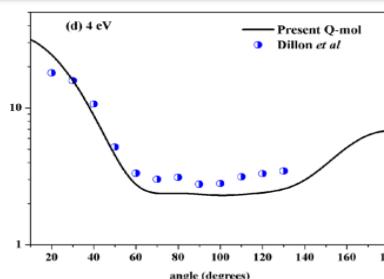
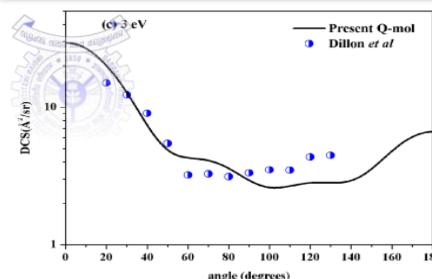
## परिणाम: इलेक्ट्रॉन स्कैटरिंग

### □ Electron Scattering Cross Sections

- ❖ Differential elastic
- ❖ Total elastic
- ❖ Momentum transfer
- ❖ Electronic excitation
- ❖ Total ionization
- ❖ Total

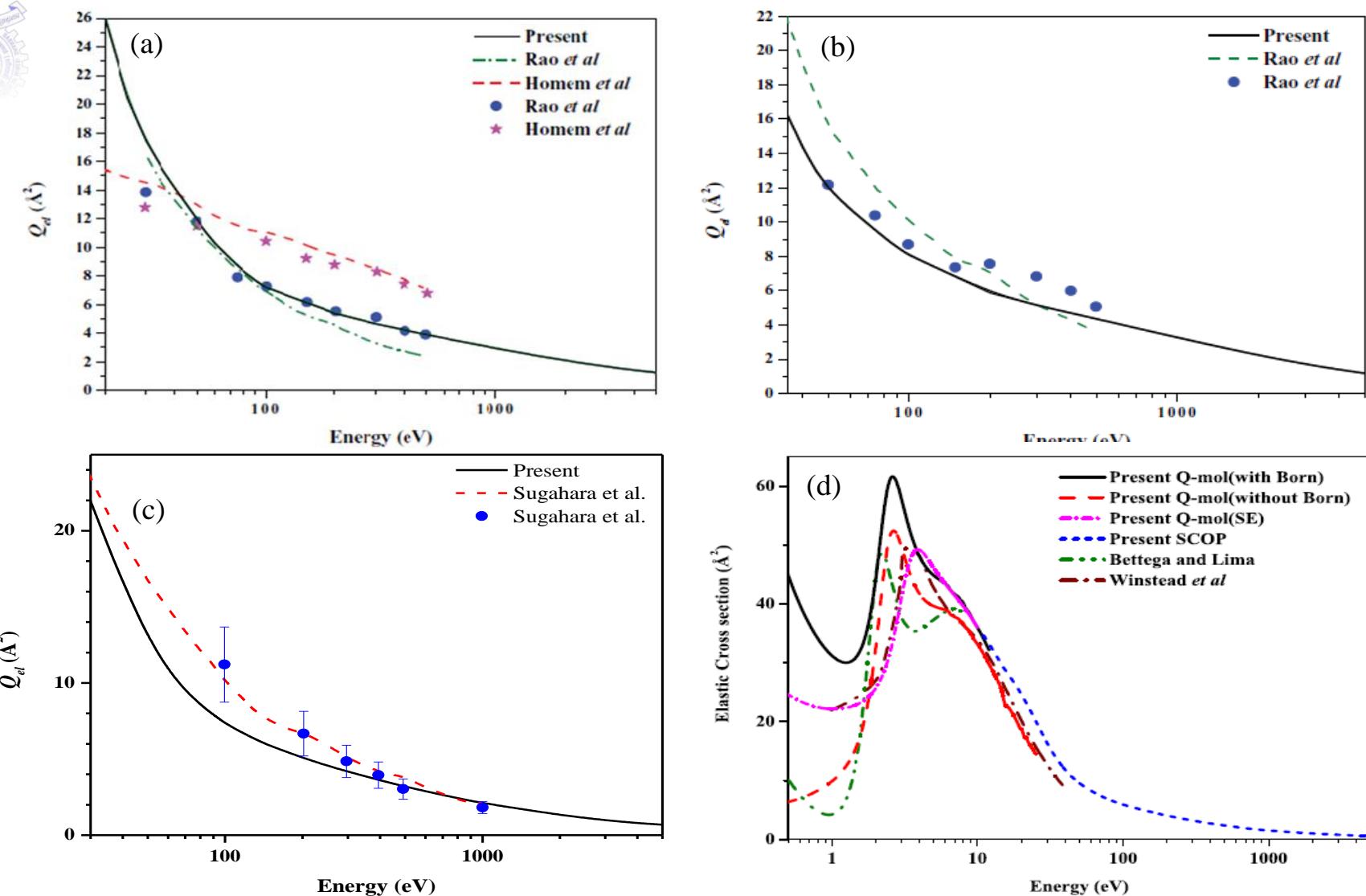
# Results: Elastic DCS

## U2012: F19210 DC2

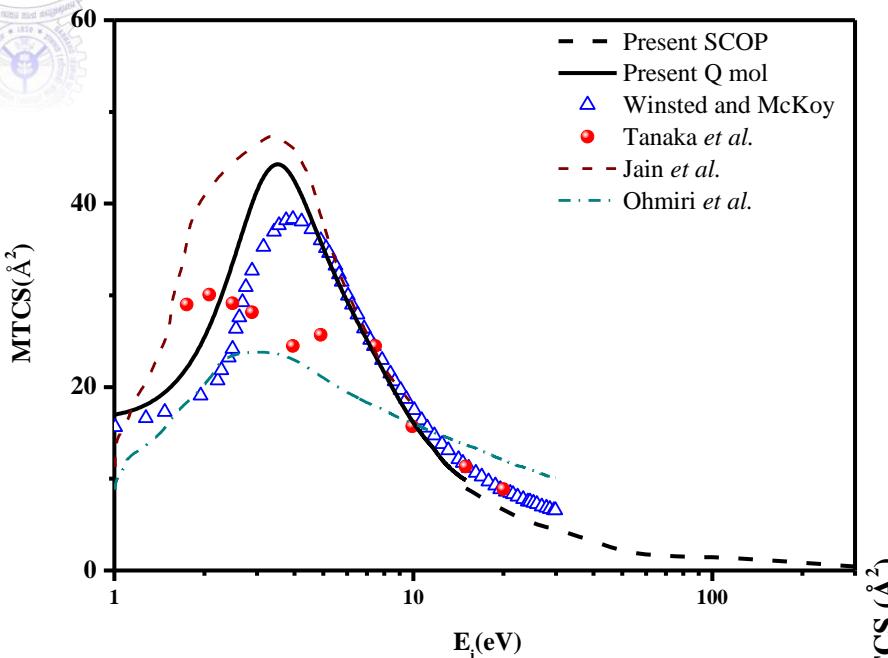


**Fig 1: DCS for e-Si<sub>2</sub>H<sub>6</sub><sup>\*</sup>**

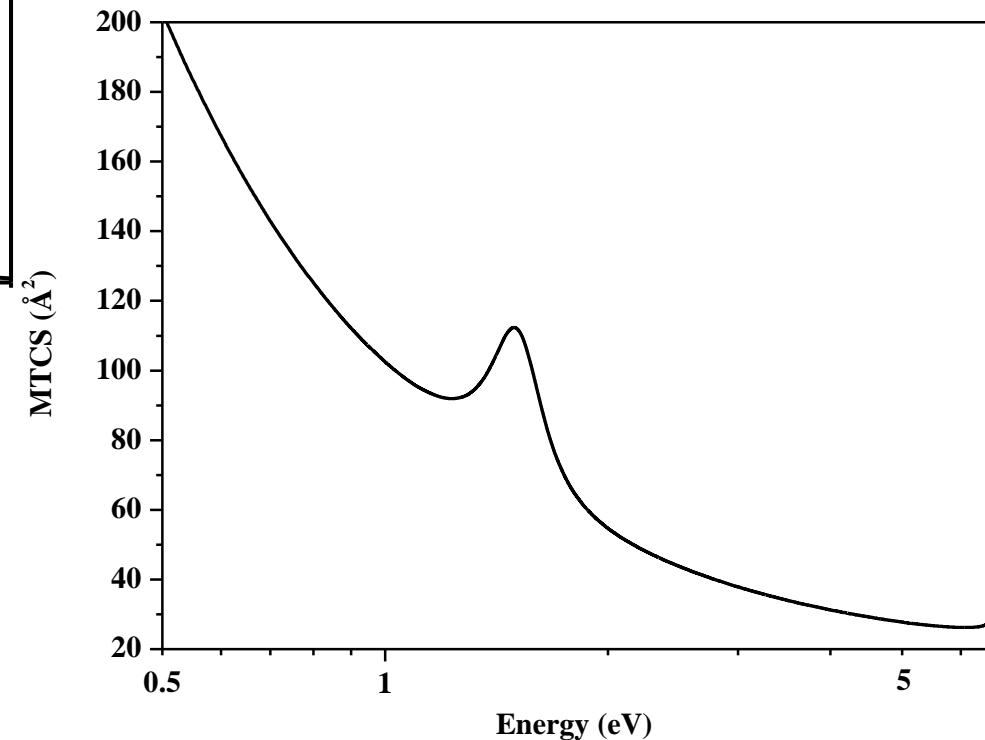
**Fig 2: DCS of e-AsH<sub>3</sub><sup>#</sup>**



**Fig 3:**  $Q_{el}$  of (a) $e\text{-}(\text{CH}_3)_2\text{S}^*$ , (b) $e\text{-}(\text{CH}_3)_2\text{SO}^*$ , (c) $e\text{-}(\text{CH}_3)_2\text{O}^\#$  (d)  $e\text{-AsH}_3^+$



**Fig 6: MTCS for  $e^-$ - $\text{SiH}_4$  scattering\***



**Fig 7: MTCS for  $e^-$ - $\text{HCCCN}$  scattering<sup>#</sup>**

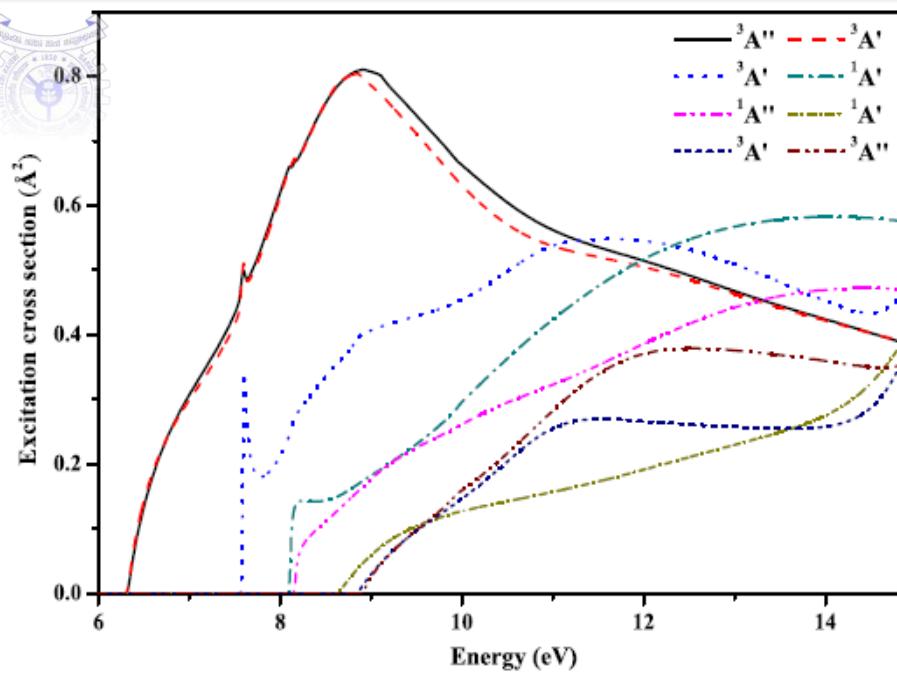


Fig 8: ECS for e-AsH<sub>3</sub> scattering\*

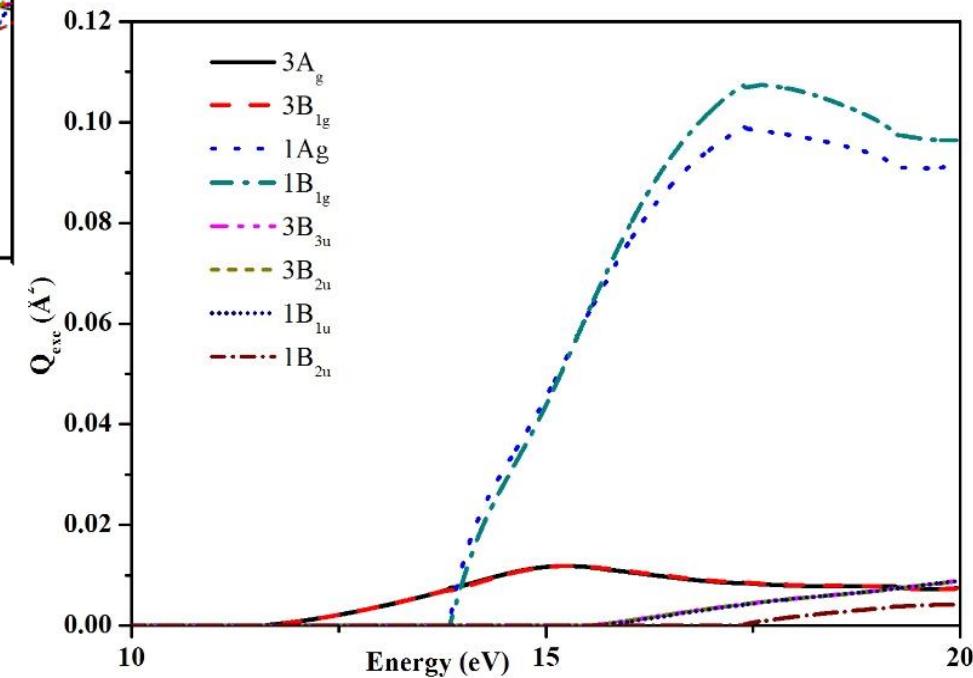
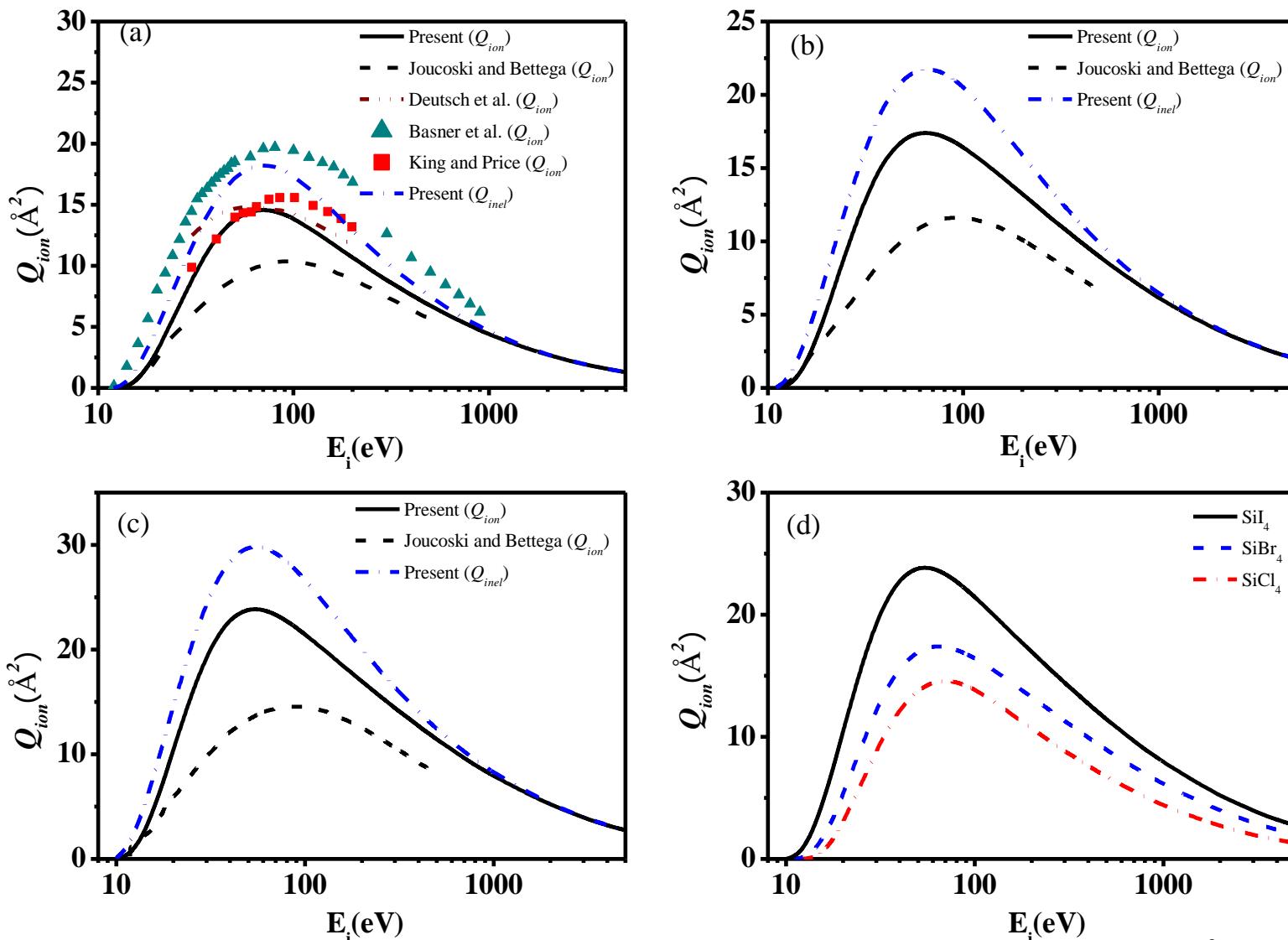


Fig 9: ECS for e-SF<sub>6</sub> scattering#



**Fig 10:**  $Q_{inel}$  and  $Q_{ion}$  of (a) e-SiCl<sub>4</sub>, (b) SiBr<sub>4</sub>, (c) SiI<sub>4</sub> scattering in  $\text{\AA}^2$ .

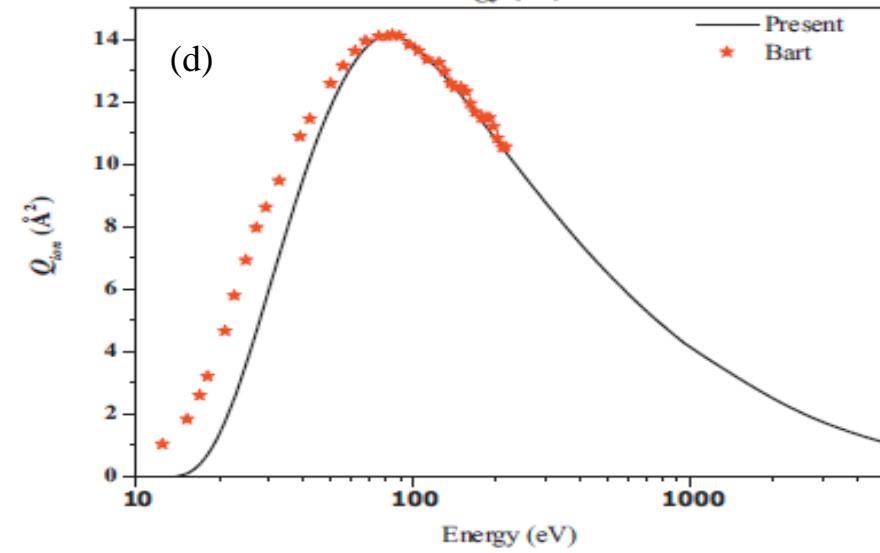
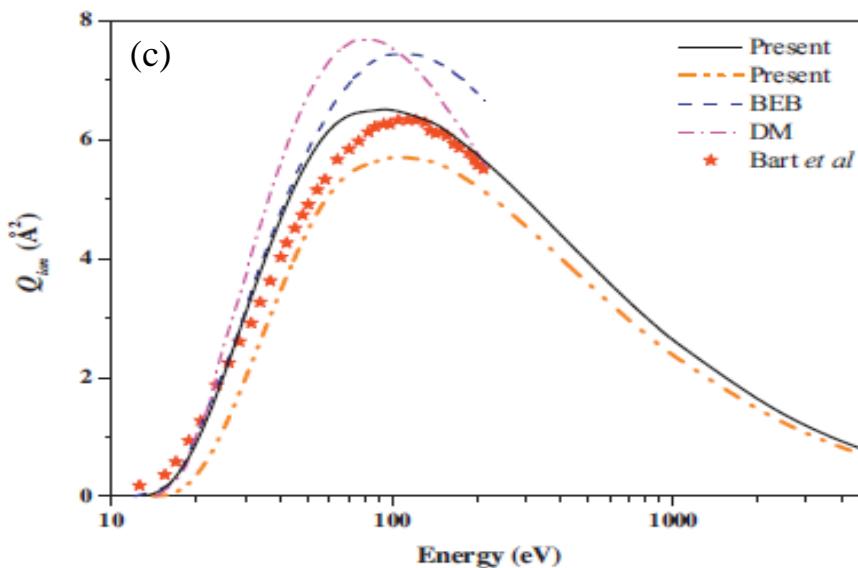
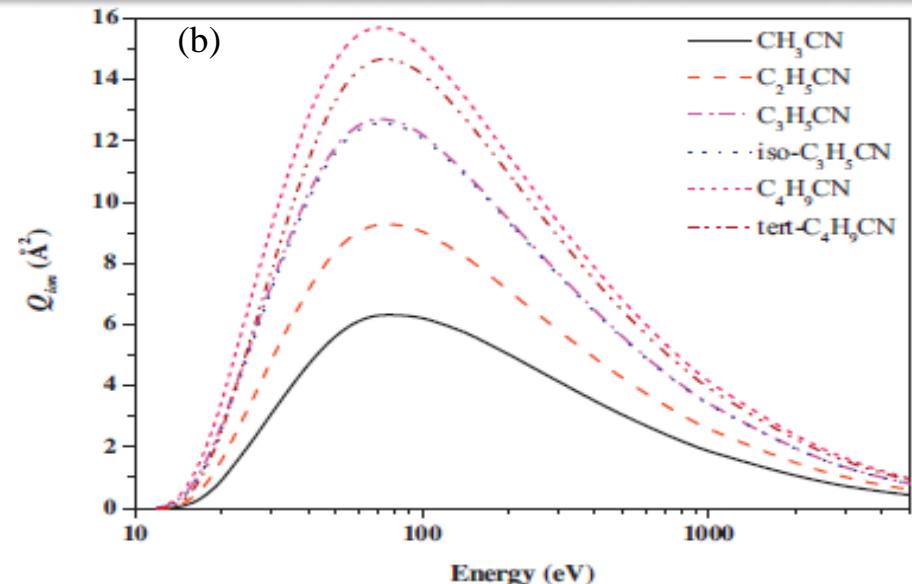
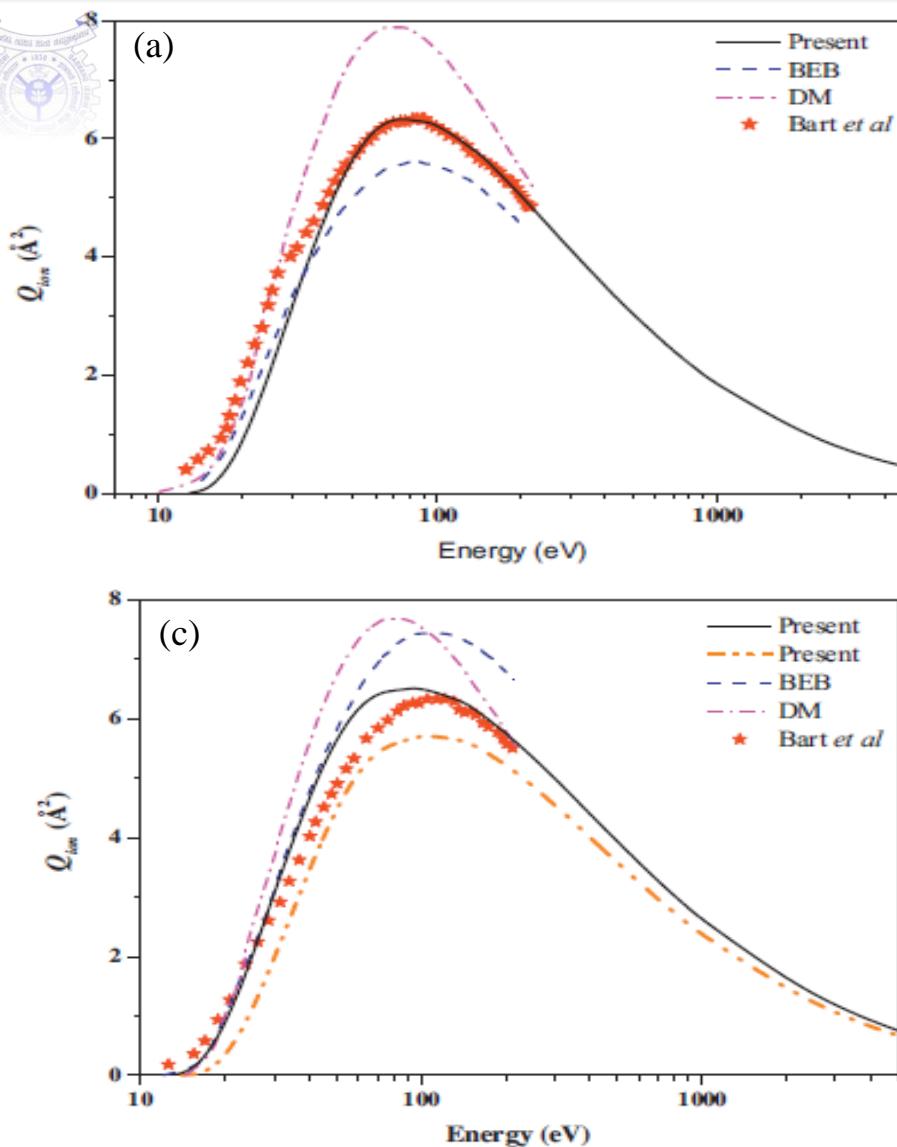
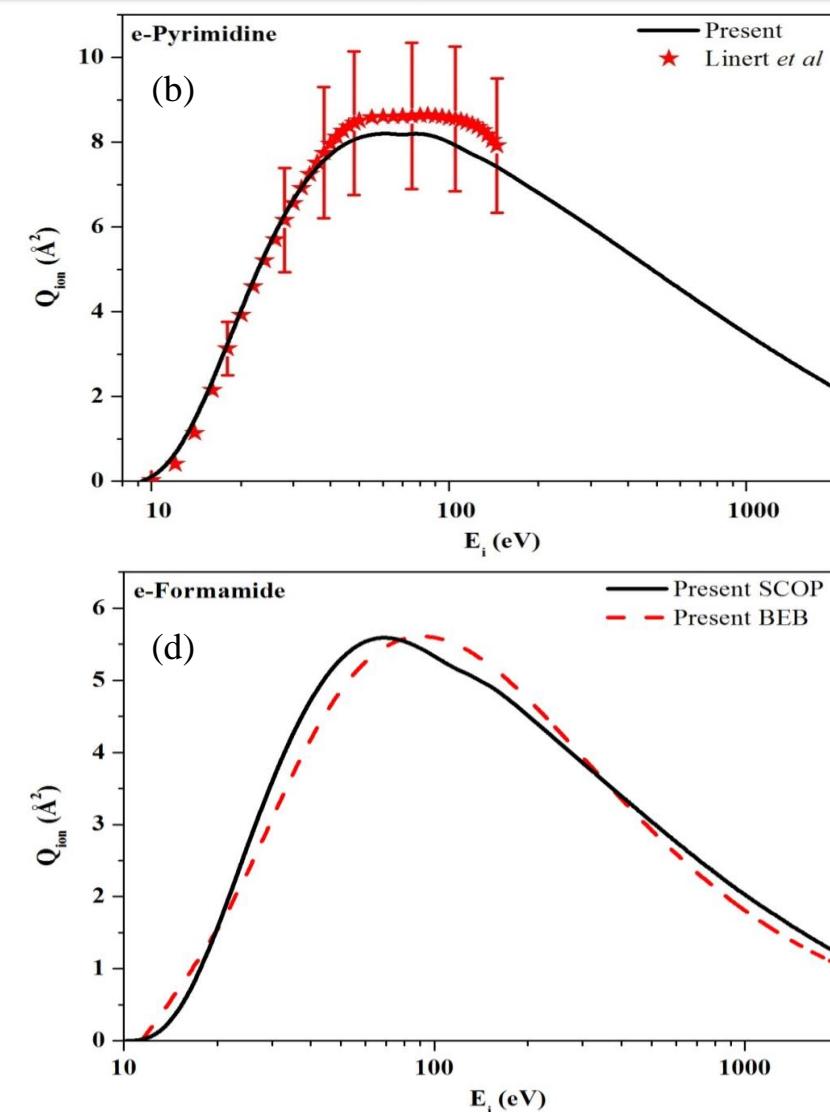
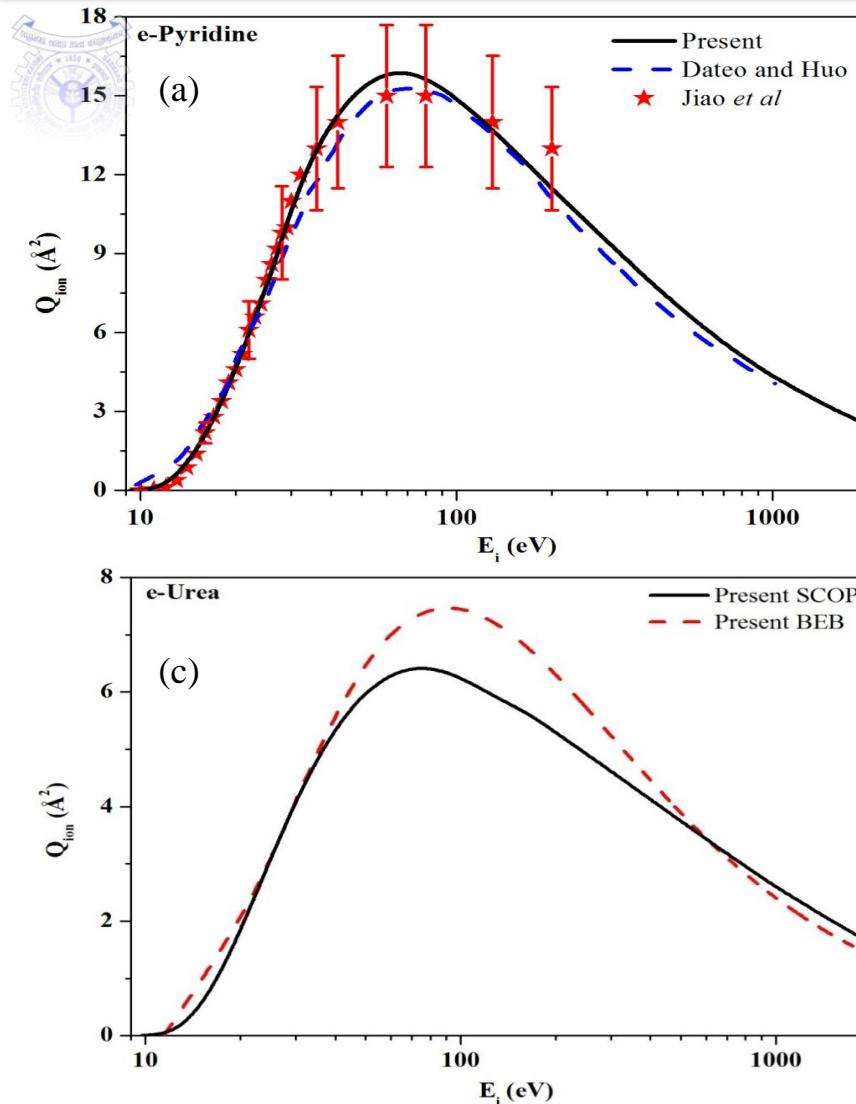
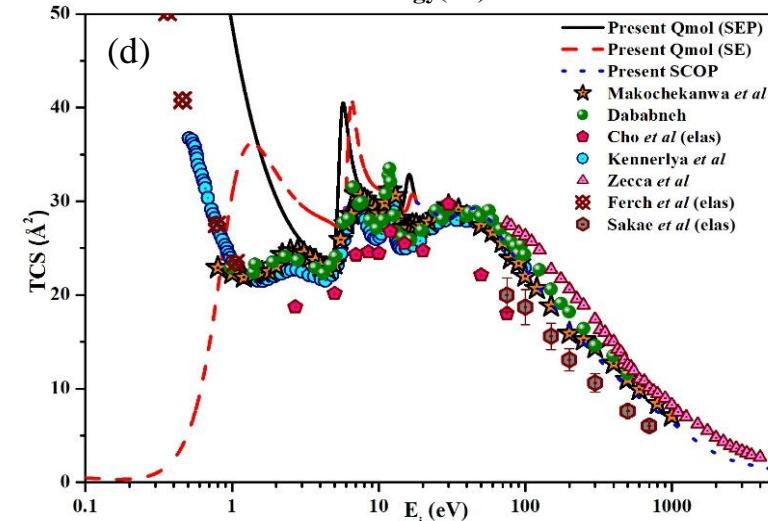
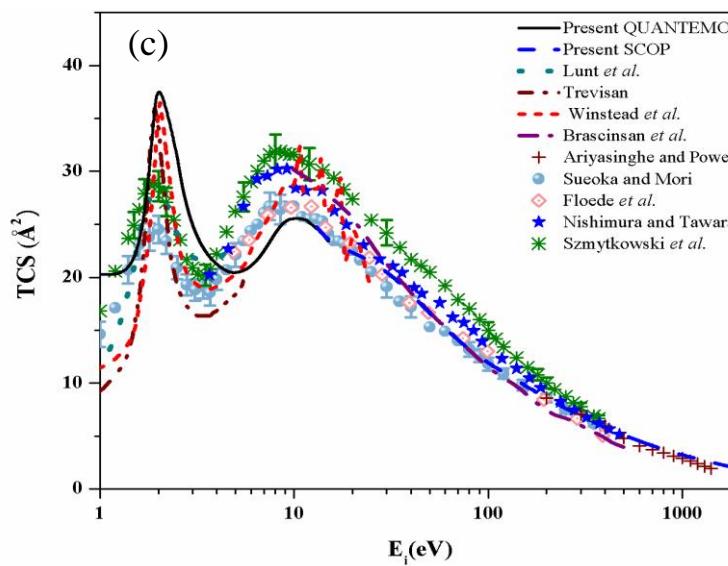
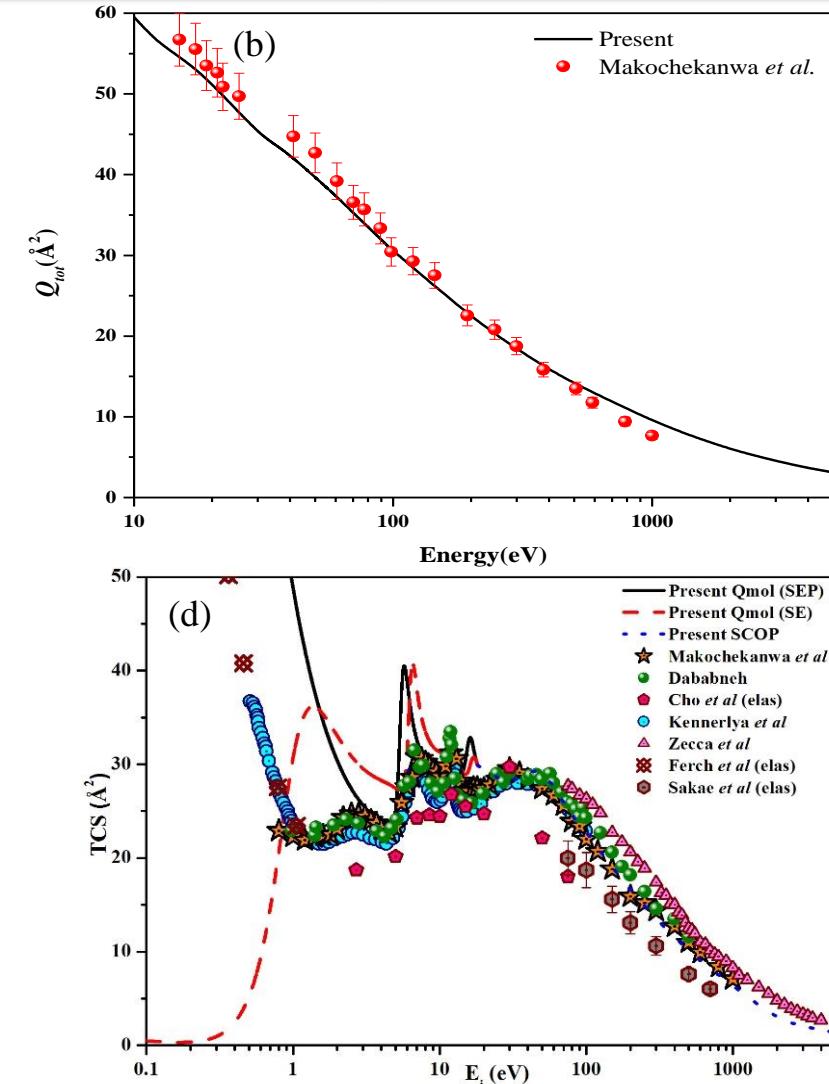
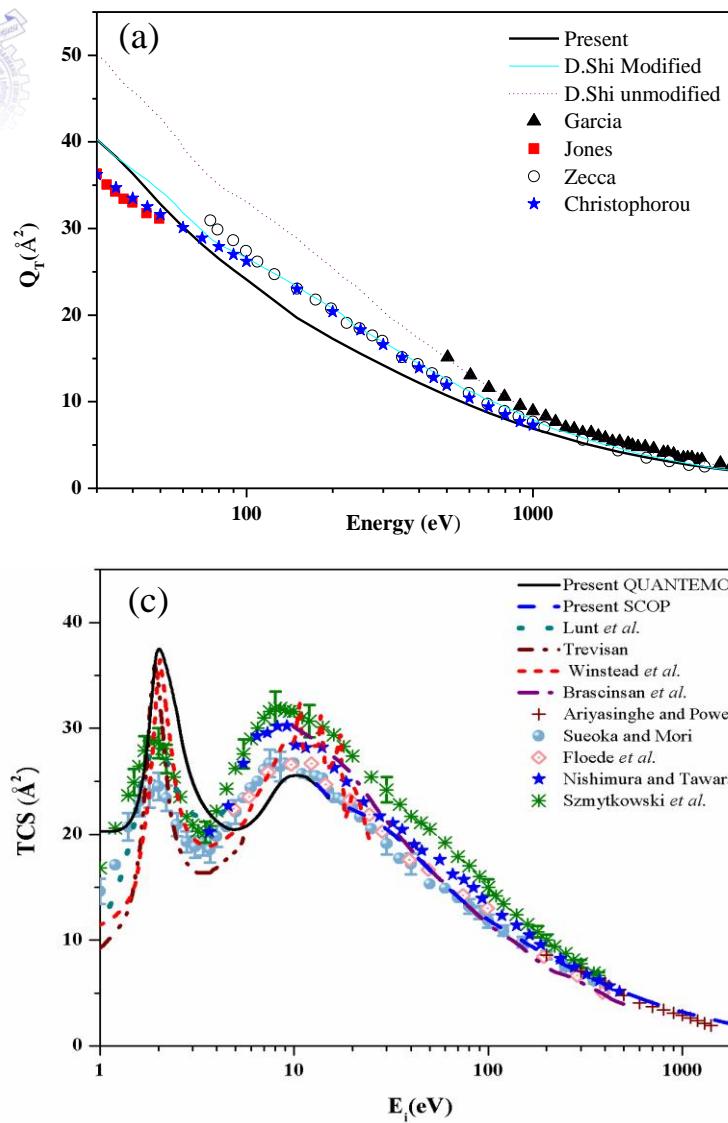


Fig 11\*:  $Q_{ion}$  of (a) e- $\text{CH}_3\text{CN}$ , (b) e- $\text{C}_n\text{H}_{2n-1}\text{CN}$ ; n=1-4, (c) e- $\text{CF}_3\text{CN}$  (d) e- $\text{CCl}_3\text{CN}$



**Fig. 12:  $Q_{ion}$  of (a) e-Pyridine, (b) e-Pyrimidine, (c) e-Urea (d) e-Formamide scattering\***



**Fig. 13:  $Q_T$  of (a)  $^*\text{e-CF}_2\text{Cl}_2$ , (b)  $^*\text{e-(C}_n\text{H}_{2n-1})_2\text{S}$ ; n=1-3, (c)  $\text{e-C}_2\text{H}_4$   $^*(\text{d})$   $^@\text{e-SF}_6$**

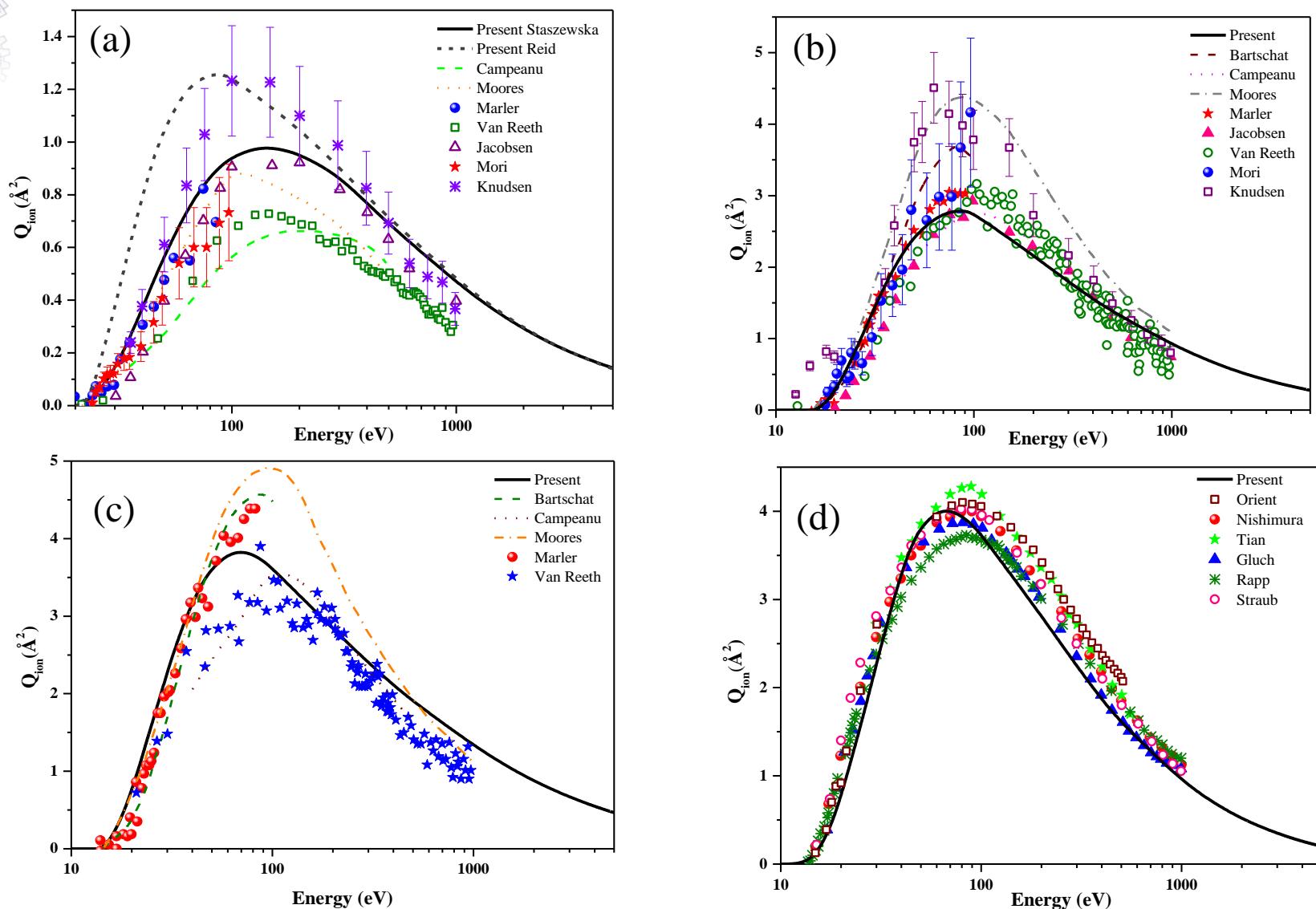
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# Results: Positron scattering

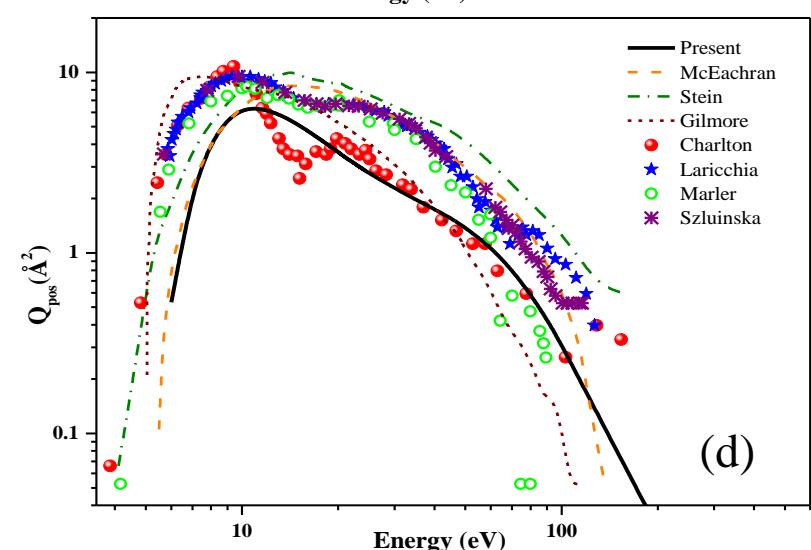
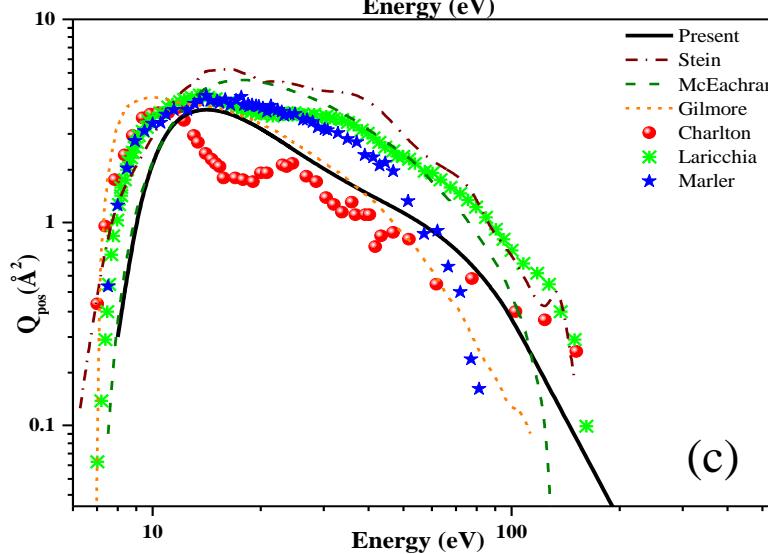
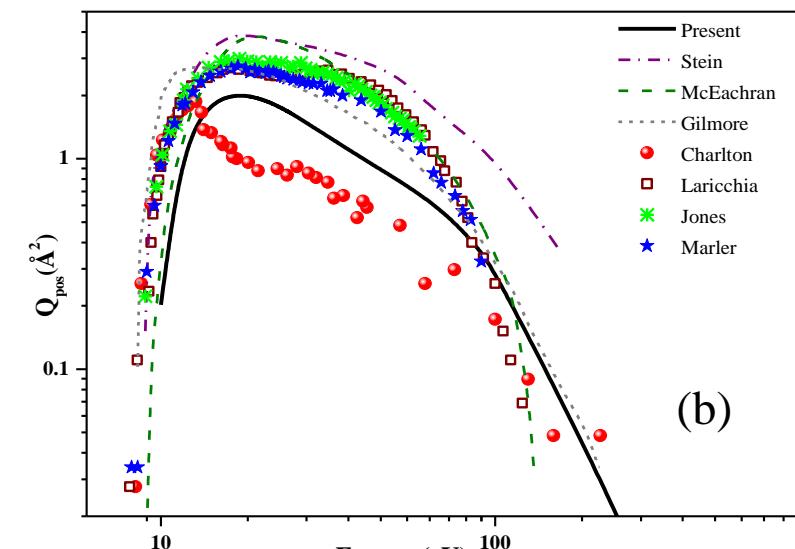
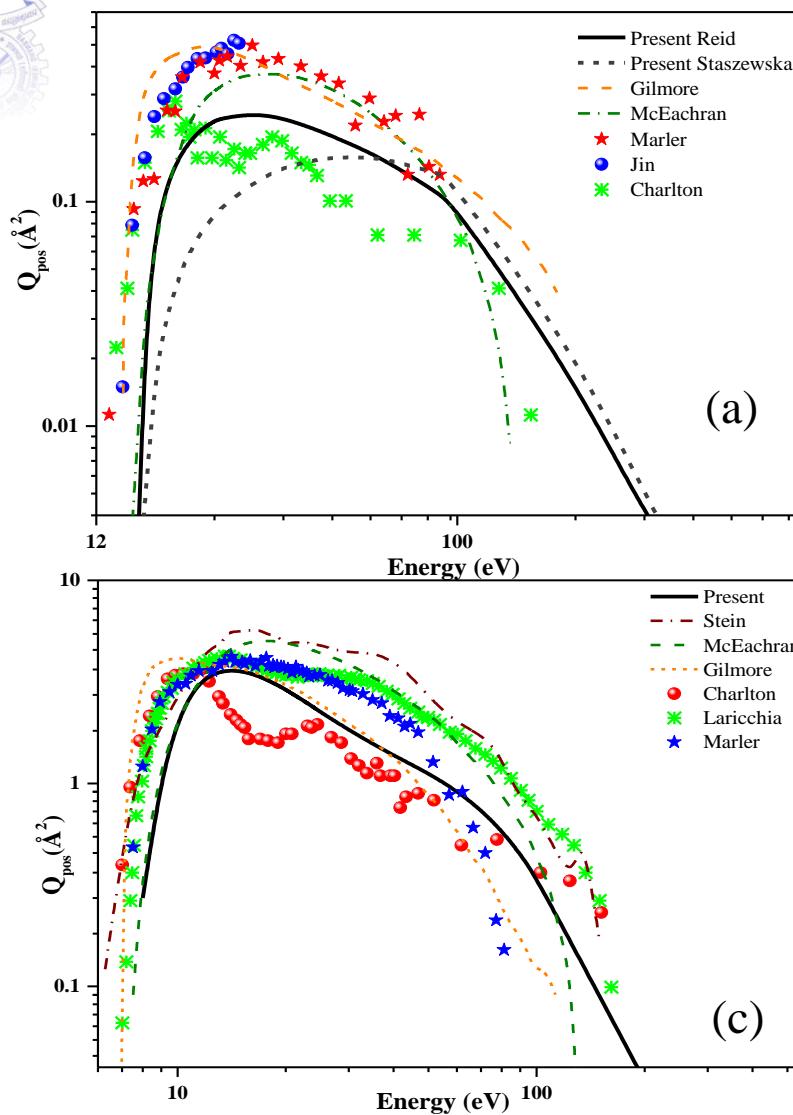
परिणाम: पॉजिट्रन स्कैटरिंग

## □ **Positron Scattering Cross Sections**

- ❖ **Direct ionization**
- ❖ **Positronium formation**
- ❖ **Total ionization**
- ❖ **Total cross section**



**Fig 16:**  $Q_{ion}$  of (a)  $e^+ - \text{Ne}$ , (b)  $e^+ - \text{Ar}$ , (c)  $e^+ - \text{Kr}$  (d)  $e^+ - \text{CH}_4$



**Fig 17:**  $Q_{pos}$  of (a)  $e^+$ -Ne, (b)  $e^+$ -Ar, (c)  $e^+$ -Kr (d)  $e^+$ -Xe scattering .

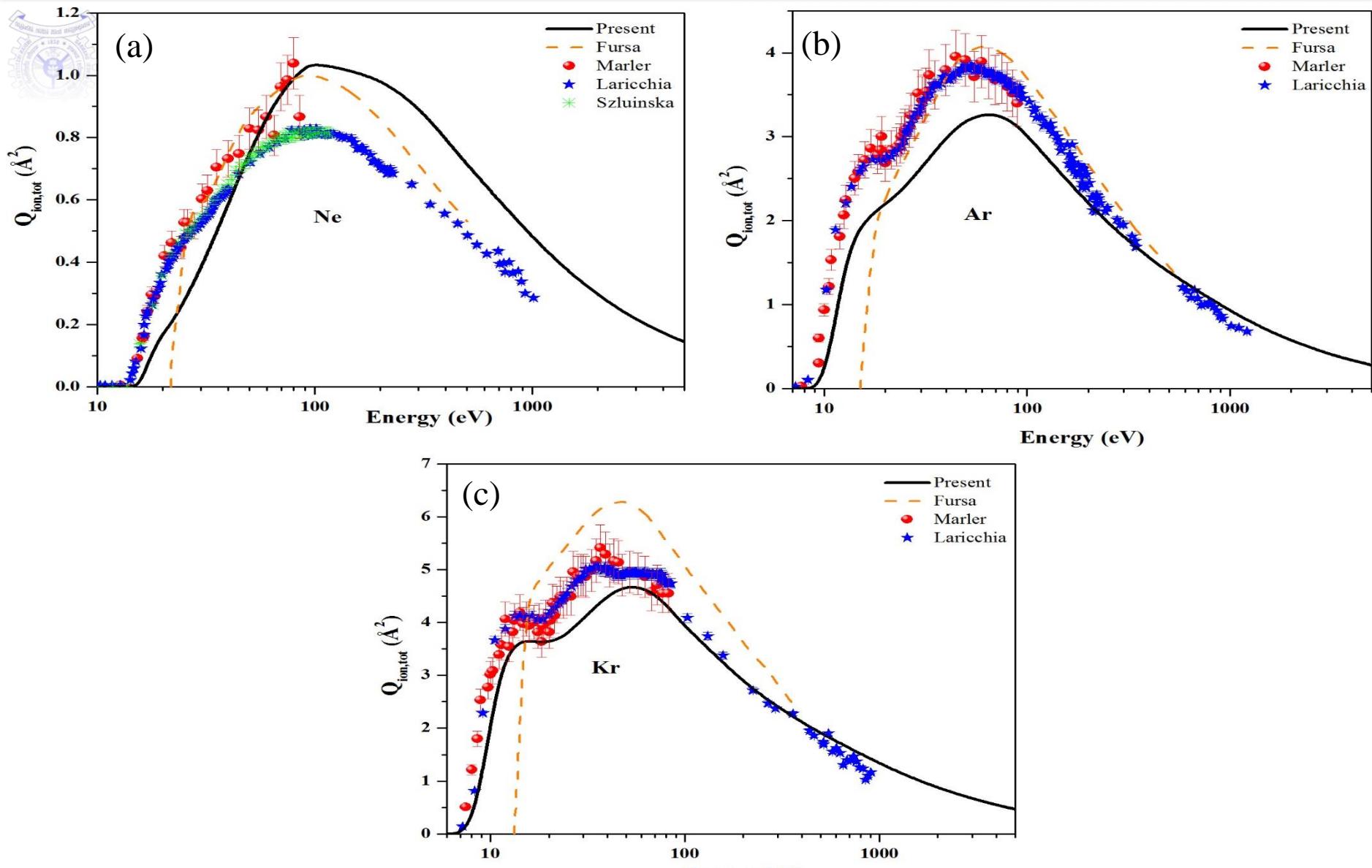
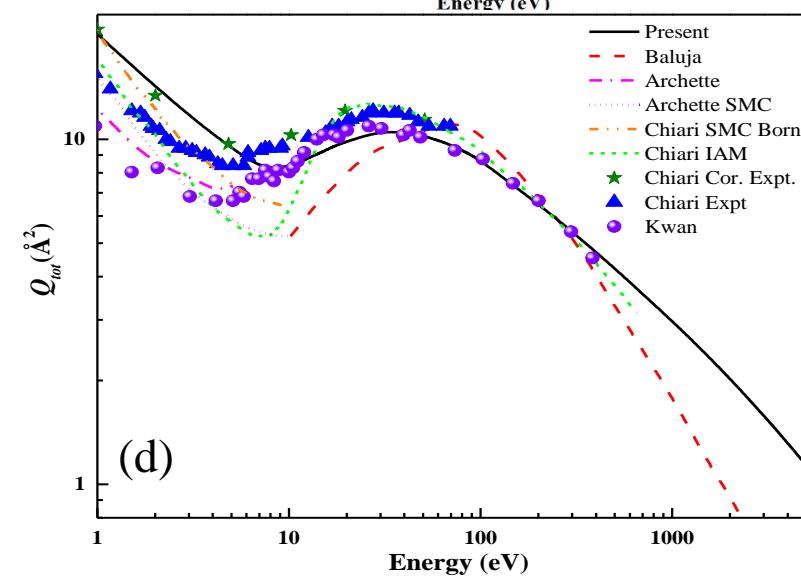
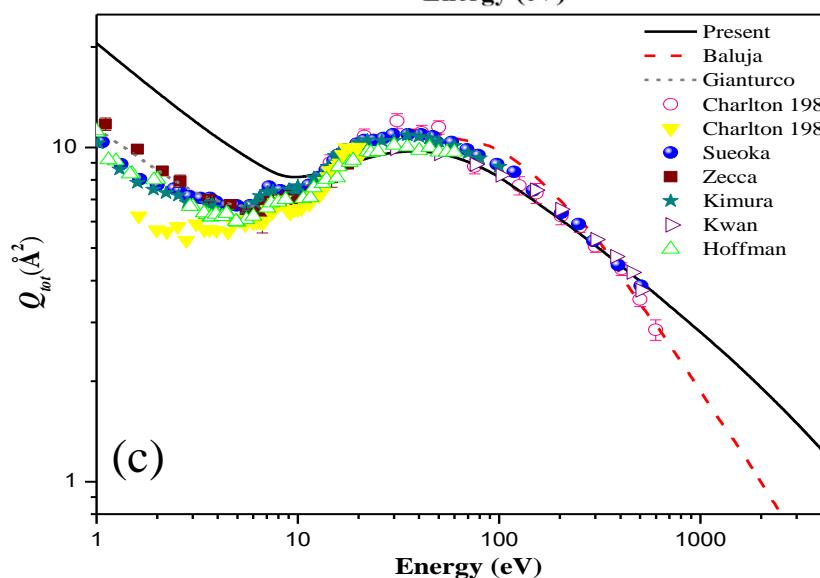
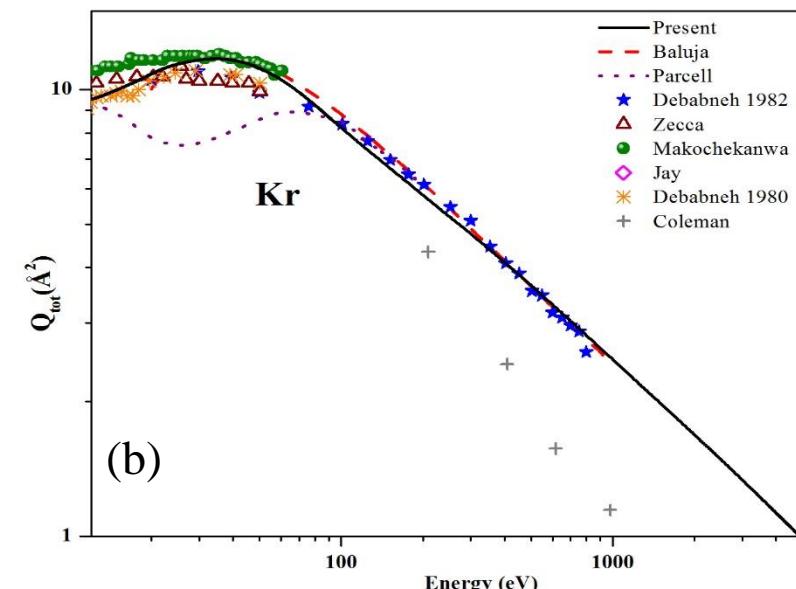
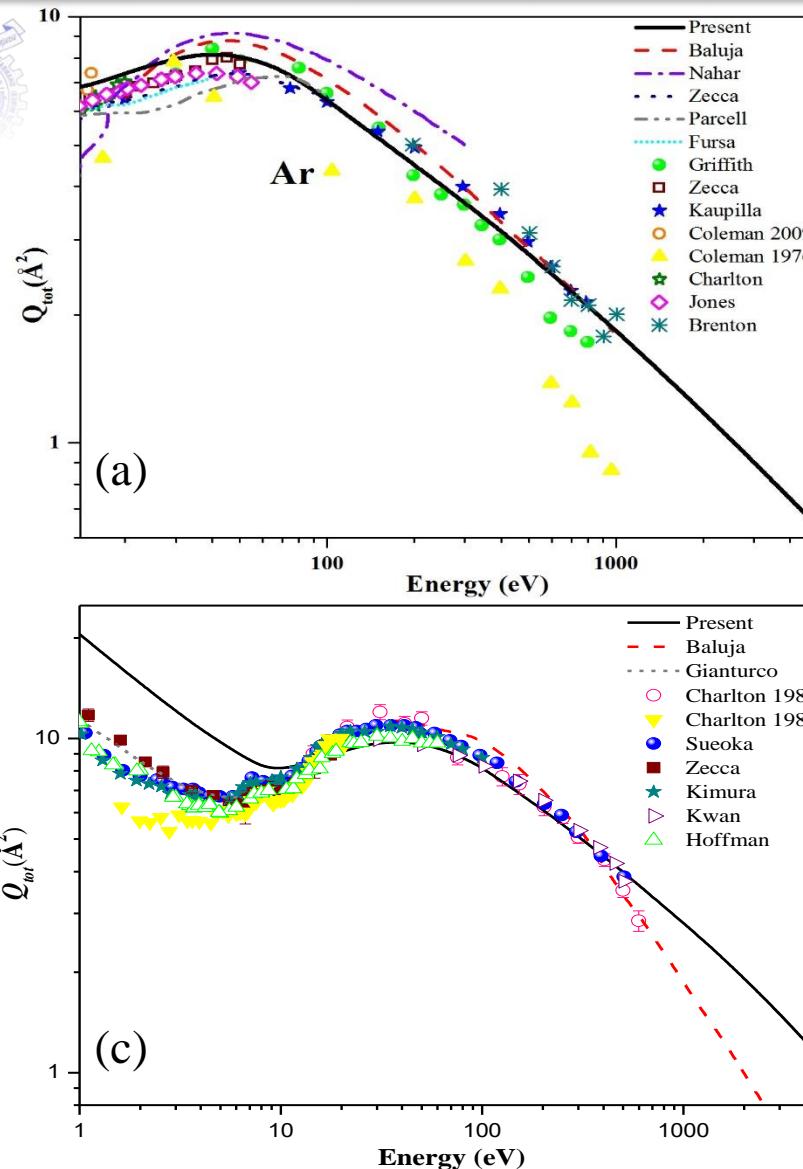


Fig 18:  $Q_{ion,tot}$  of (a)  $e^+$ -Ne, (b)  $e^+$ -Ar, (c)  $e^+$ -Kr scattering

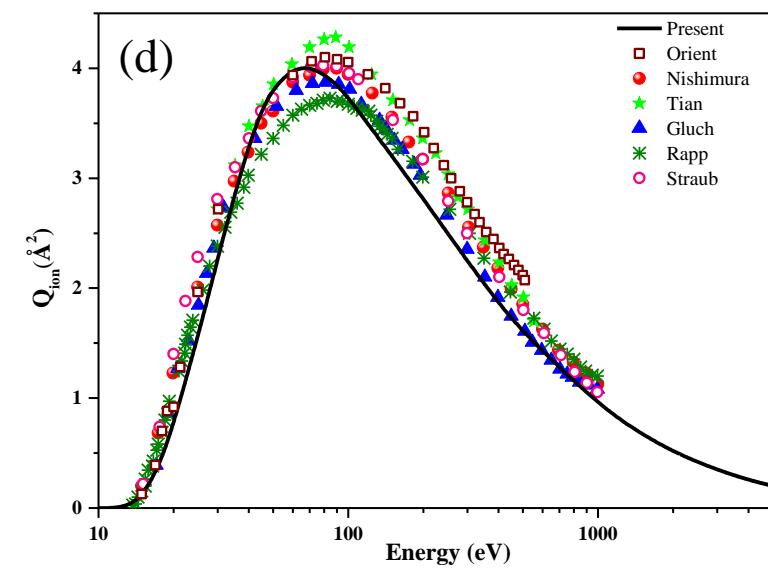
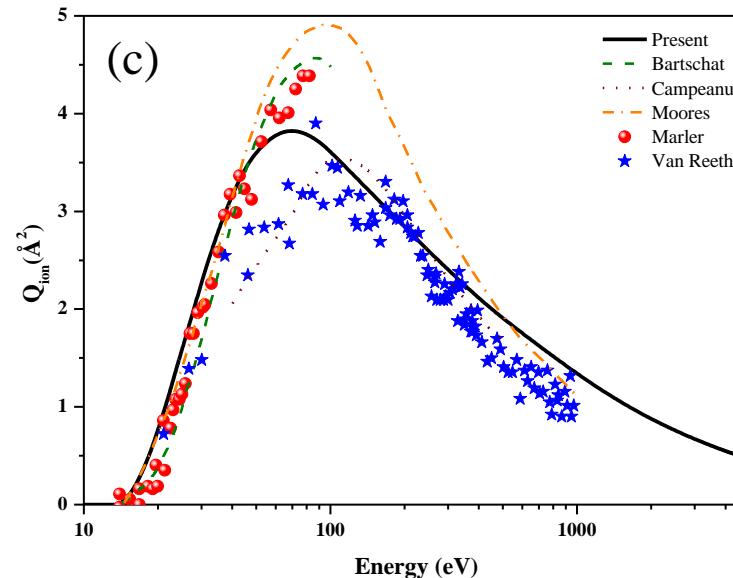
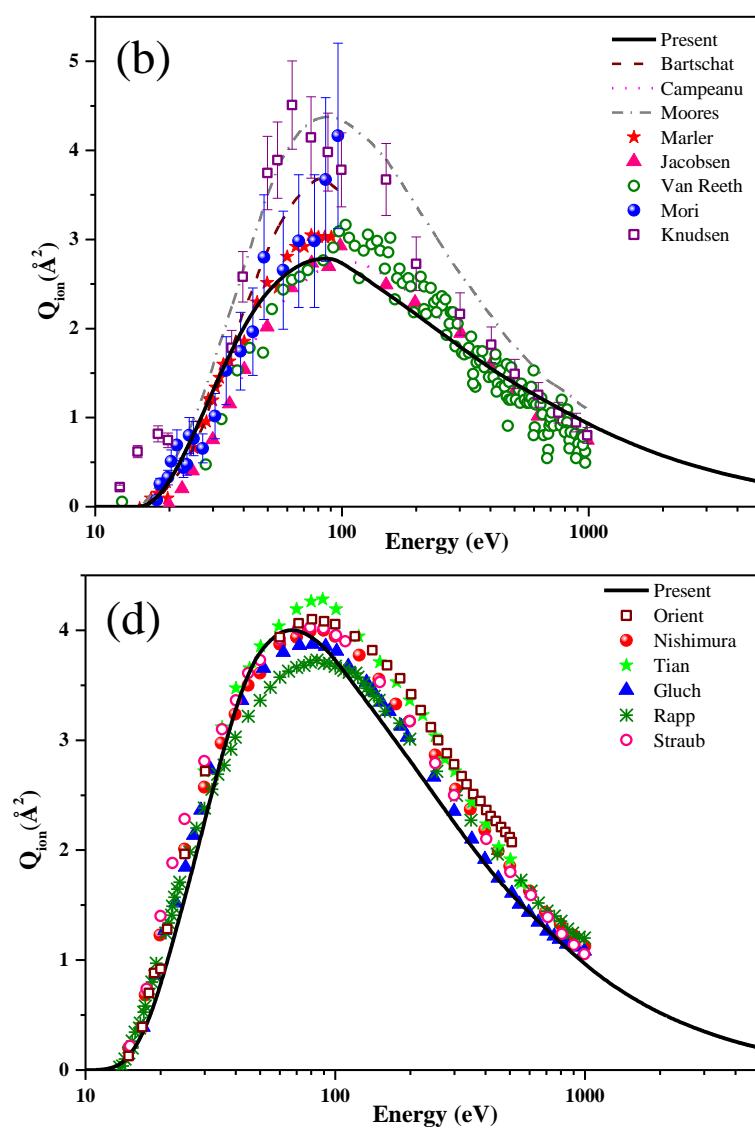
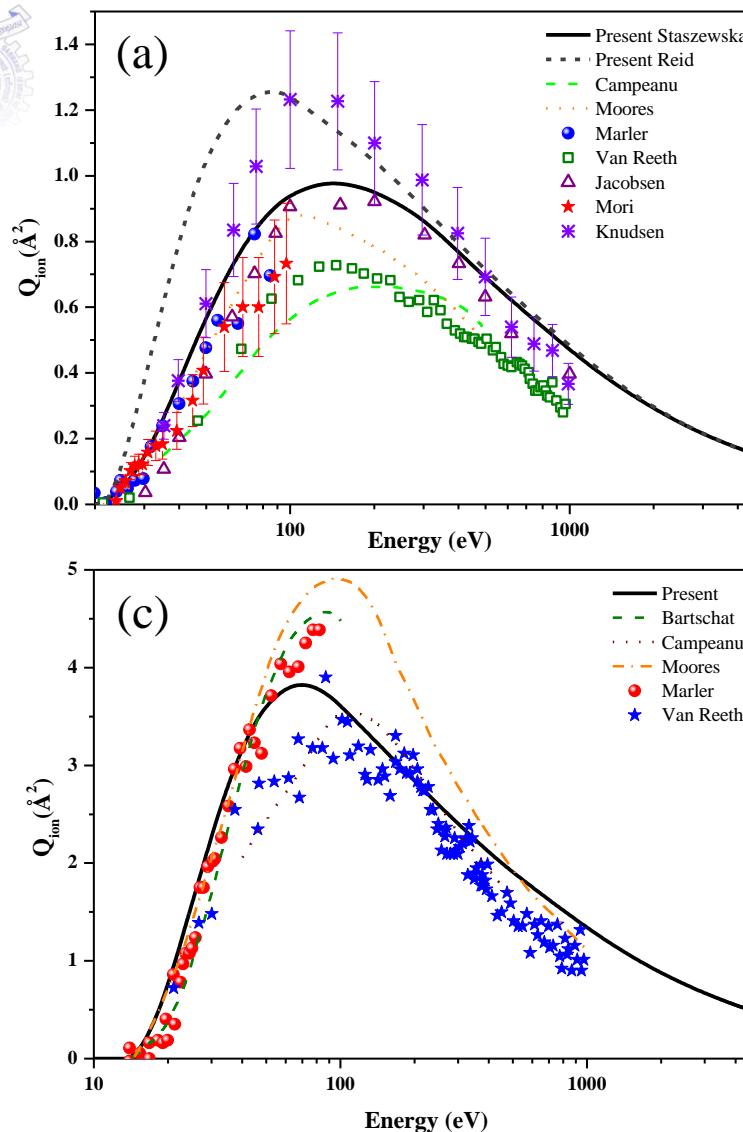


**Fig 19:  $Q_{tot}$  for (a)  $e^+$ -Ar (b)  $e^+$ -Kr (c)  $*e^+$ -CO and (d)  $*e^+$ -NO scattering in  $\text{\AA}^2$**



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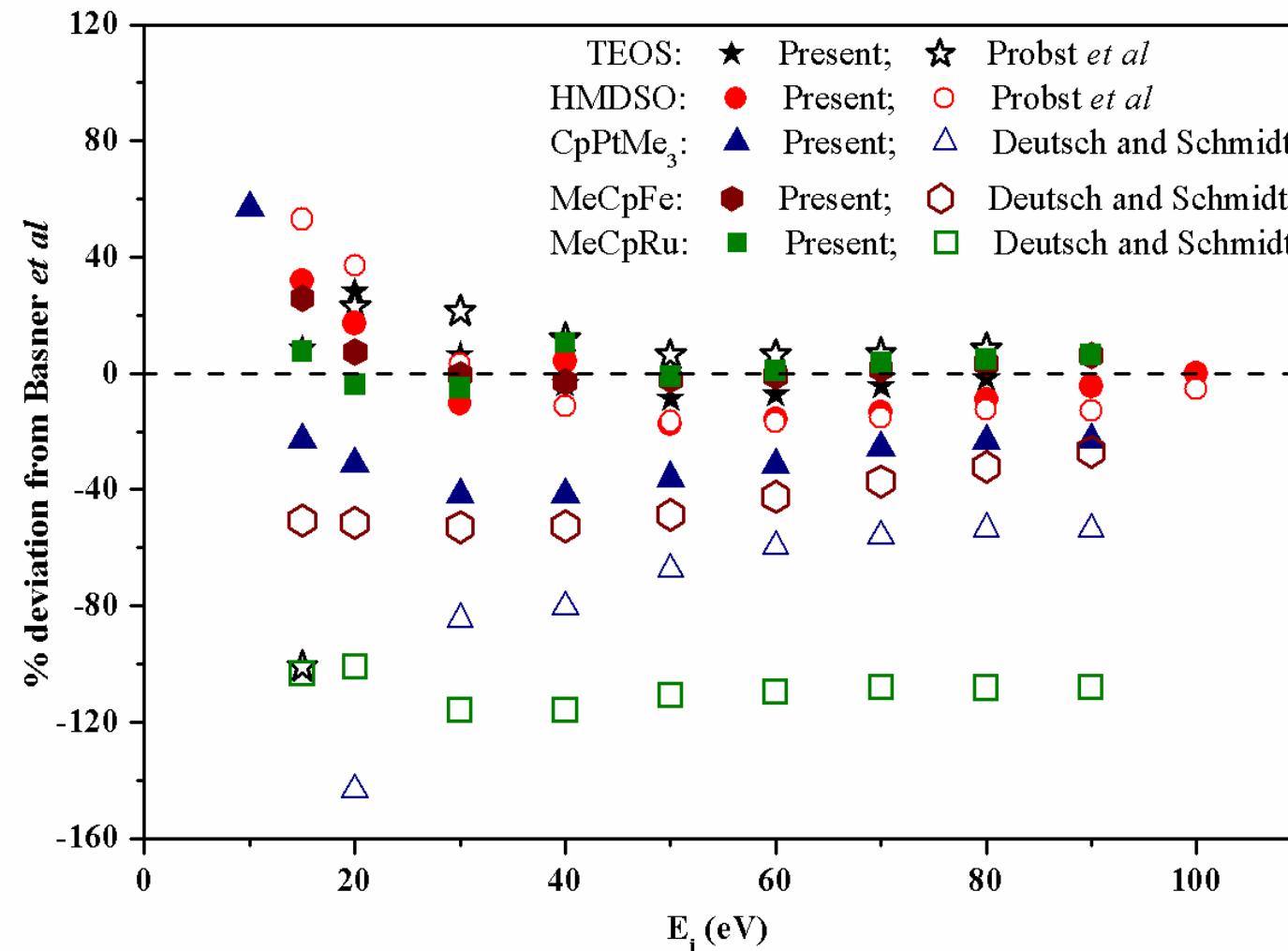


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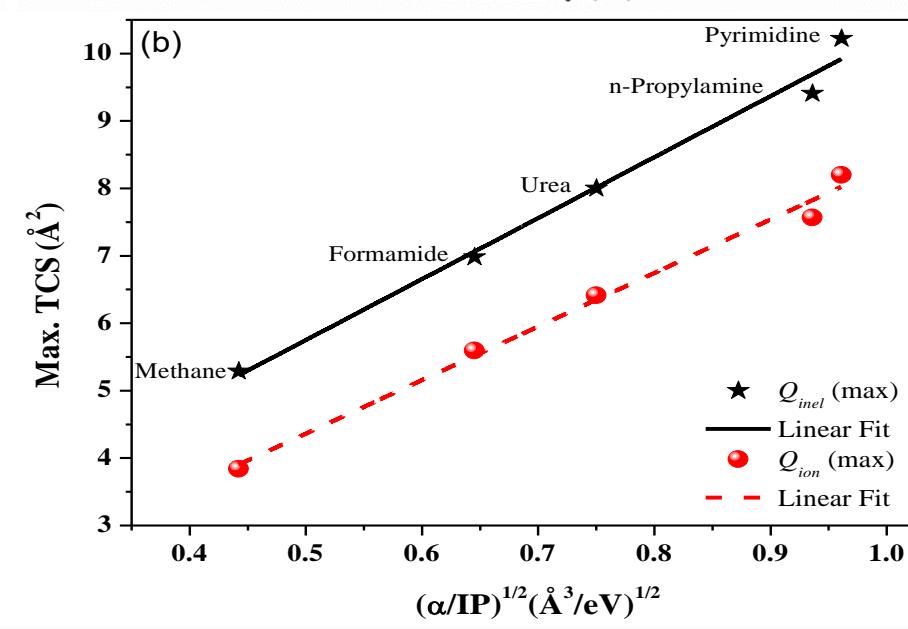
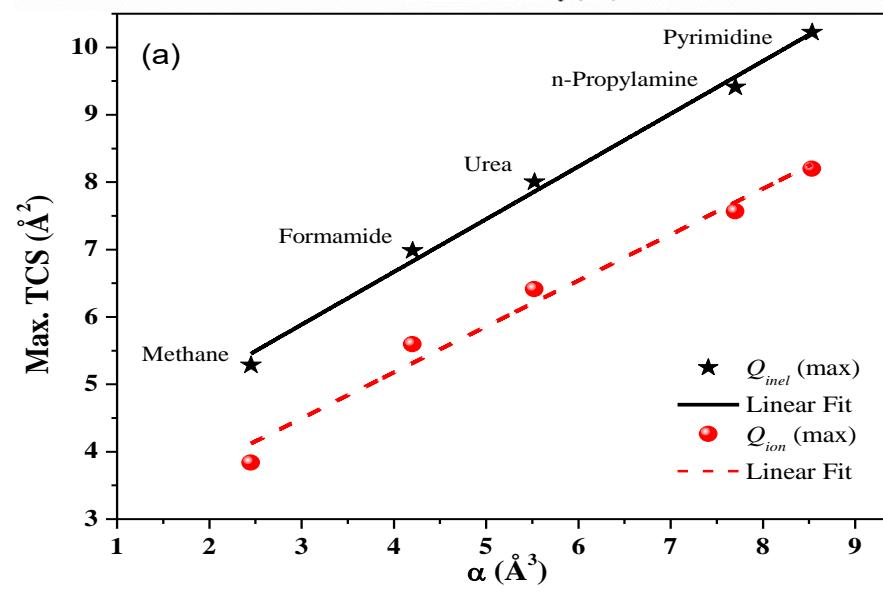
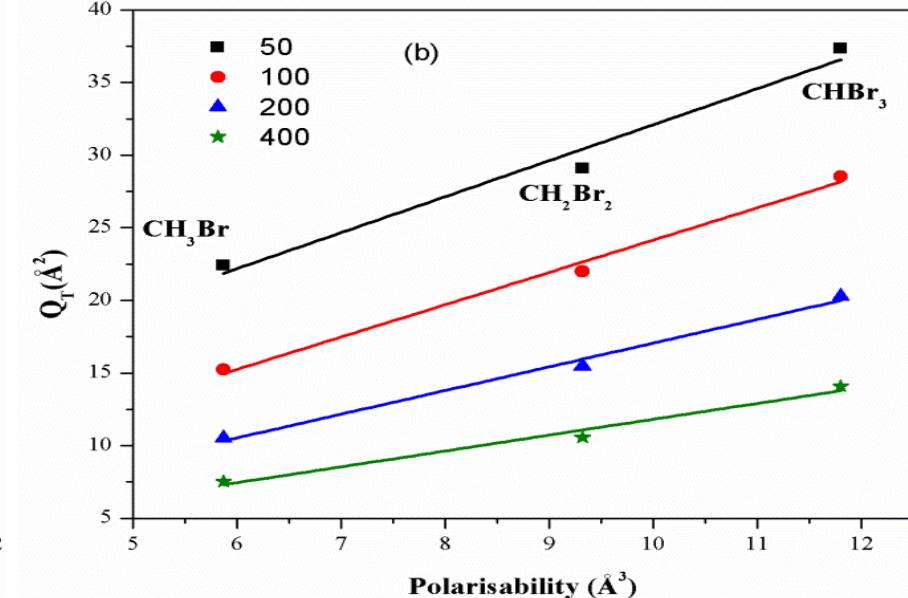
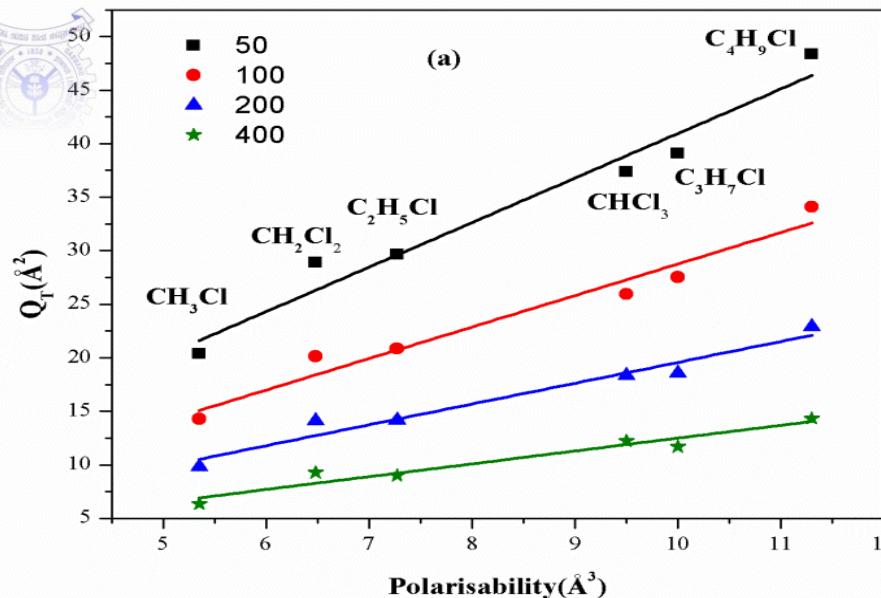


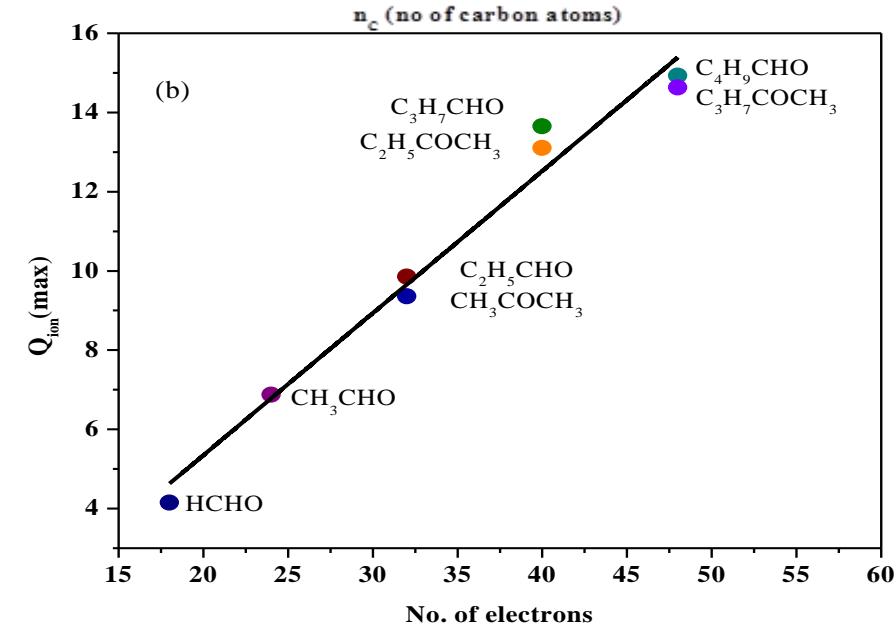
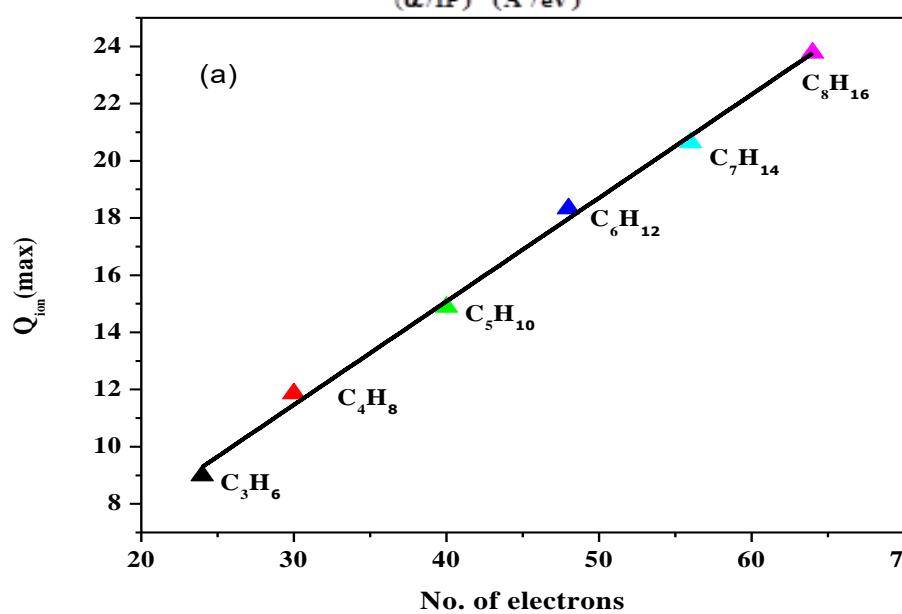
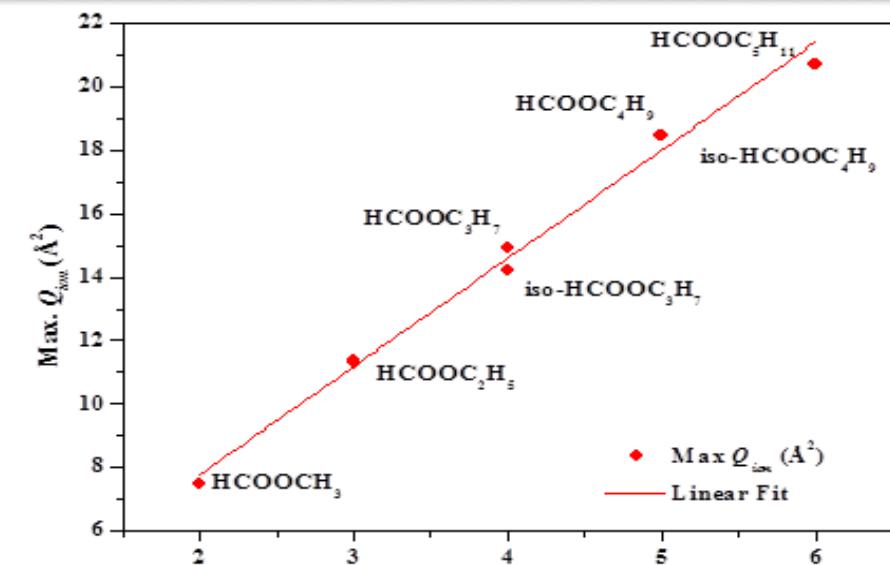
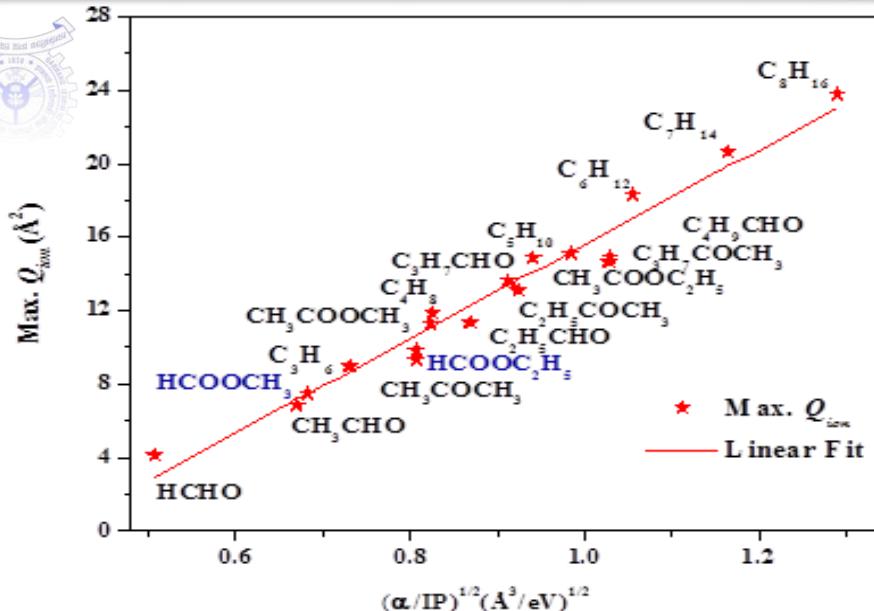
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**Fig. 17: Deviation of theoretical results from the experiments (organometallic compounds)**

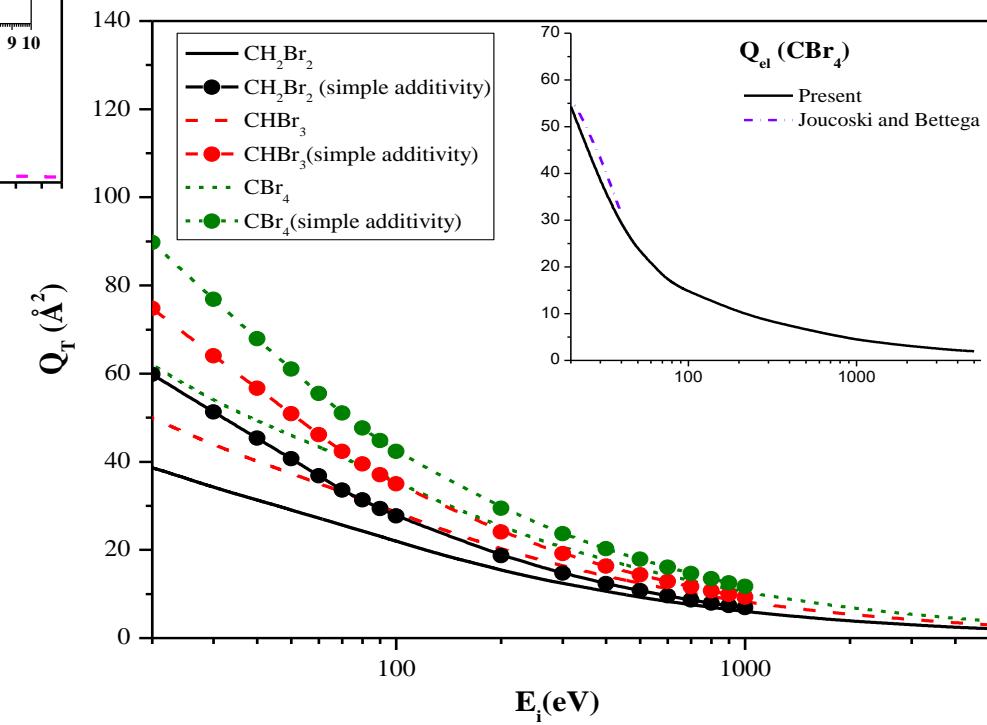
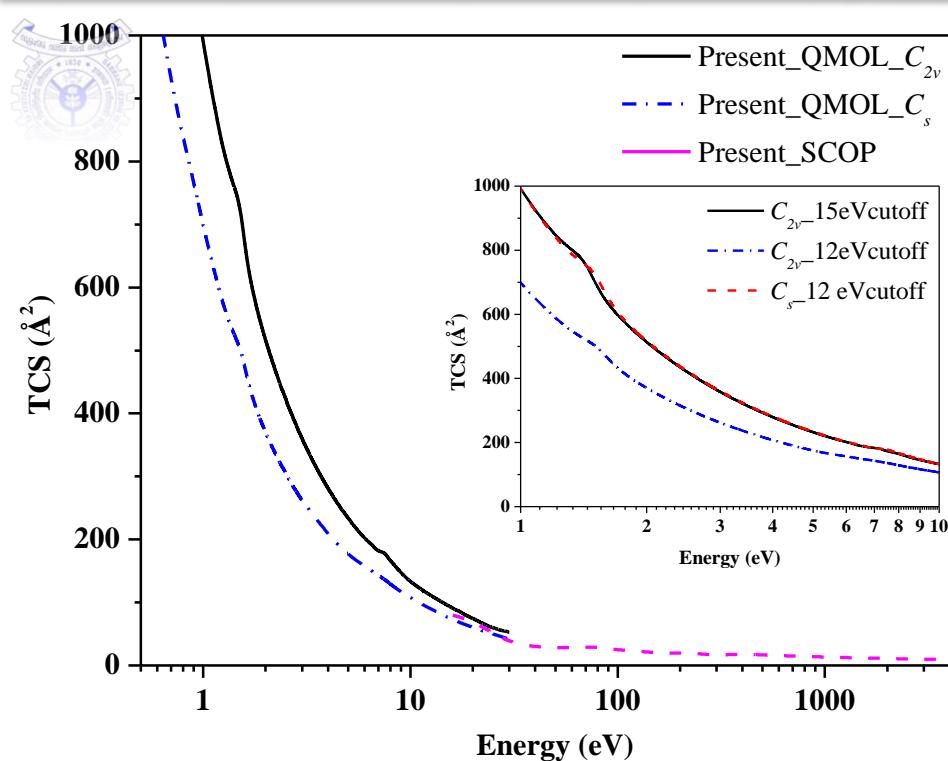


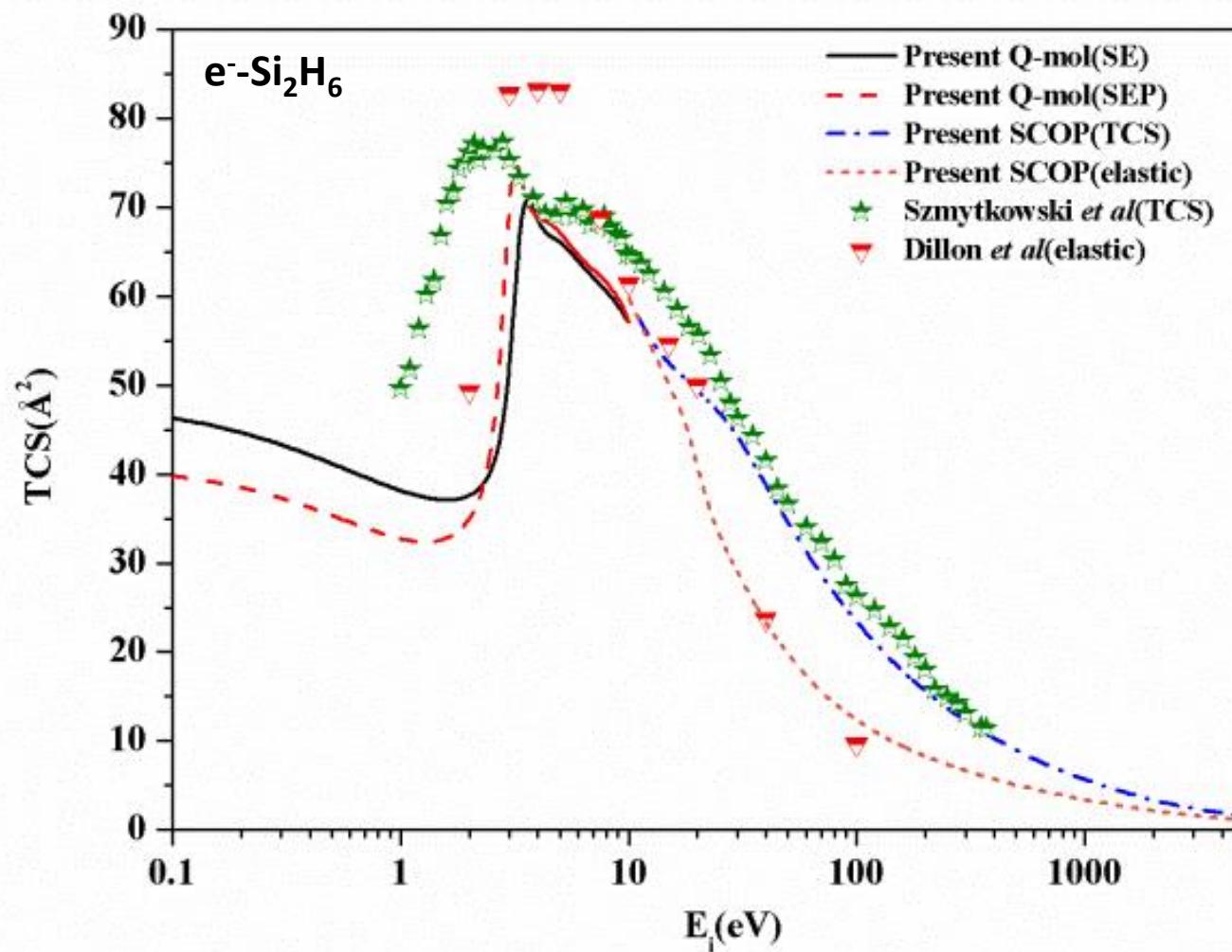




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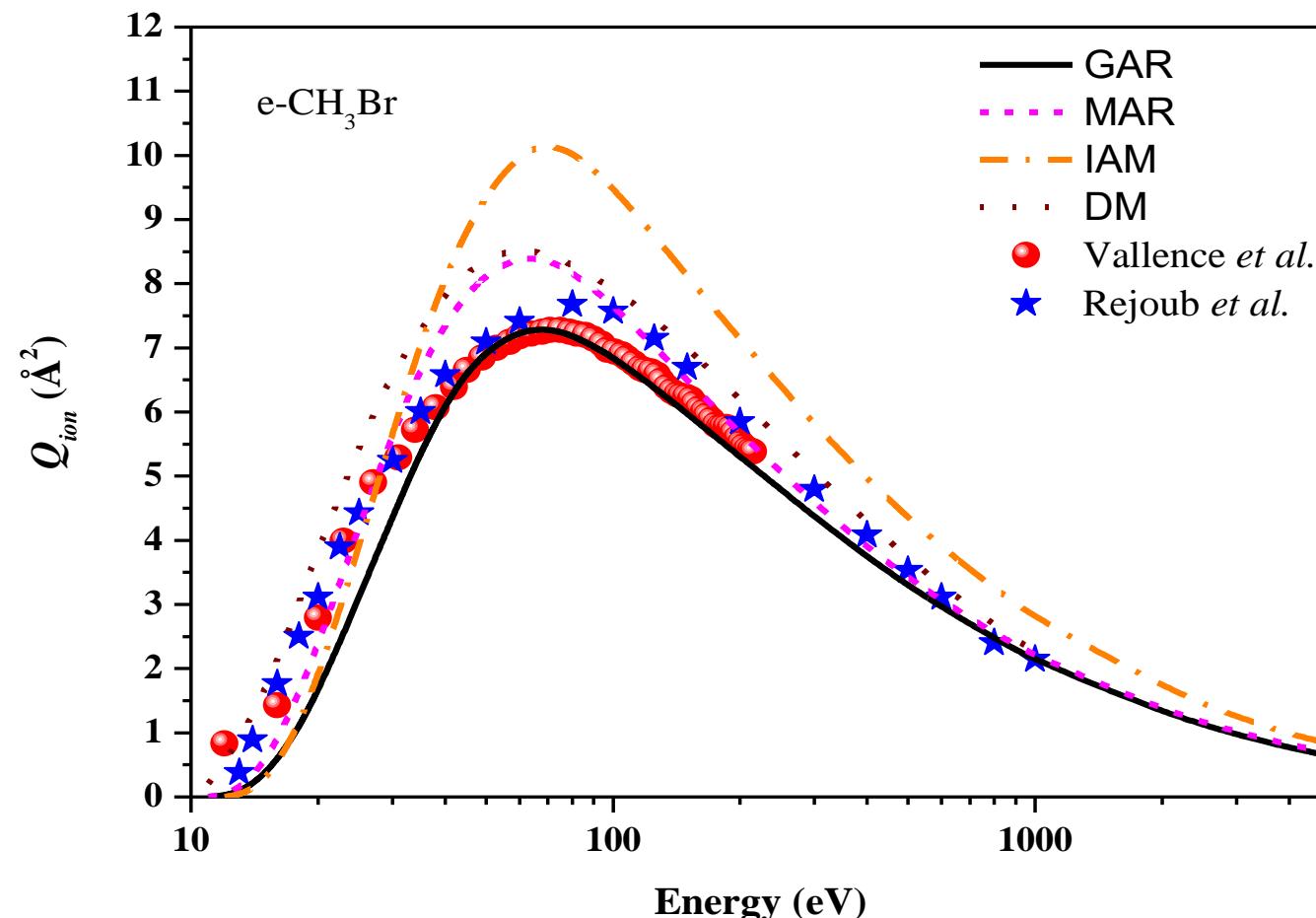
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# Uncertainty: Convergence check



**IAM:** Independent Atom Model

**MAR:** Modified Additivity Rule

**GAR:** Group Additivity Rule



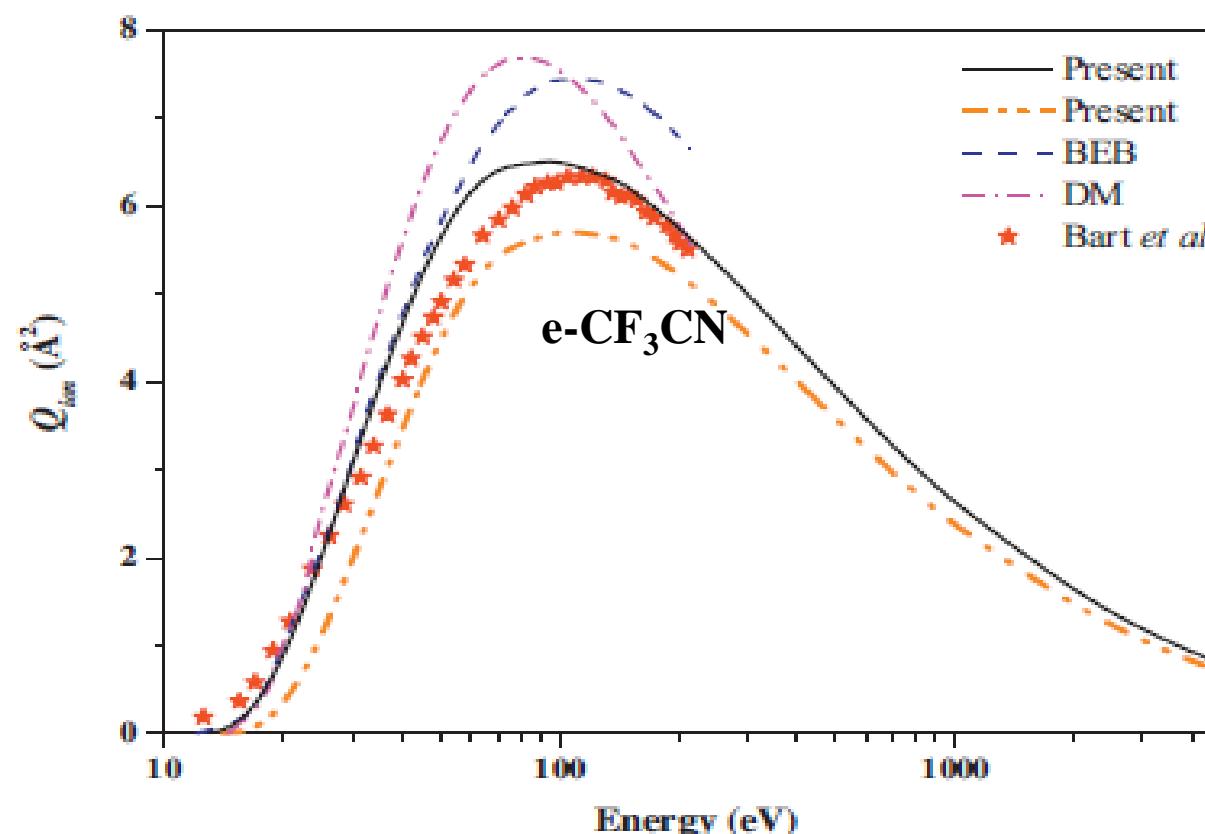
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## Sensitivity to ***Ionization Potential***

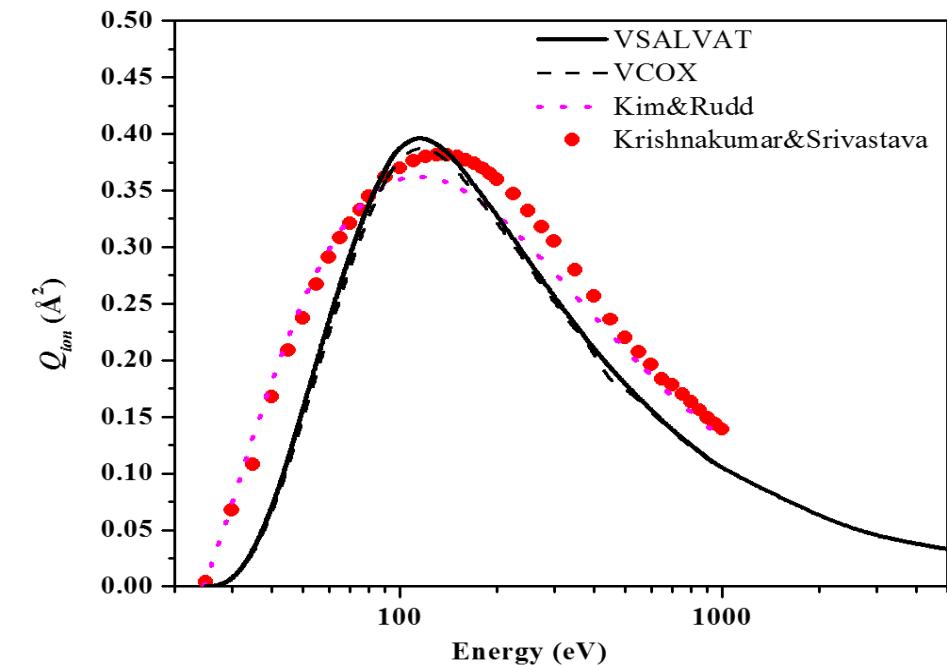
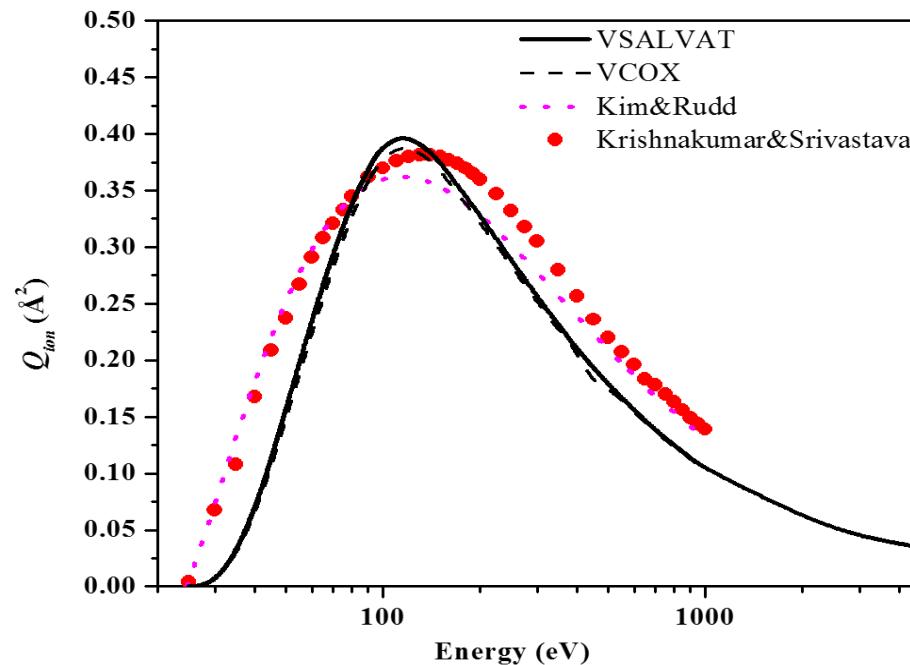
$$\begin{aligned} \text{IP (CCCBDB)} &= 13.93 \text{ eV} \\ \text{IP (BEB threshold)} &= 12.11 \text{ eV} \end{aligned}$$



**Deviation: ~14 %**



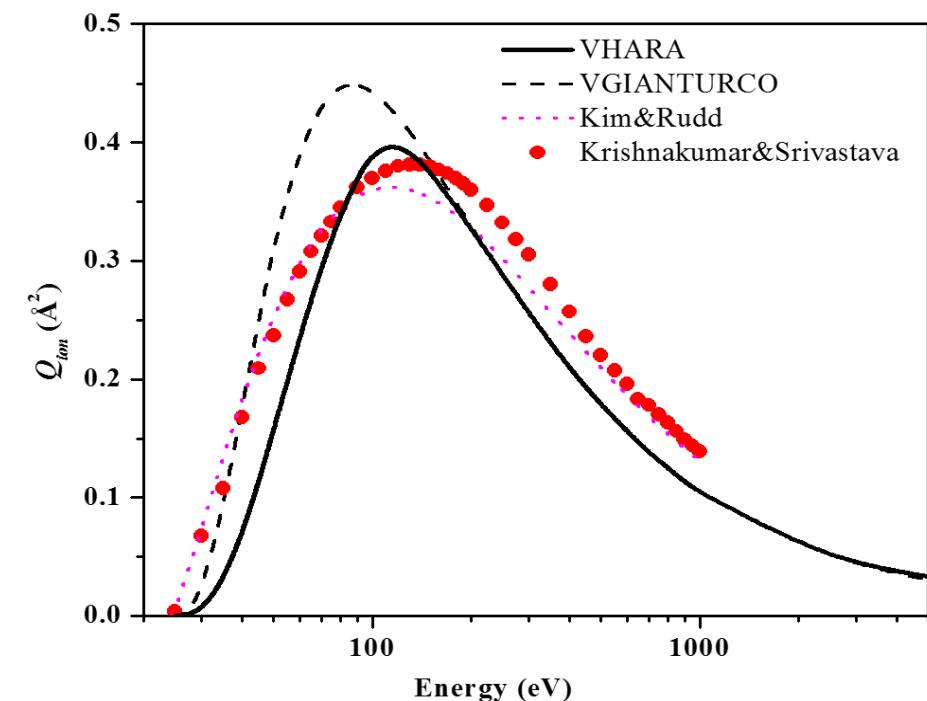
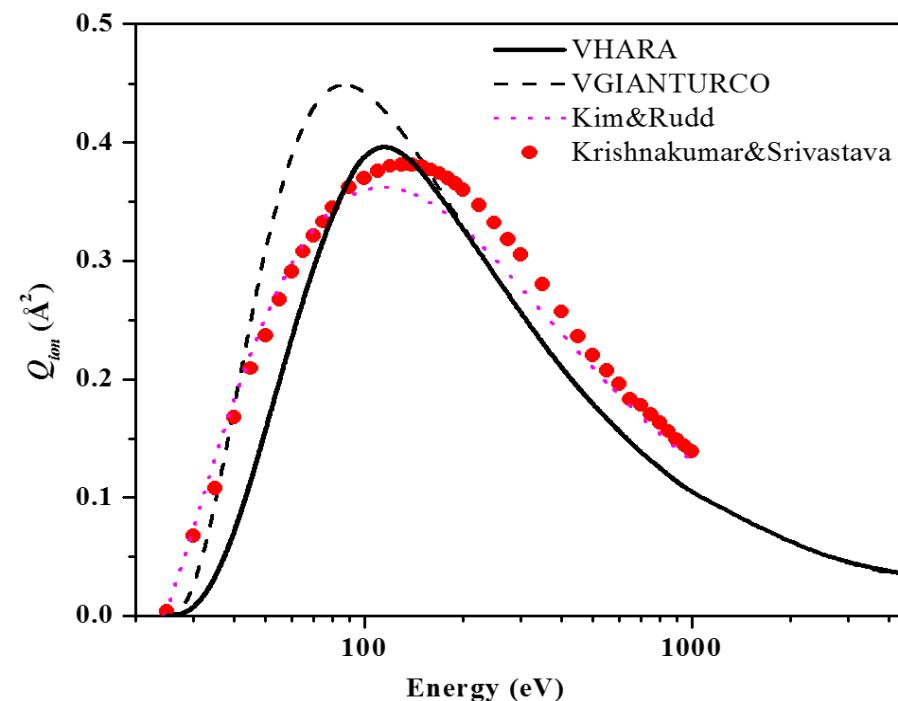
➤ Sensitivity to **Static Potential (V\_COX Vs V\_SALVAT)**



Deviation: ~2.29 %



➤ Sensitivity to **Exchange Potential**  
**(V\_HARA Vs V\_GIANTURCO)**

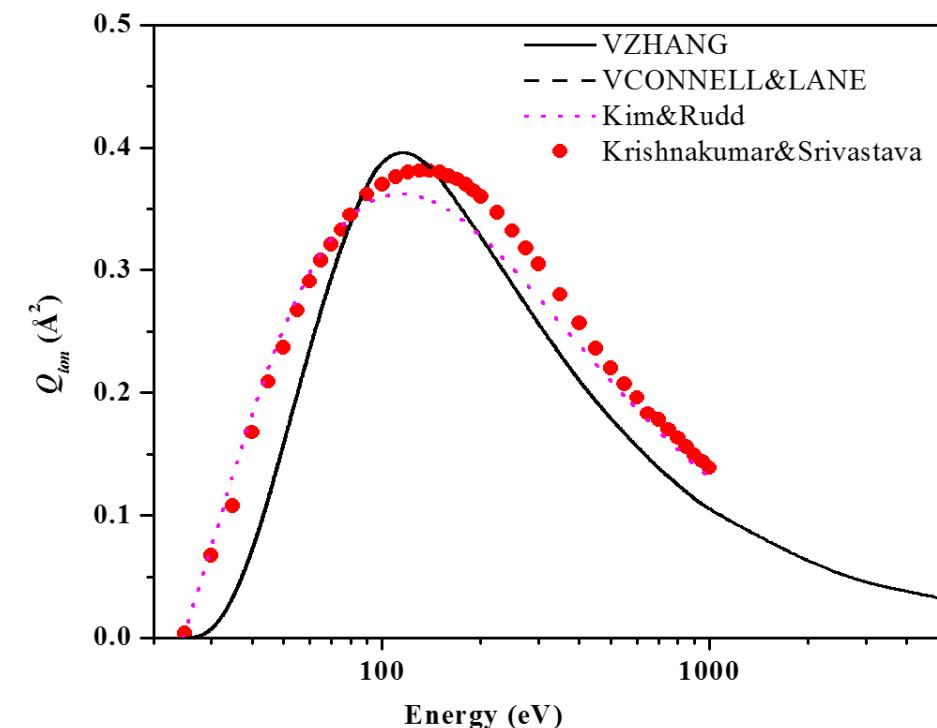
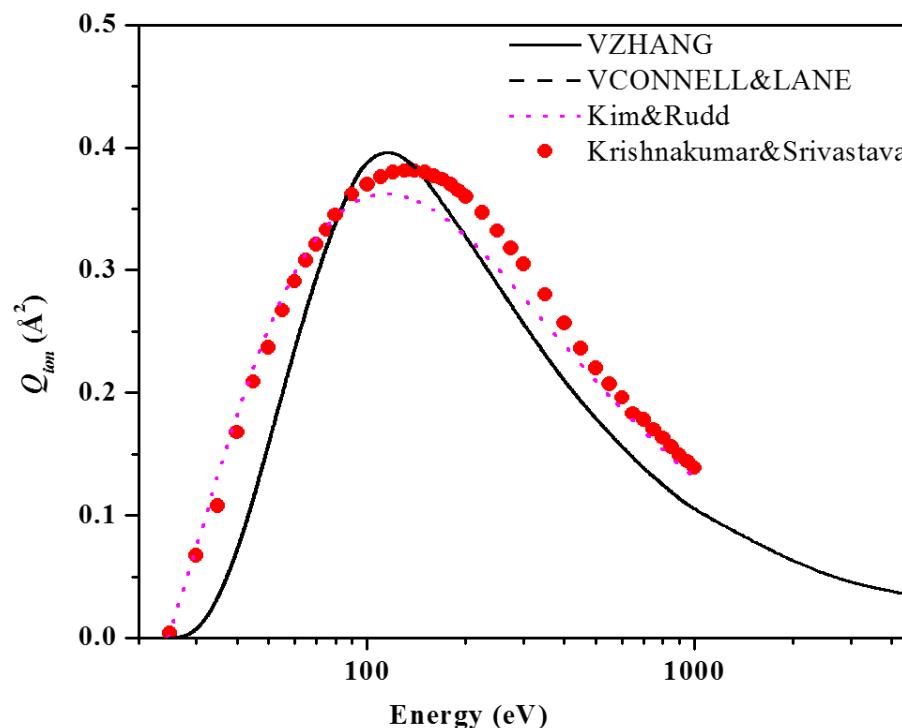


**Deviation: ~13.2 %**



## Sensitivity to **Polarization Potential**

(V\_ZHANG Vs V\_CONNELL&LANE)

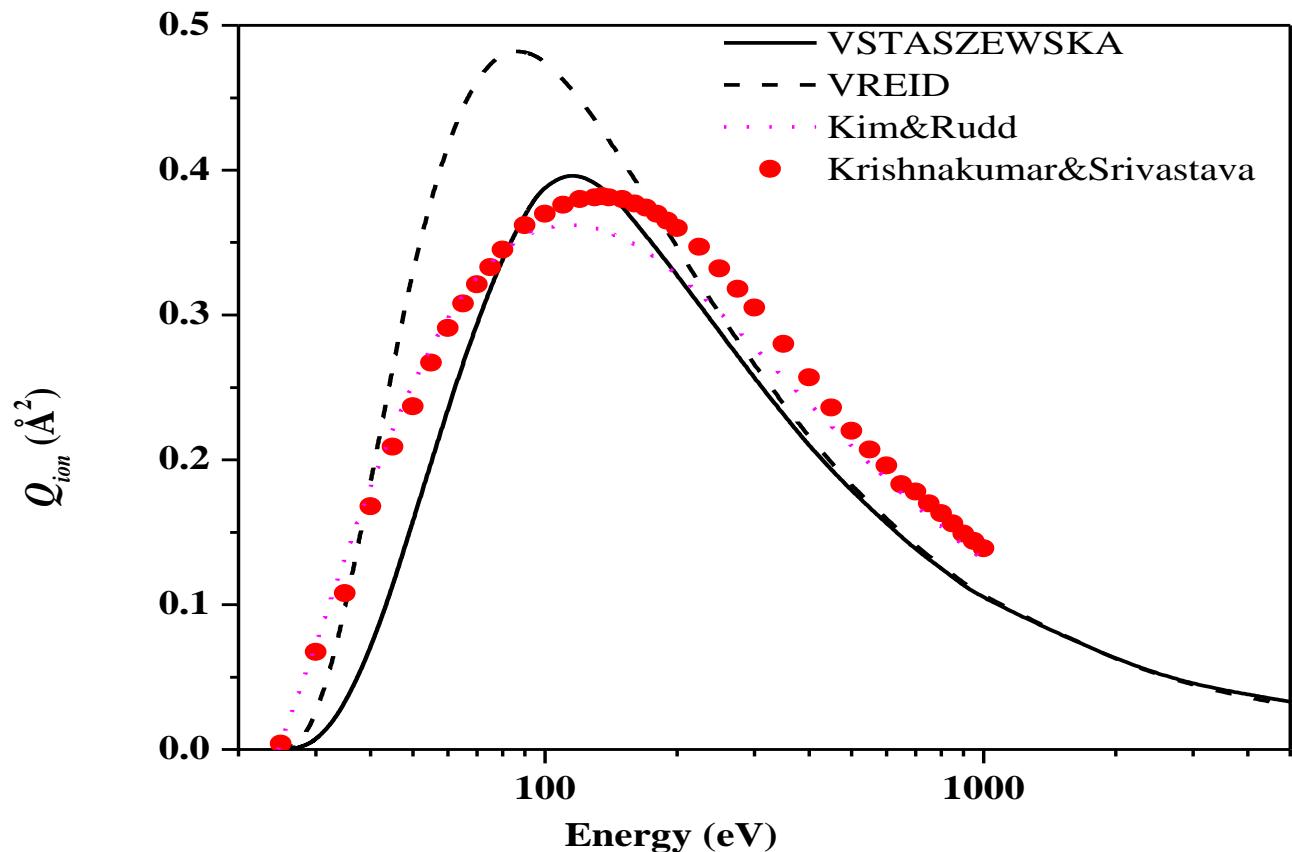


**Deviation: ~0 %**

# Uncertainty estimation Nuclear fission

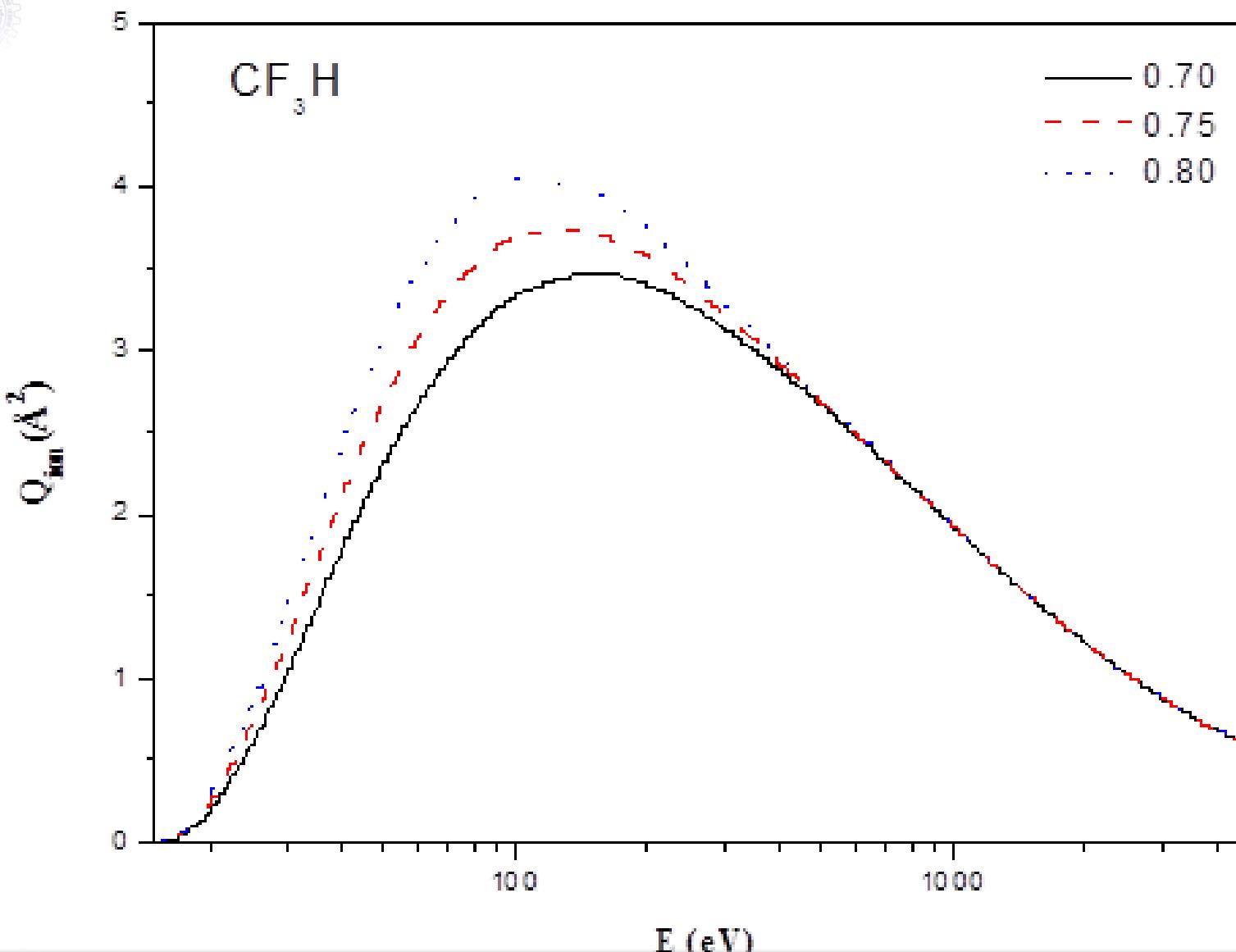
## ➤ Sensitivity to *Absorption Potential*

### (V\_STASZEWSKA Vs V\_REID)



**Deviation: ~21.6 %**

# Uncertainty: Sensitivity to input parameters





# Outline

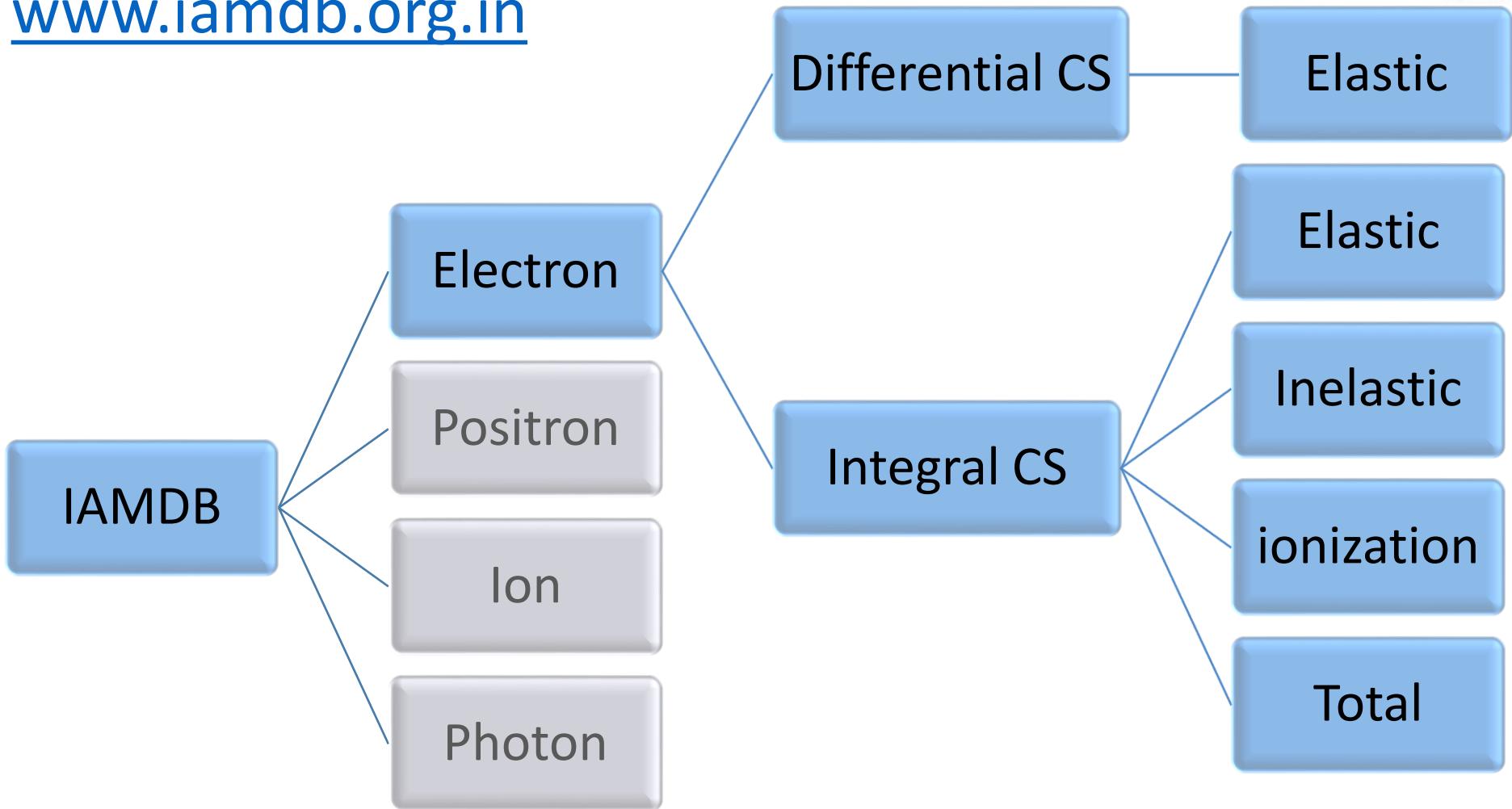
- Need for cross section data
- Theoretical methodology & Sample Results
  - ❖ Electron Scattering
  - ❖ Positron Scattering
- Uncertainty estimation
  - ❖ Benchmarking Data
  - ❖ Consistency check
  - ❖ Convergence check
  - ❖ Sensitivity to input parameters
  - ❖ Further plan
- IAMDB



- ❖ Estimate uncertainties associated with cross section data.
- ❖ Develop a standard methodology???

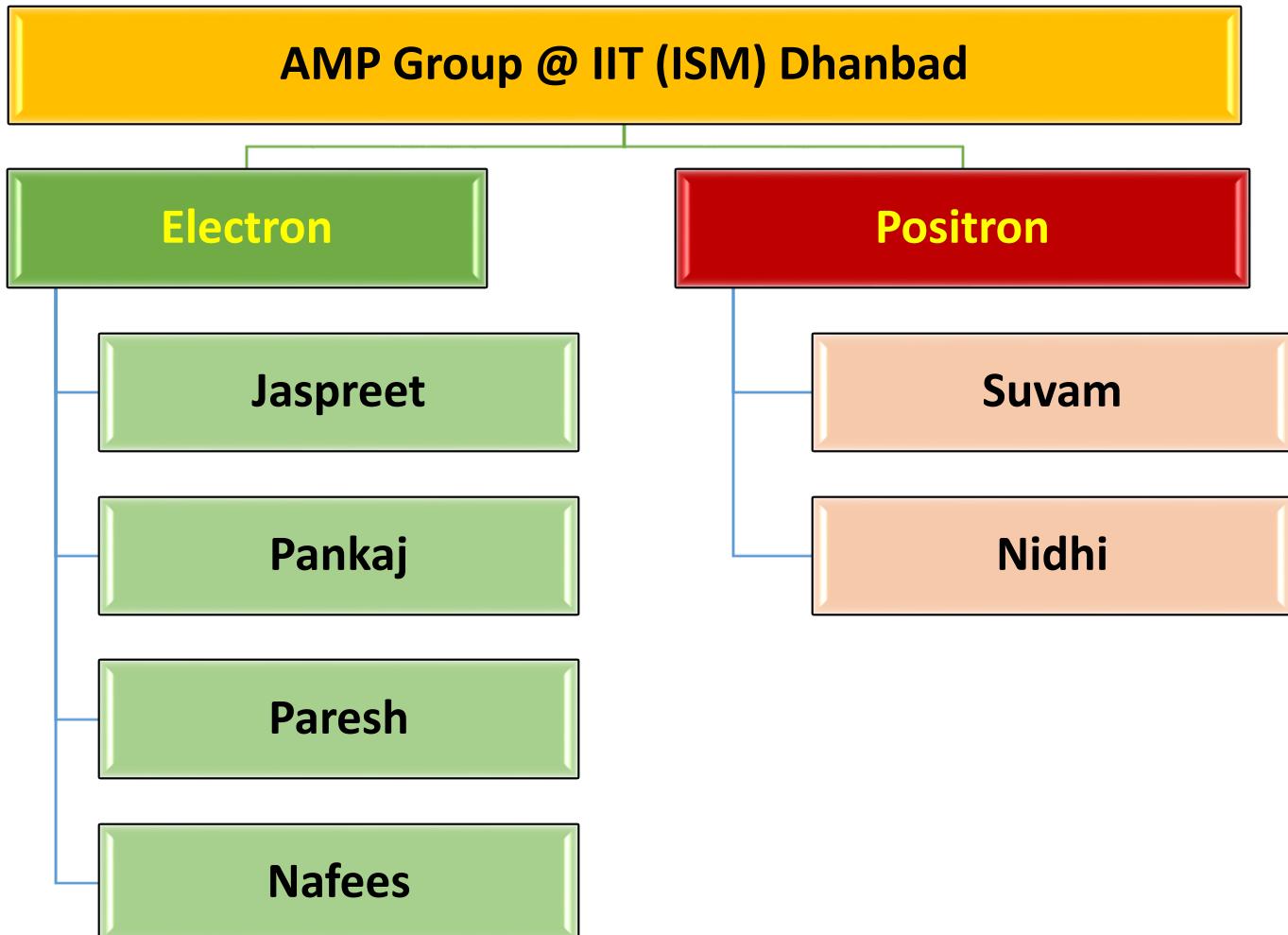
- Need for cross section data
- Theoretical methodology & Sample Results
  - ❖ Electron Scattering
  - ❖ Positron Scattering
- Uncertainty estimation
  - ❖ Benchmarking Data
  - ❖ Consistency check
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- IAMDB

[www.iamdb.org.in](http://www.iamdb.org.in)





# Acknowledgement





Thank you