

# The Few-Body Problem in Simple Atomic Systems



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# Relevance of few-body problem to controlled fusion?

**Controlled fusion:** Reliable rate coefficients for various processes in ion-atom collisions needed

**Experimental data:** tedious and costly to obtain, afflicted with experimental uncertainties

difficult to account for e.g. thermal energy distribution of ions and density effects in plasma

Alternative: **theoretical calculations**

Major challenge: Schrödinger equation not analytically solvable for more than 2 mutually interacting particles even when underlying forces are precisely known  $\Rightarrow$  **few-body problem**

**⇒ Theory has to resort to heavy numerical modelling efforts.**

**Assumptions entering in models have to be tested by detailed experimental data**

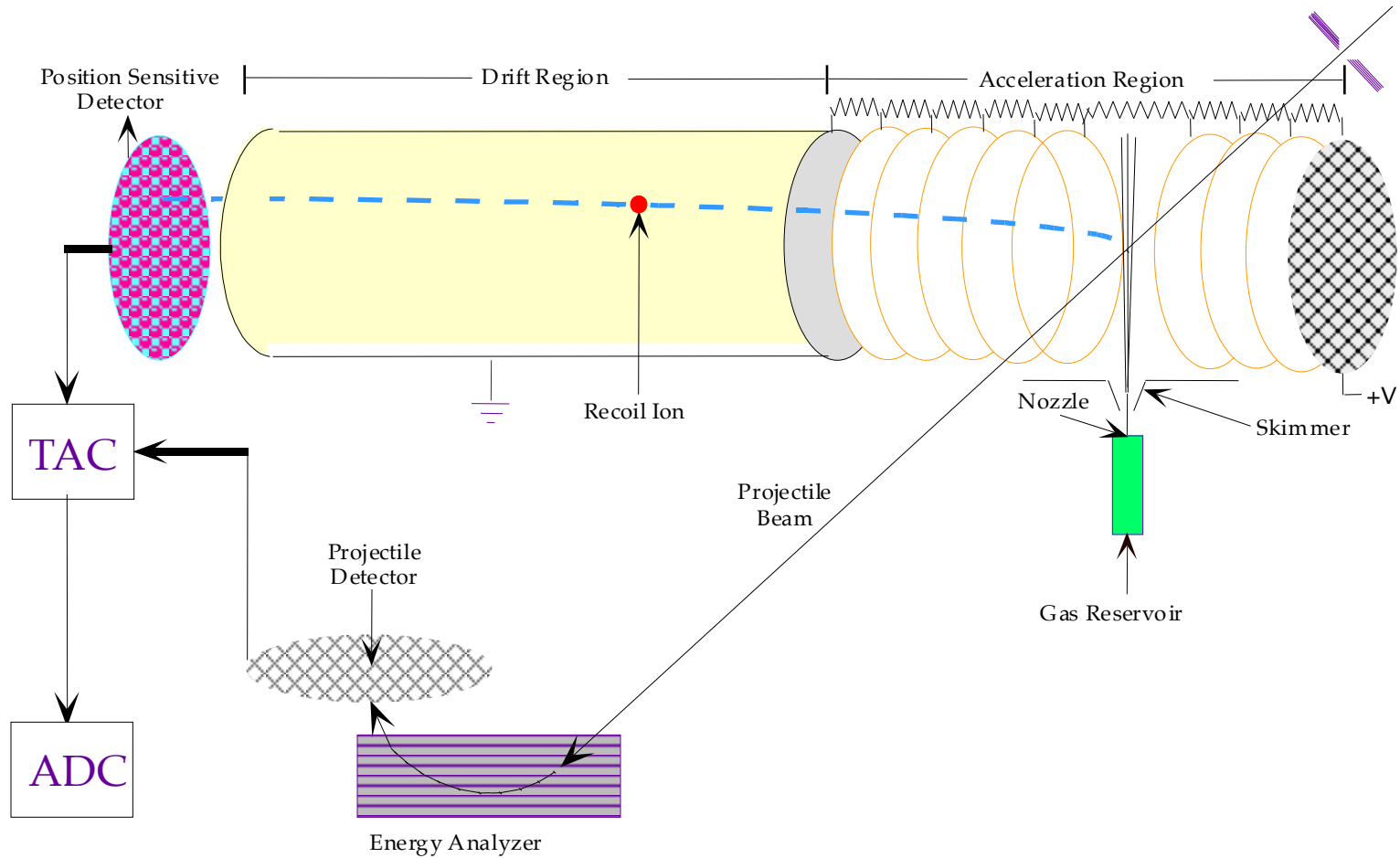
**Kinematically complete experiments** particularly important as they offer most sensitive test of theory

**Kinematically complete experiment on ionization**



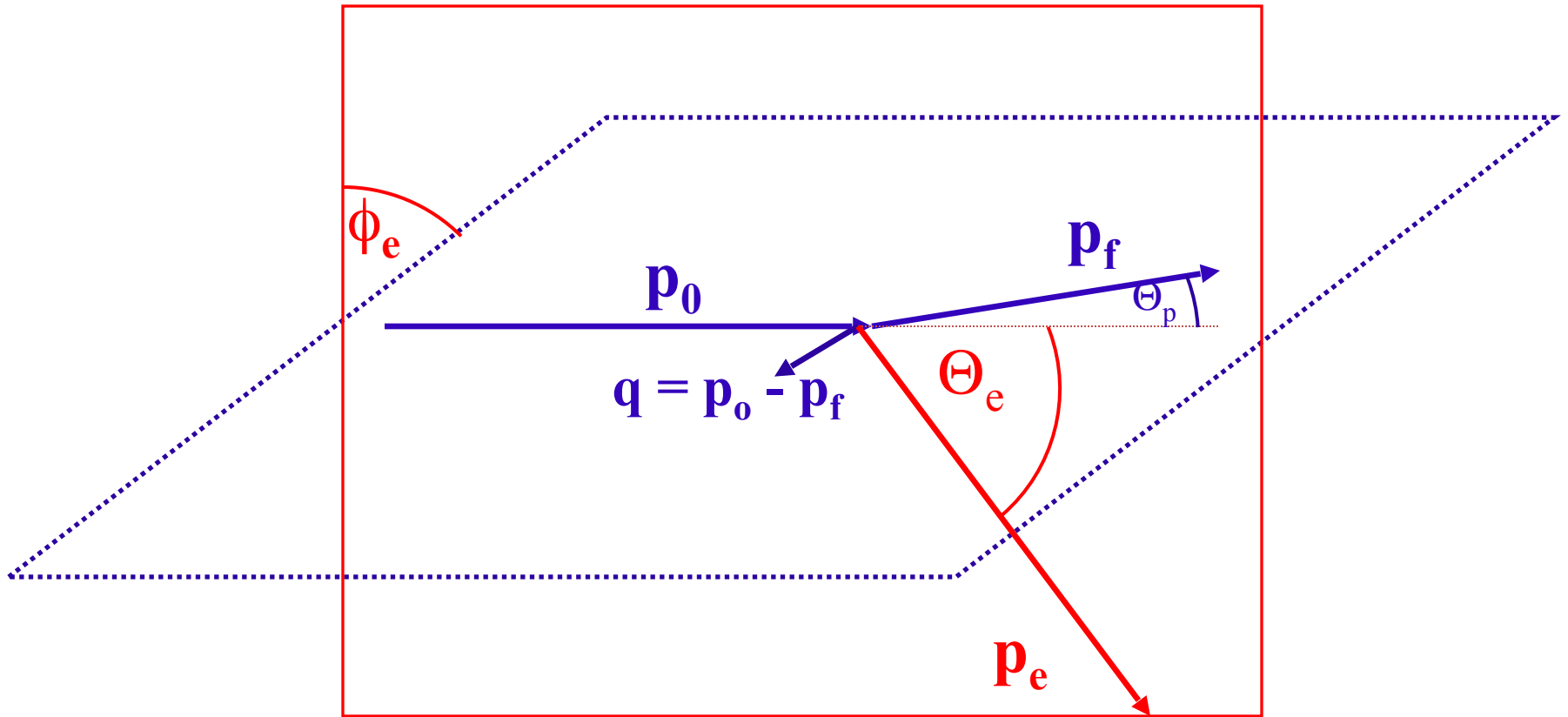
**Measure 2 momentum vectors, third determined by **momentum conservation****

# Experimental Setup, 75 keV p + H<sub>2</sub>, He



Complete projectile and recoil-ion momenta measured. Electron momentum from conservation laws  $\Rightarrow$  **kinematically complete**  $\Rightarrow$  **FDCS**

# Three-Dimensional Fully Differential Single Ionization Data

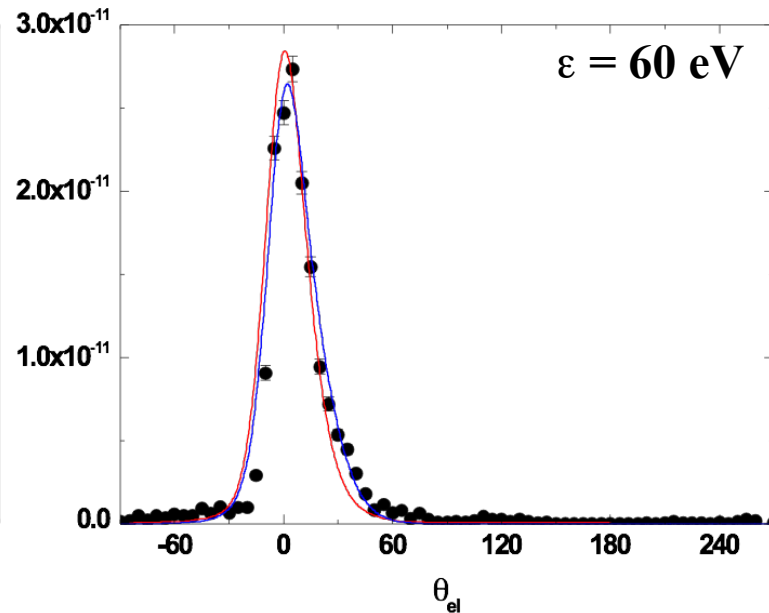
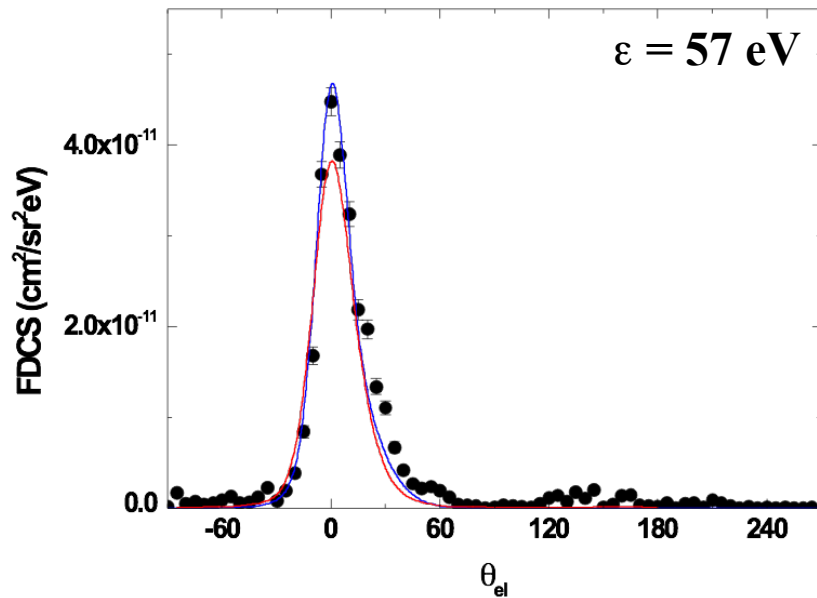
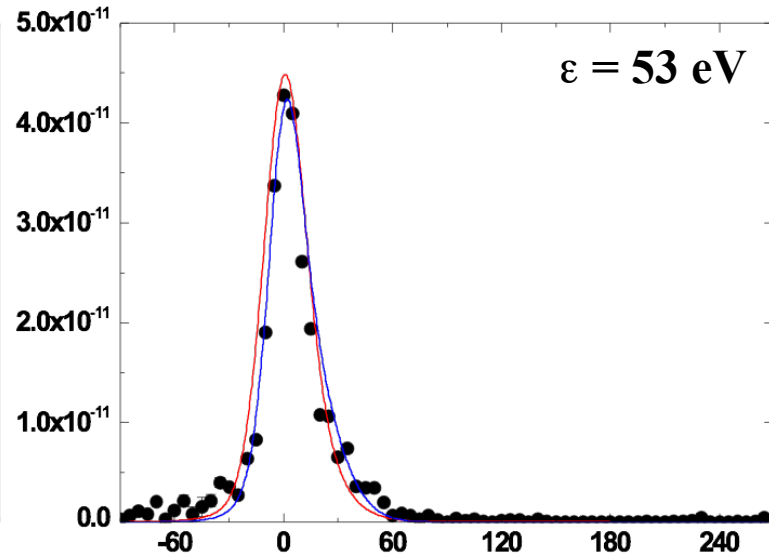
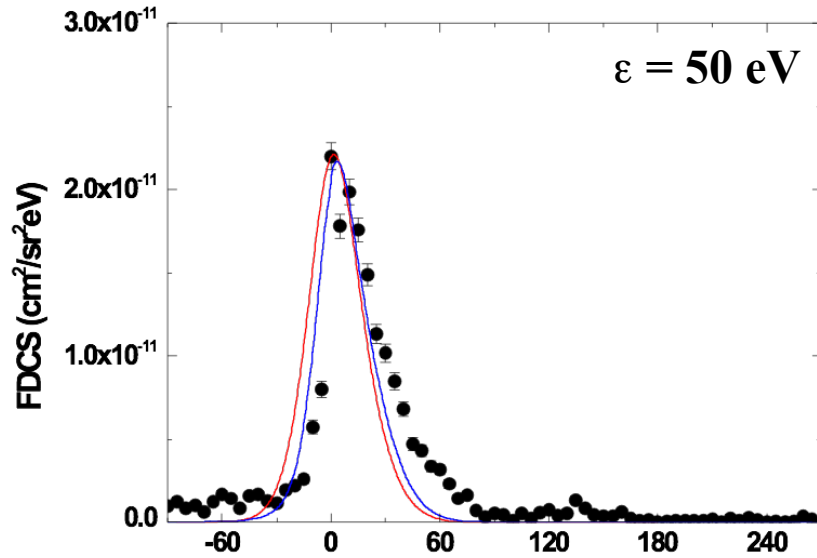


**Blue:** Scattering plane defined  
by  $p_0$  and  $p_f$

**Red:** electron emission plane  
defined by  $p_0$  and  $p_e$

Quantities fixed:  $\phi_p$ ,  $q$ , and  $E_e$ , spectra plotted as a fct. of  $\phi_e$  and  $\theta_e$

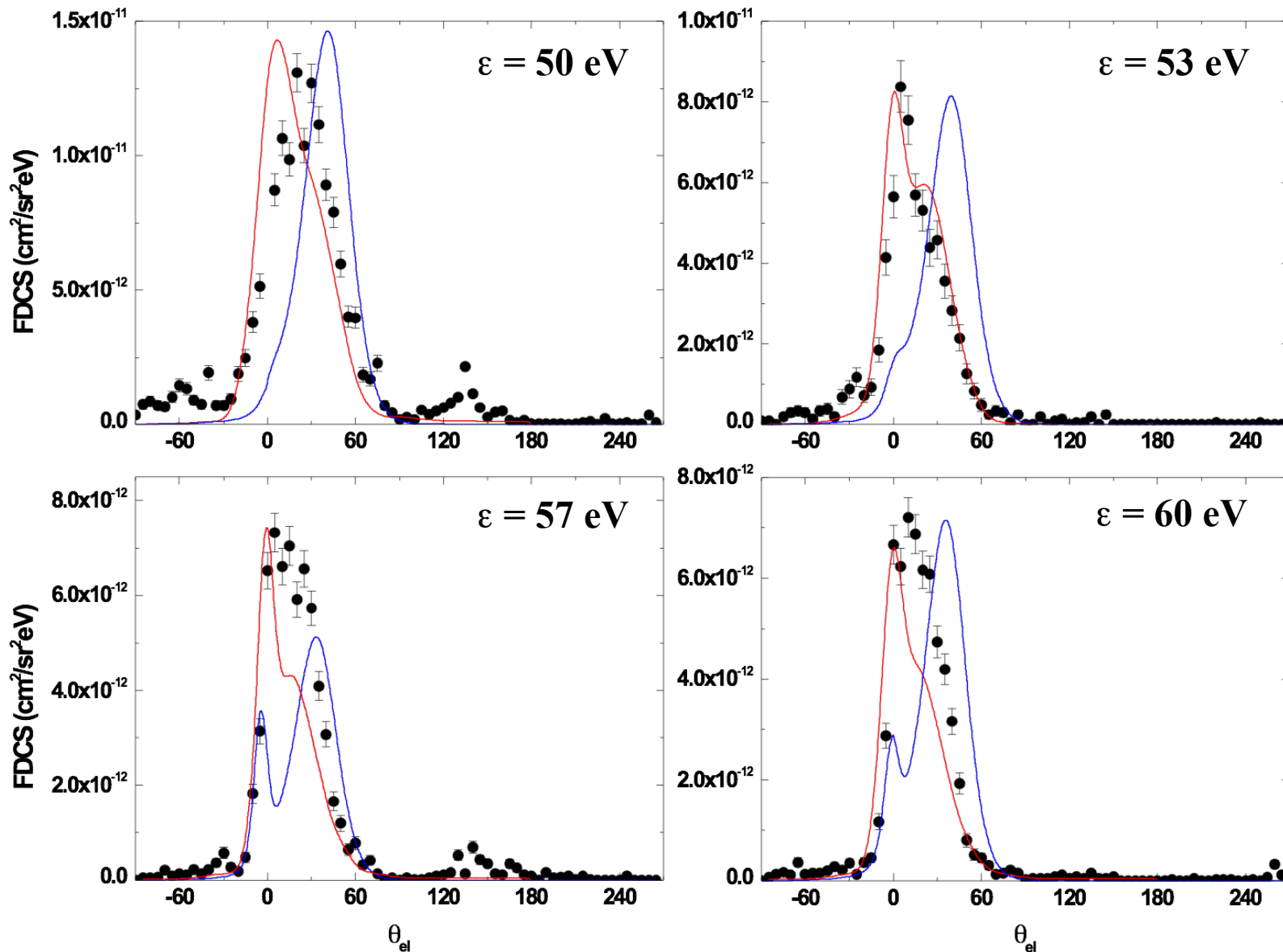
# Electrons ejected into scattering plane, $\theta_p = 0.1$ mrad



**Red lines: 3DW model**

**blue lines: CDW-EIS model**

# Electrons ejected into scattering plane, $\theta_p = 0.325$ mrad



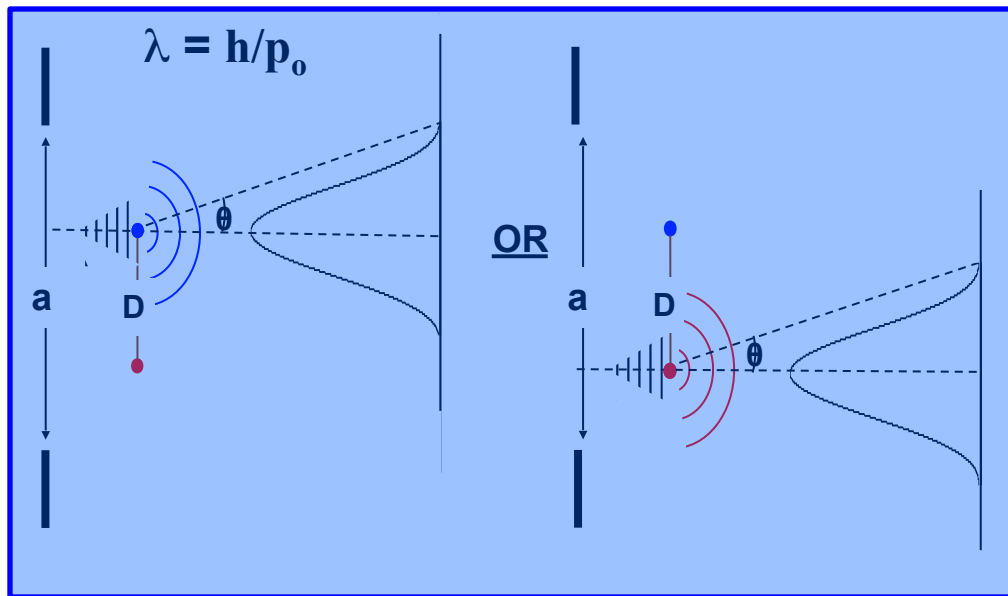
$\Rightarrow$  Ball is in the theorists court now

Interference in atomic scattering well established. E.g.: two-center interference in projectile diffraction from diatomic molecules

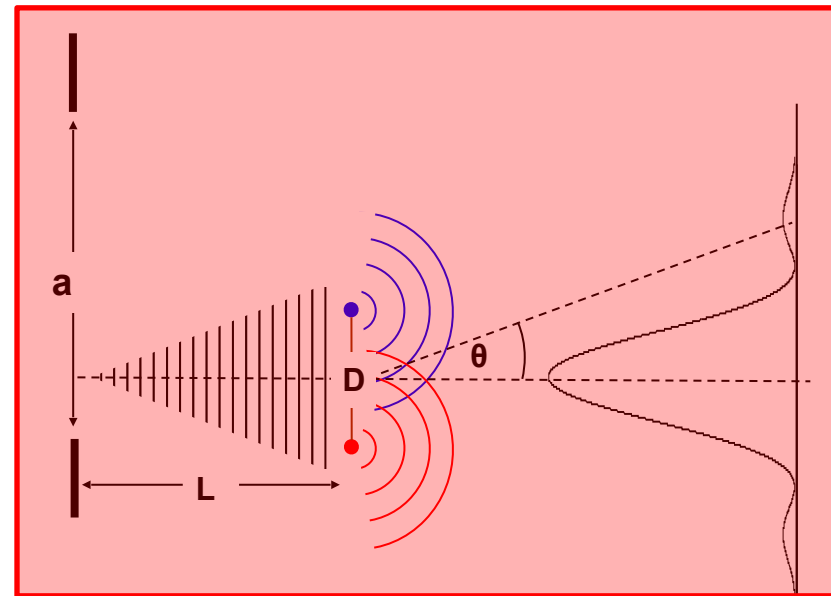
**BUT:** **transverse coherence length  $\Delta x$**  must be large enough to coherently illuminate both centers simultaneously:  **$\Delta x > D$**

$\Delta x$  given by geometry of collimating slit and DeBroglie wavelength:

$$\Delta x = 1/2 \lambda L/a$$



Small  $L \Rightarrow \Delta x < D \Rightarrow$  no interference



Large  $L \Rightarrow \Delta x > D \Rightarrow$  interference

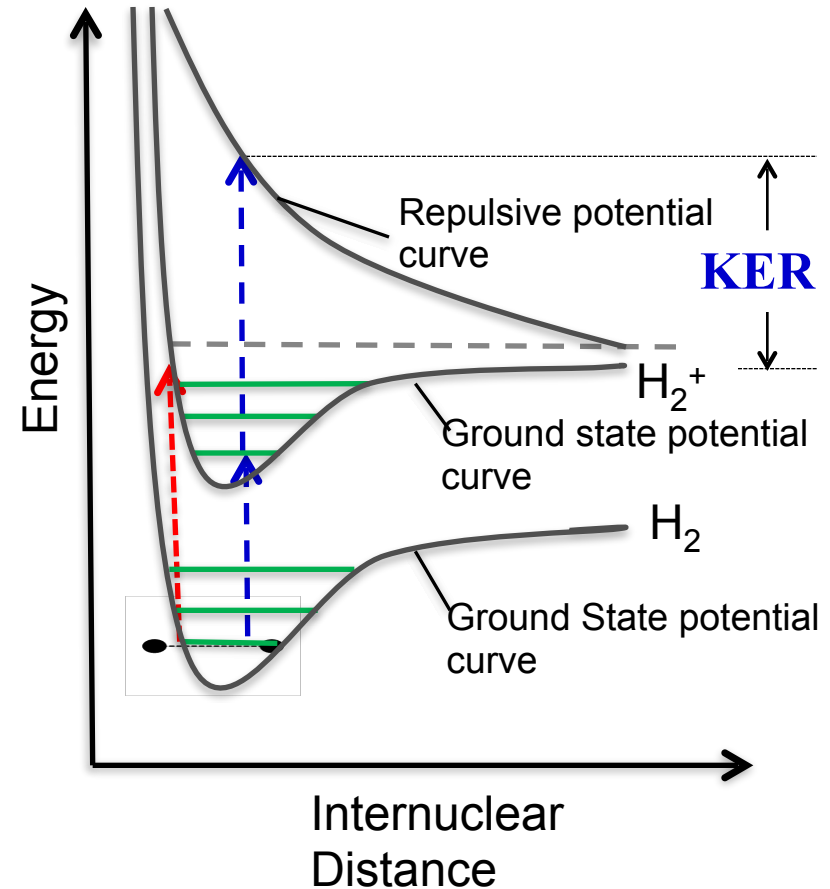
**Completely overlooked by theory for decades!**



# Dissociation of Hydrogen molecule



- **Electronic transition to a repulsive state**
- **large KER**
  
- **Vibrational excitation of the nuclear motion**
- **small KER**

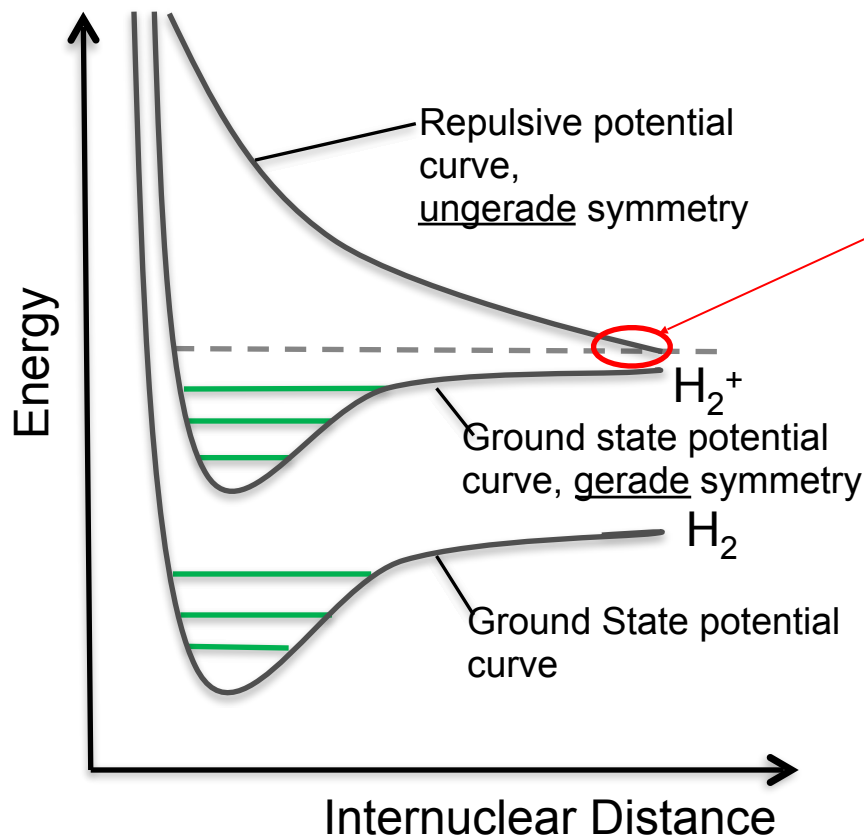


$d\sigma_{\text{coh}} = d\sigma_{\text{inc}} I \Rightarrow$  ratio  $R = d\sigma_{\text{coh}}/d\sigma_{\text{inc}}$  is interference term  $I$

$$I = 1 + \alpha \cos(p_o \sin\theta_p D + \pi)$$

**what leads to this  $\pi$ -phase shift?**

# Shaofeng Zhang (IMP Lanzhou):



**curve crossing**  
transition to ungerade state?

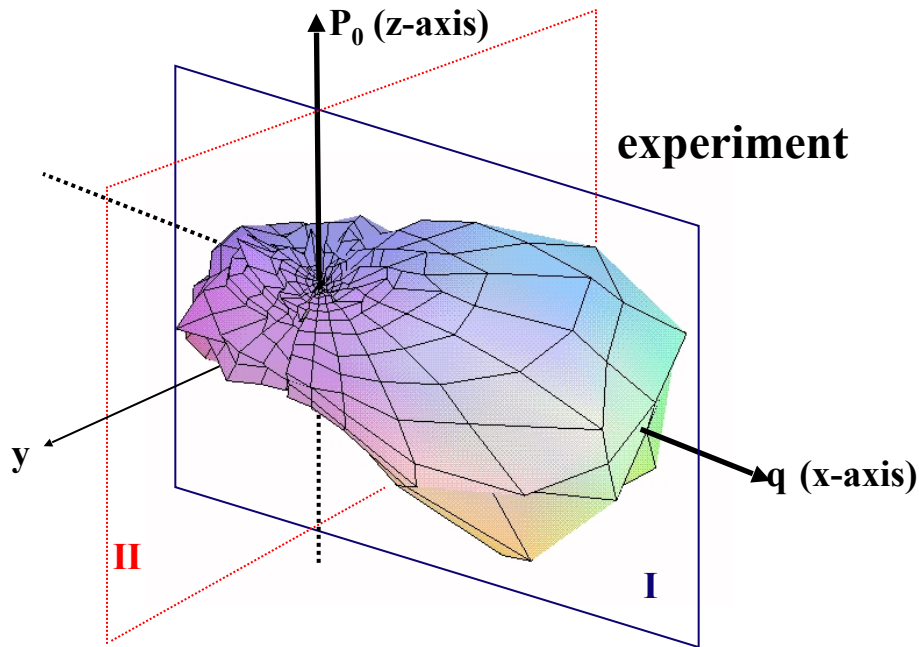
**parity conservation:**  
projectile needs to compensate for symmetry switch in electronic wavefunction  
 **$\pi$  phase shift**

- Problems:** a) coupling probability needs to be close to 1! Realistic?  
b) when fragments reach coupling region projectile is long gone!  
how does it “know” about switch in symmetry?  
**entanglement?**

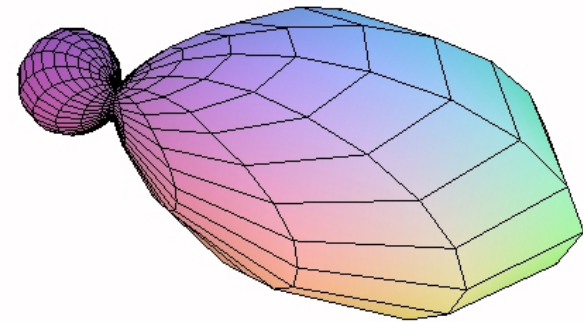
# Collaborations

**I. IMP Lanzhou, Xinwen Ma, Shaofeng Zhang, ...  
various projects**

**a) very fast collisions: discrepancies observed earlier**



**1.2 GeV  $C^{6+} + He$**



**3DW, quantum-mechanical NN**

**Due to unrealistic projectile coherence properties in theory?**

**Need to repeat experiment. Facilities available at IMP**

- b) Fully differential cross sections for highly charged ions (e.g.  $\text{Ne}^{10+}$ ) at very small projectile energies ( $\approx 10$  to  $20$  keV)  
very **non-perturbative regime** ( $\eta = Q_p/v_p \approx 30$  to  $50$ )  
important regime for plasmas  
**no fully differential data available!**

## II. Theory

- a) Don Madison at S&T, pioneer on 3DW model  
b) Marcelo Ciappina, Czech Republic, CDW-EIS model  
c) Raul Barrachina, Argentina, and  
Ladislau Nagy, Romania, projectile coherence effects

## III. Desired future collaborations:

Theory groups using **non-perturbative and time-dependent** models to describe slow HCI collisions and coherence effects

**funding??**



**Funding situation in US:**

**two agencies fund collision physics: NSF and DOE  
both under increasing financial pressure  
policy seems to be (at least at NSF) to reduce funding level  
before reducing number of funded projects**

**⇒ All AMO research activities at S&T currently still funded,  
but budget puts us in increasingly difficult situation.**