

# Introduction to FLYCHK

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Joint ICTP-IAEA School on Atomic and Molecular Spectroscopy in Plasmas  
Trieste, Italy

# **FLYCHK COLLISIONAL-RADIATIVE MODEL**

# Population Kinetics Modeling

Rate equations are solved for level population distributions for given plasma conditions

$$\frac{dn_i}{dt} = -n_i \sum_{j \neq i}^{N_{\max}} W_{ij} + \sum_{j \neq i}^{N_{\max}} n_j W_{ji}$$

$$W_{ij} = B_{ij} \overline{J_{ij}} + n_e C_{ij} + \beta_{ij} + n_e \gamma_{ij}$$

$$W_{ji} = A_{ij} + B_{ji} \overline{J_{ji}} + n_e D_{ji} + n_e (\alpha_{ji}^{RR} + \alpha_{ji}^{DR}) + n_e^2 \delta_{ij}$$

$B_{ij}$  Stimulated absorption

$A_{ij}$  Spontaneous emission

$C_{ij}$  Collisional excitation

$B_{ij}$  Stimulated emission

$\gamma_{ij}$  Collisional ionization

$D_{ij}$  Collisional deexcitation

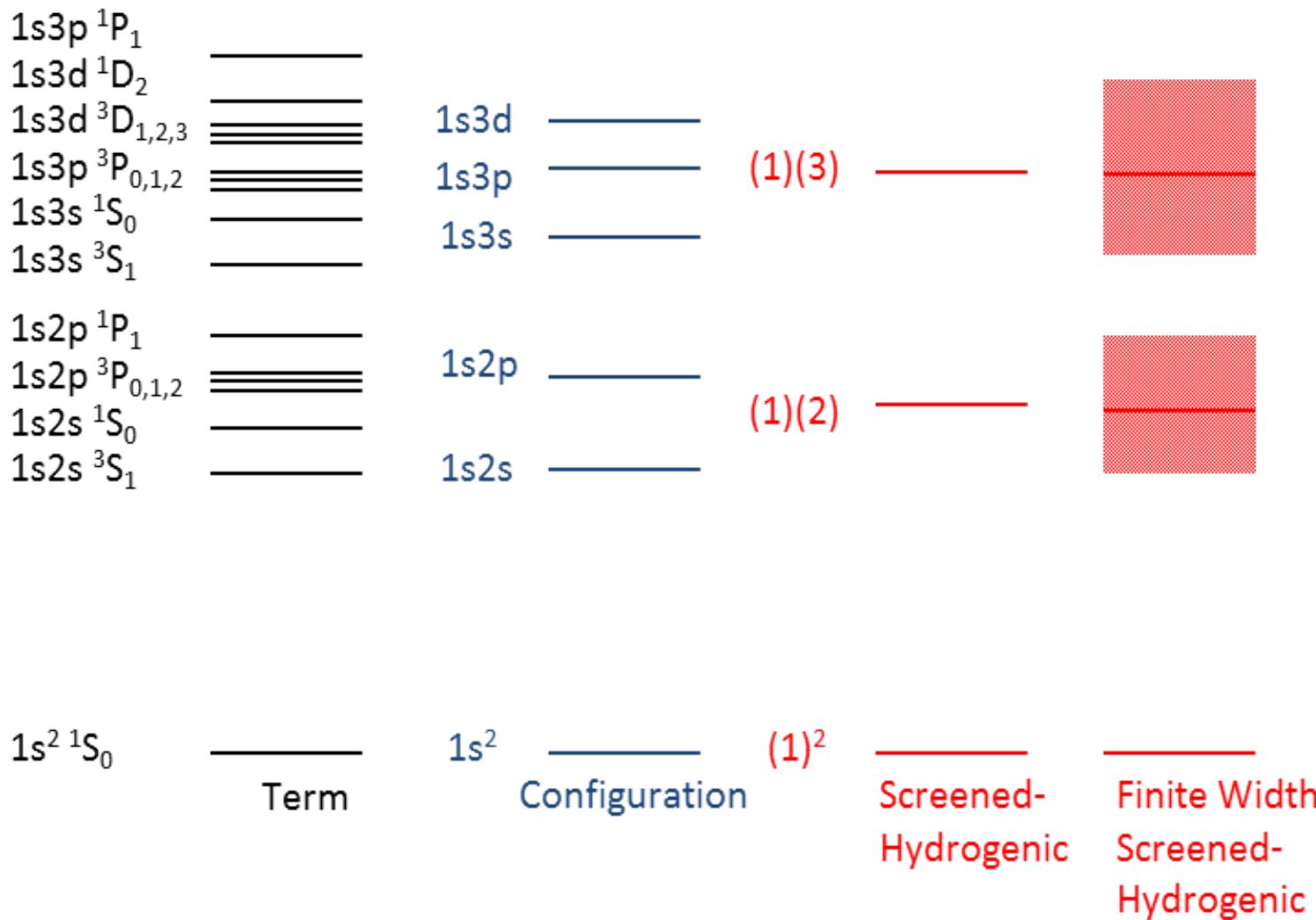
$\beta_{ij}$  Photoionization (+st. recom)

$a_{ij}^{DR}$  Dielectronic recombination

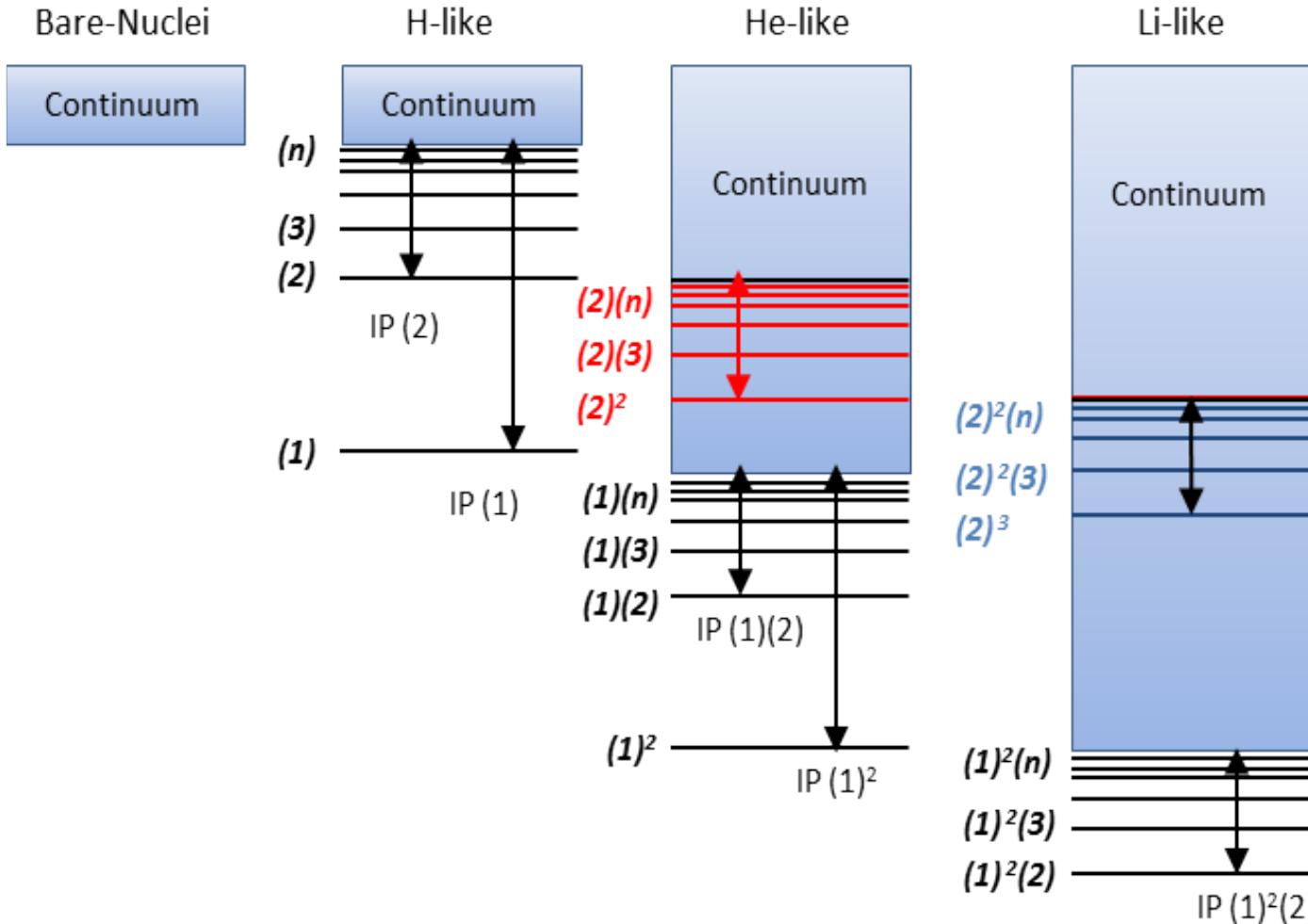
$a_{ij}^{RR}$  Radiative recombination

$\delta_{ij}$  Collisional recombination

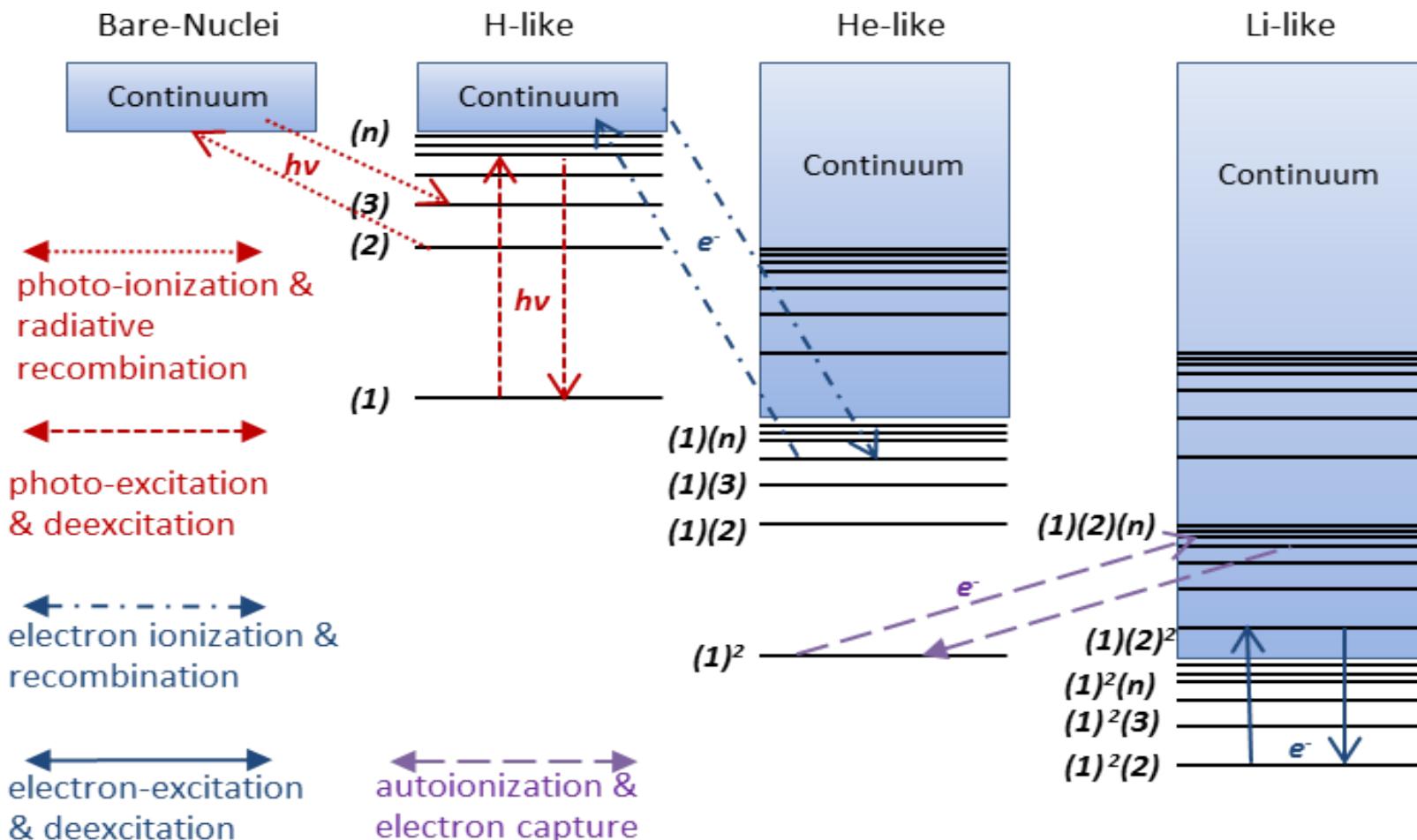
# FLYCHK uses screened hydrogenic levels (super configurations)



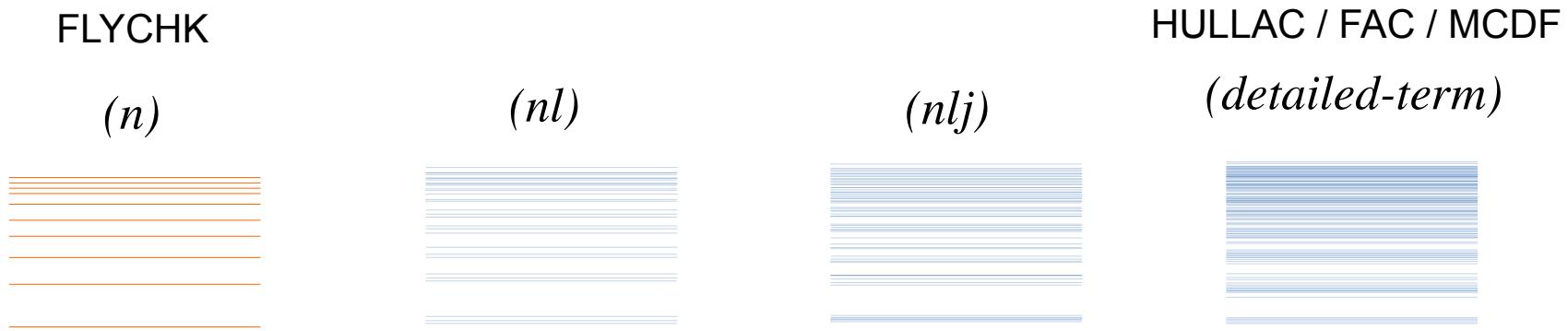
# Level energy obtained with ionization potential from its 1<sup>st</sup> continuum level



# Atomic processes included in FLYCHK



# FLYCHK Model : *simple, but complete*



- Screened hydrogenic energy levels with relativistic corrections
- Relativistic Hartree-Slater oscillator strengths (M. Chen) and photoionization cross-sections (J. Scofield, + Kramer)
- Fitted collisional cross-section to PWB approximation (M. Chen)
- Semi-empirical cross-sections for collisional ionization (A. Burgess)
- Detailed counting of autoionization and electron capture (M. Chen)
- Continuum lowering (Stewart-Pyatt, Ecker-Kroll)

# Application to a wide range of Z & experiments:

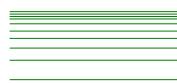
*Excitation autoionization (EA) / Dielectronic recombination (DR) processes  
are modeled with extensive inner-shell (IS) states*

Low Z atom

Promotion of **IS** electrons leads to states far from continuum limit and *rarely matters in CSD* (charge state distribution)

$1s^1 2l^{Z+1} nl''$

Inner-Shell



$1s^2 2l^{Z-1} 3l' nl''$

Doubly-excited



Bound



L-shell Ion  
 $1s^2 2l^Z$

L-shell Ion  
 $1s^2 2l^{Z+1}$

High Z atom

Promotion of **IS** electrons can lead to states near the continuum limit and hence EA/DR process is *critical in CSD*

$3l^{17} 4l^z nl$

$3l^{16} 4l^{z+1} nln'l'$



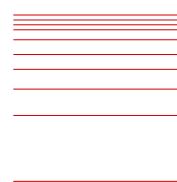
Doubly-excited

Bound

N-shell Ion  
 $3l^{18} 4l^{z+1}$

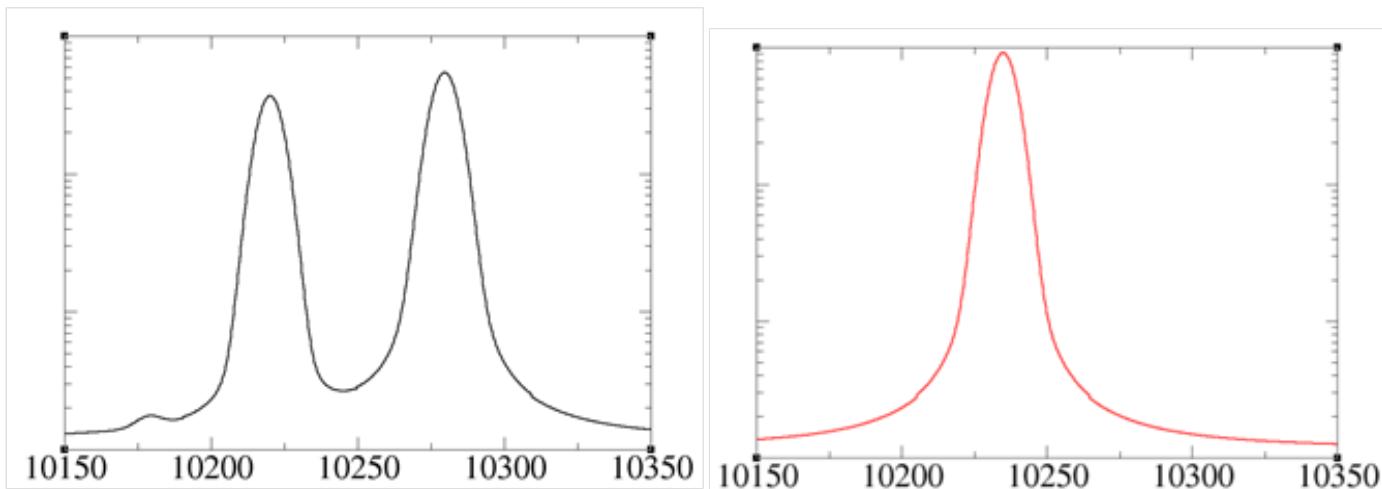
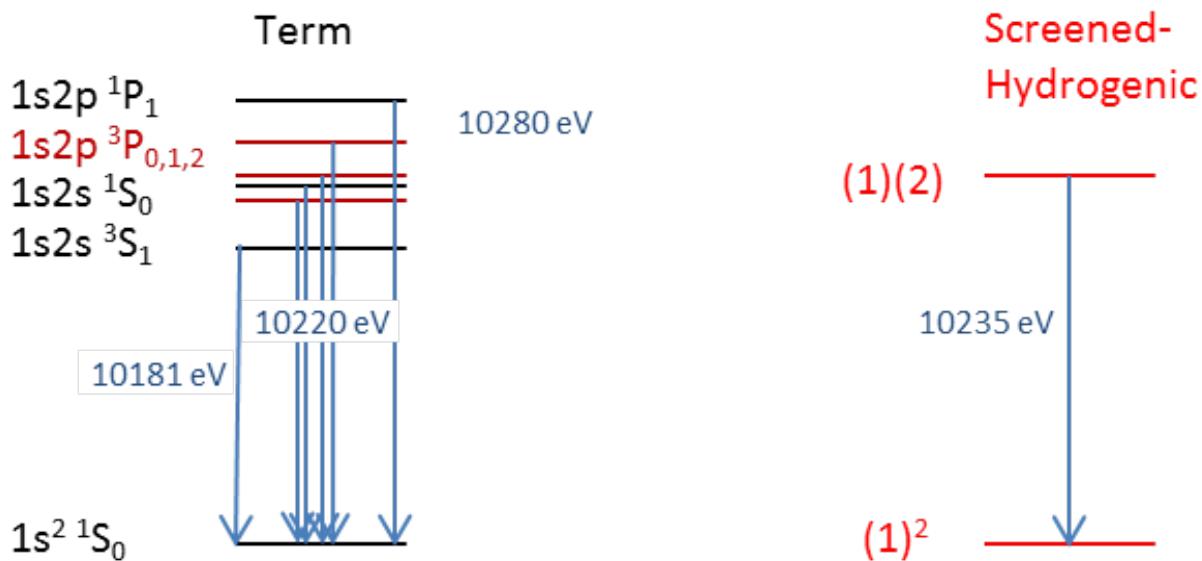
N-shell Ion

N-shell Ion  
 $3l^{18} 4l^z$



# **FLYSPEC SPECTROSCOPIC MODULE**

# FLYSPEC uses detailed (H, He, Li-like) and Super Transition Array for spectra



# Data Types for Spectroscopic Model

Z < 27 H, He and Li	FLY model
Z > 27 H, He and Li	HULLAC data (term levels up to n=4)
Be-like and lower charge states	Super Transition Array (STA) made with Configurations (jj) 1s, 2s, 2p <sup>-</sup> , 2p <sup>+</sup> , 3s, 3p <sup>-</sup> , 3p <sup>+</sup> , 3d <sup>-</sup> , 3d <sup>+</sup> , Up to n=6

# Energy-dependent spectral intensity in the STA formalism

Spectra for specific E/ ranges: STA formalism

Spectra using configuration-average atomic data generated by the DHS (Dirac-Hartree-Slater) code (M.Chen)

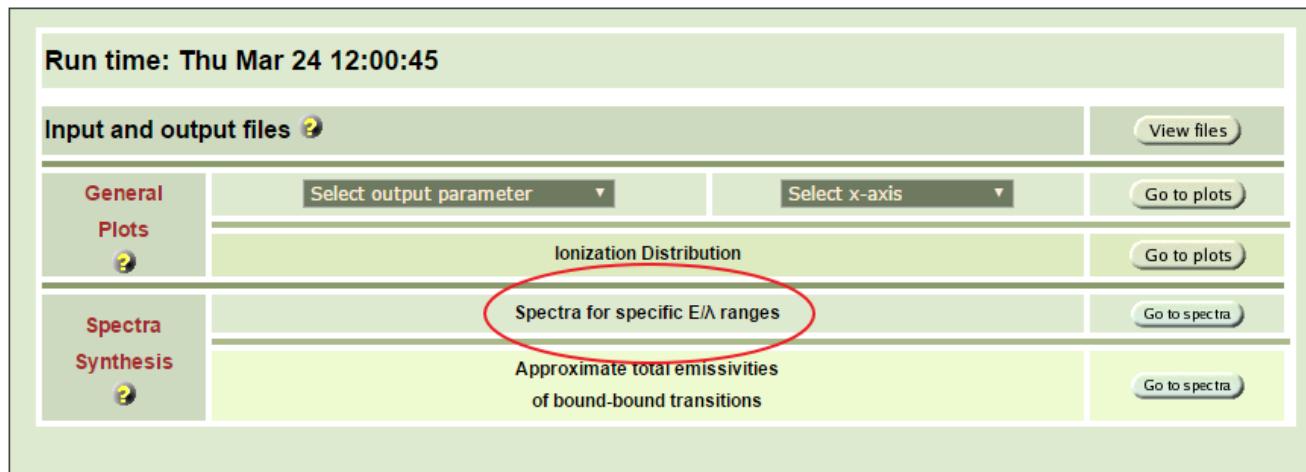
$$\eta(v) = n_A A_{AB} E_{AB} \phi(v) = \frac{n_A \sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e) A_{ij} E_{ij} \phi(v)}{\sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e)}$$

[ergs/s/Hz/cm<sup>3</sup>/ster]

$$A_{AB} = \frac{\sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e) A_{ij}}{\sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e)}$$

$$E_{AB} = \frac{\sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e) A_{ij} E_{ij}}{\sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e) A_{ij}}$$

$$\mu_{AB}^2 = \left[ \frac{\sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e) A_{ij} E_{ij}^2}{\sum_{i \in A: j \in B} g_i \exp(-E_i / kT_e) A_{ij}} \right]^2 - E_{AB}^2$$

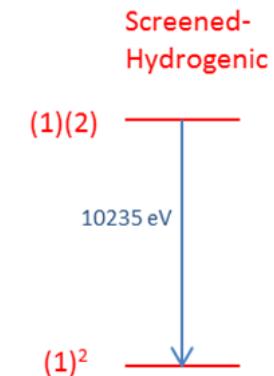


# Total line emissivity in the STA formalism

## Approximate total line emissivity:

A plot shows approximate line emission spectra and provides information on energy range of dominant emission

$$S = n_u A_{ul} E_{ul} / N_e$$



Run time: Thu Mar 24 12:00:45

**Input and output files**

**General** **Plots**

Select output parameter ▾ Select x-axis ▾ Go to plots

Ionization Distribution Go to plots

**Spectra** **Synthesis**

Spectra for specific E/λ ranges Go to spectra

Approximate total emissivities of bound-bound transitions Go to spectra

# **FLYCHK APPLICATIONS**

# FLYCHK Help Pages

- [http://nlte.nist.gov/FLY/Doc/  
Manual\\_FLYCHK\\_Nov08.pdf](http://nlte.nist.gov/FLY/Doc/Manual_FLYCHK_Nov08.pdf)
- <http://nlte.nist.gov/FLY/README.html>
- <http://nlte.nist.gov/FLY/EXAMPLE.html>
- Click on the Question Marks
  - <http://nlte.nist.gov/FLY/Help/runfile.html>
  - <http://nlte.nist.gov/FLY/Help-opacity.html>

.....

Available to the community at password-protected NIST website: <http://nlte.nist.gov/FLY>

**Advantages:** simplicity and versatility → applicability

- $\langle Z \rangle$  for fixed any densities: electron, ion or mass
- Mixture-supplied electrons (eg: Argon-doped hydrogen plasmas)
- External ionizing sources : a radiation field or an electron beam.
- Multiple electron temperatures or arbitrary electron energy distributions
- Optical depth effects

**Outputs:** population kinetics code and spectral synthesis

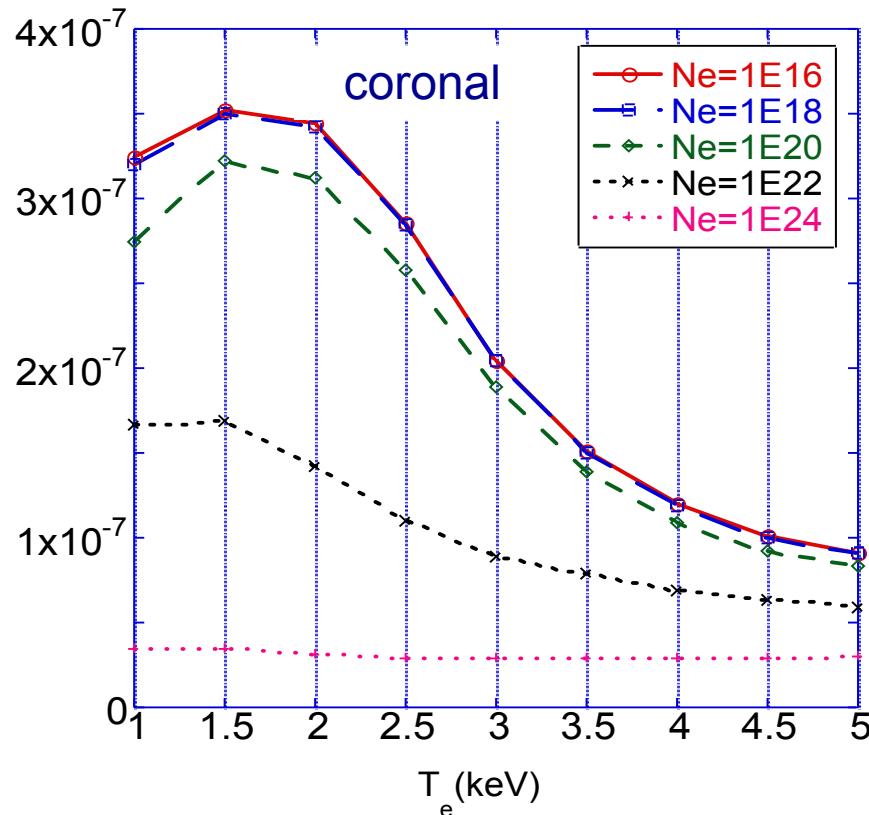
- $\langle Z \rangle$  and charge state distribution
- Radiative Power Loss rates under optically thin assumption
- Energy-dependent spectral intensity of uniform plasma with a size

**Caveats:** simple atomic structures and uniform plasma approximation

- Less accurate spectral intensities for non-K-shell lines
- Less accurate for low electron densities and for LTE plasmas
- When spatial gradients and the radiation transport affect population significantly

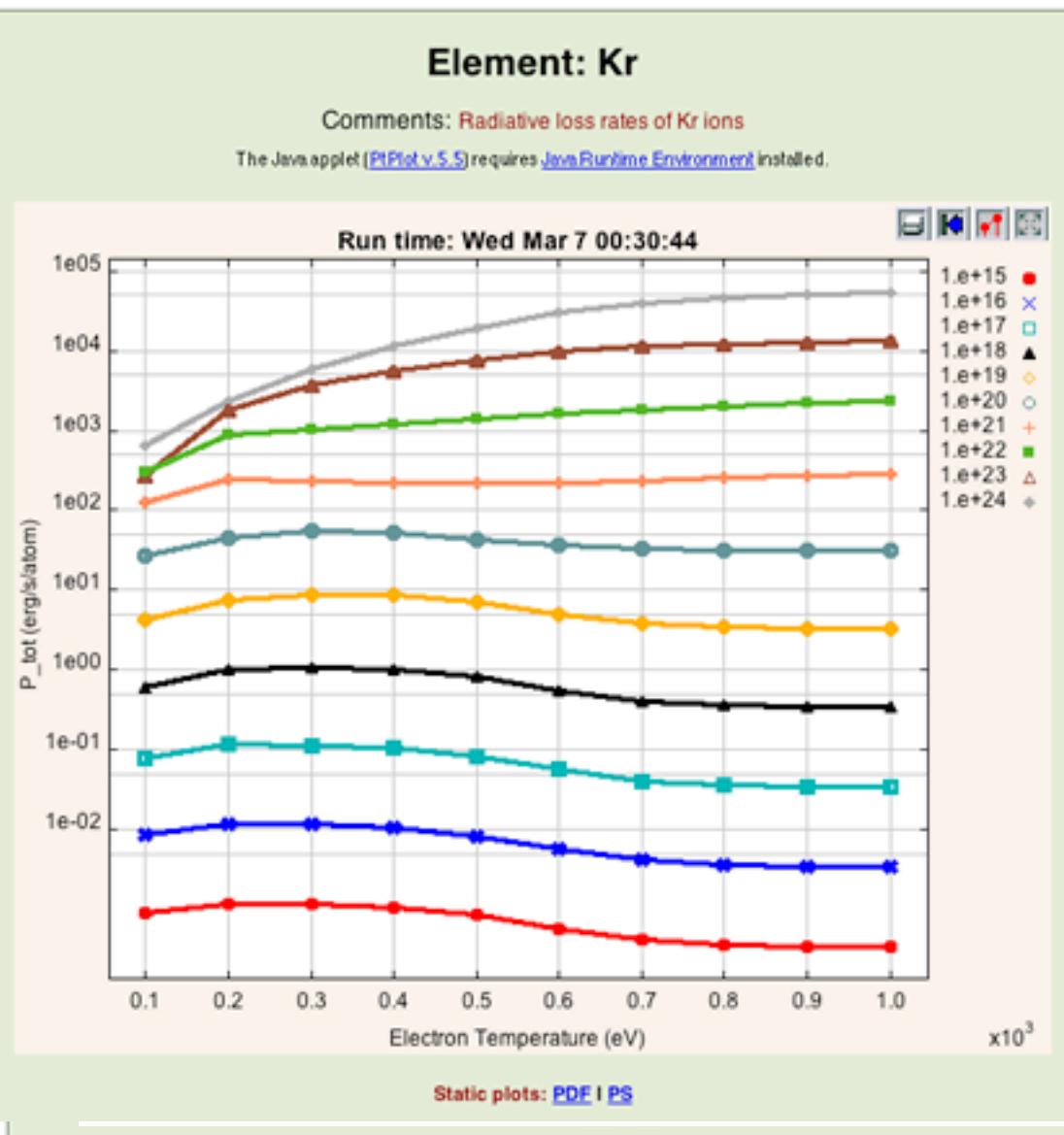
# Example: Radiative loss rates are important as an energy loss mechanism of high-Z plasmas

Calculated Kr radiative cooling rates per  $N_e$   
[eV/s/atom/cm<sup>-3</sup>]



# of radiative transitions  
using HULK code

# Data for Radiation Hydrodynamics: Kr Radiative loss rates over (Ne, Te)



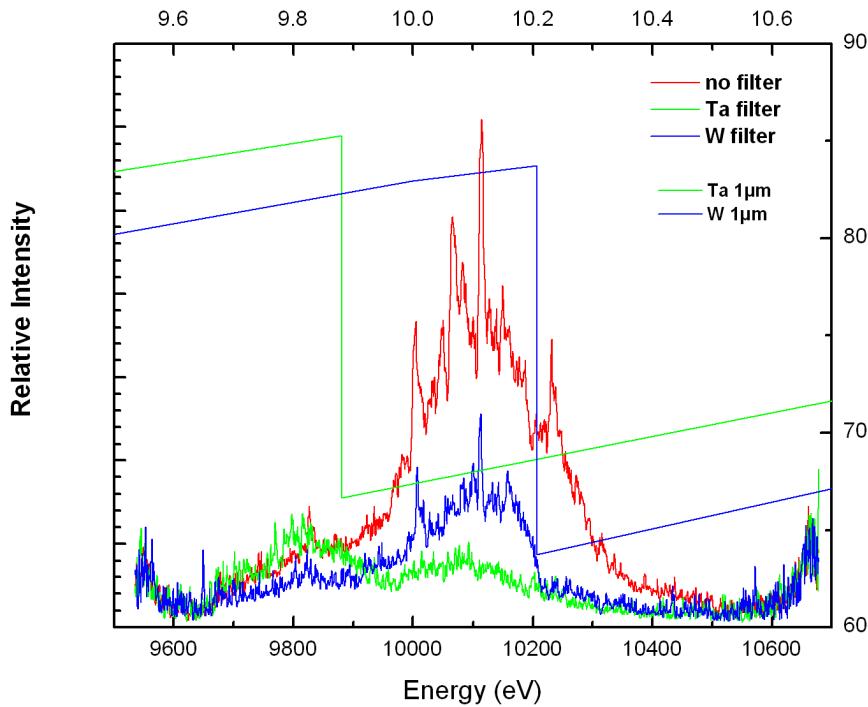
List of Selected Cases	
Dens	Data
1.e+15	<a href="#">file</a>
1.e+16	<a href="#">file</a>
1.e+17	<a href="#">file</a>
1.e+18	<a href="#">file</a>
1.e+19	<a href="#">file</a>
1.e+20	<a href="#">file</a>
1.e+21	<a href="#">file</a>
1.e+22	<a href="#">file</a>
1.e+23	<a href="#">file</a>
1.e+24	<a href="#">file</a>

The radiative loss rates show the similar coronal behavior up to  $N_e = 10^{17}$  and the rate/ $N_e$  stays constant. As  $N_e$  increases, the rate/ $N_e$  decreases from the coronal value

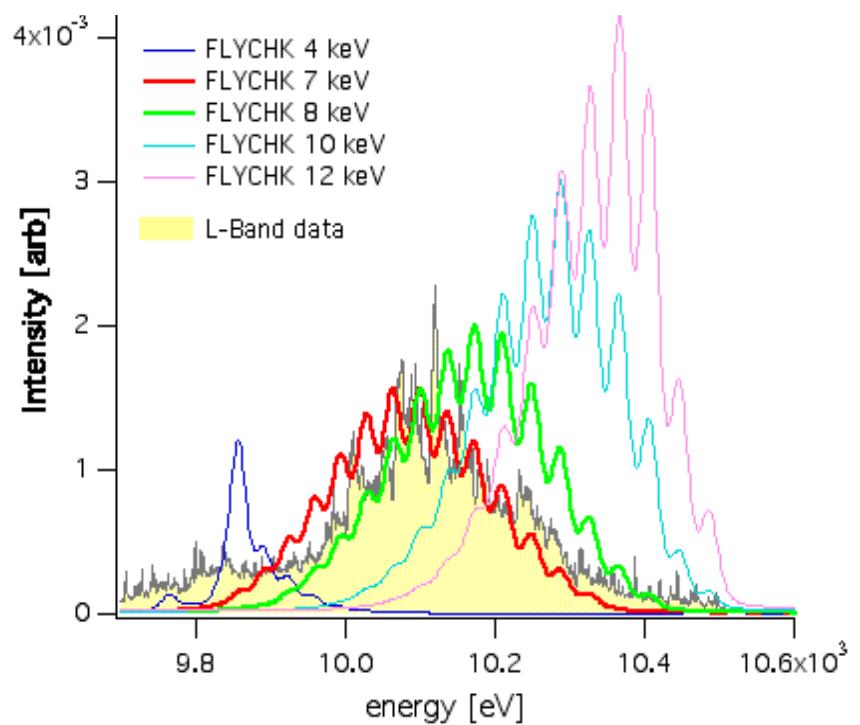
# Example: Gold ionization balance in high temperature hohlraum (HTH) experiments

- High-T hohlraum reach temperatures:  $\sim 10$  keV
- Spectrum from  $n_e \sim 4 \times 10^{21} \text{ cm}^{-3}$ ,  $T_e \sim 7\text{-}10$  keV measured for first time

L-shell gold spectra (K. Widmann)



Spectroscopic data and calculation



FLYCHK gives an estimate of Gold L-shell spectra

# Long pulse laser plasmas: Gold L-shell spectroscopy

**FLYCHK**

User: hchung

Runfile Input  
Parameter Input  
Results  
-Previous  
[log out](#)

Title of this run: Gold L-shell spectra

Diagnostics output:

Run FLYCHK Clear

Nuclear Charge ? 79 or upload file. Non-LTE Steady State Browse... Non-LTE Steady State

Initial Condition ? Non-LTE Steady State

System Evolution ?

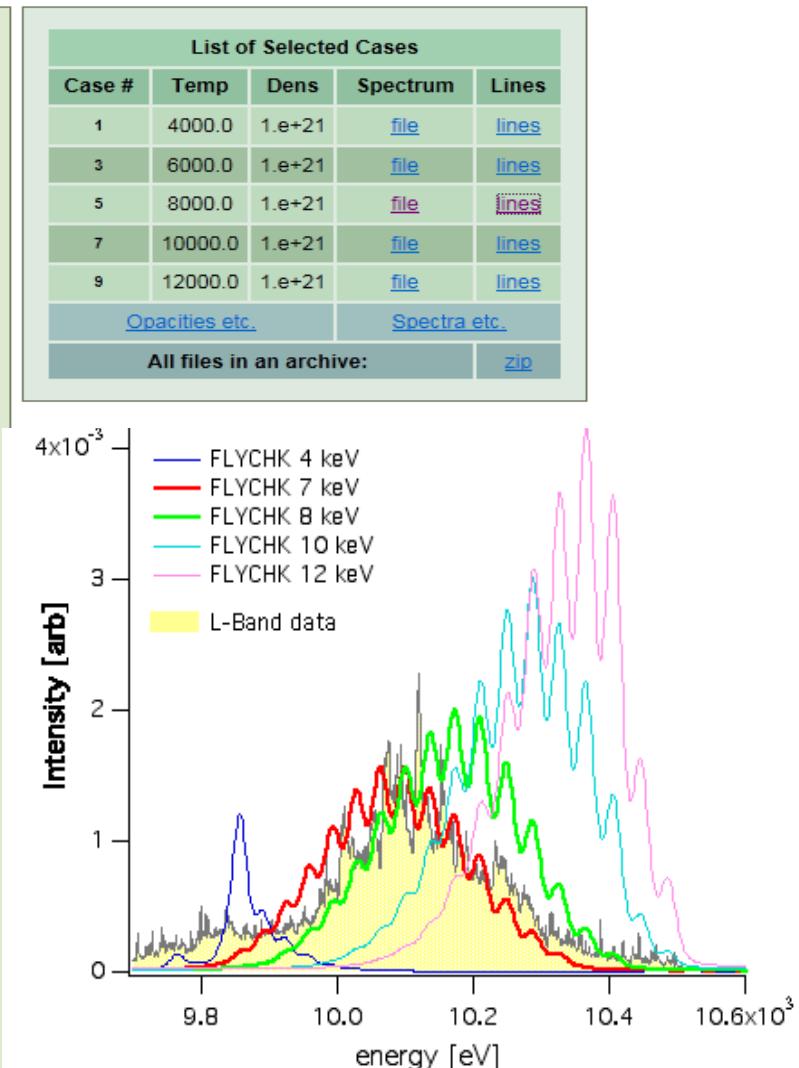
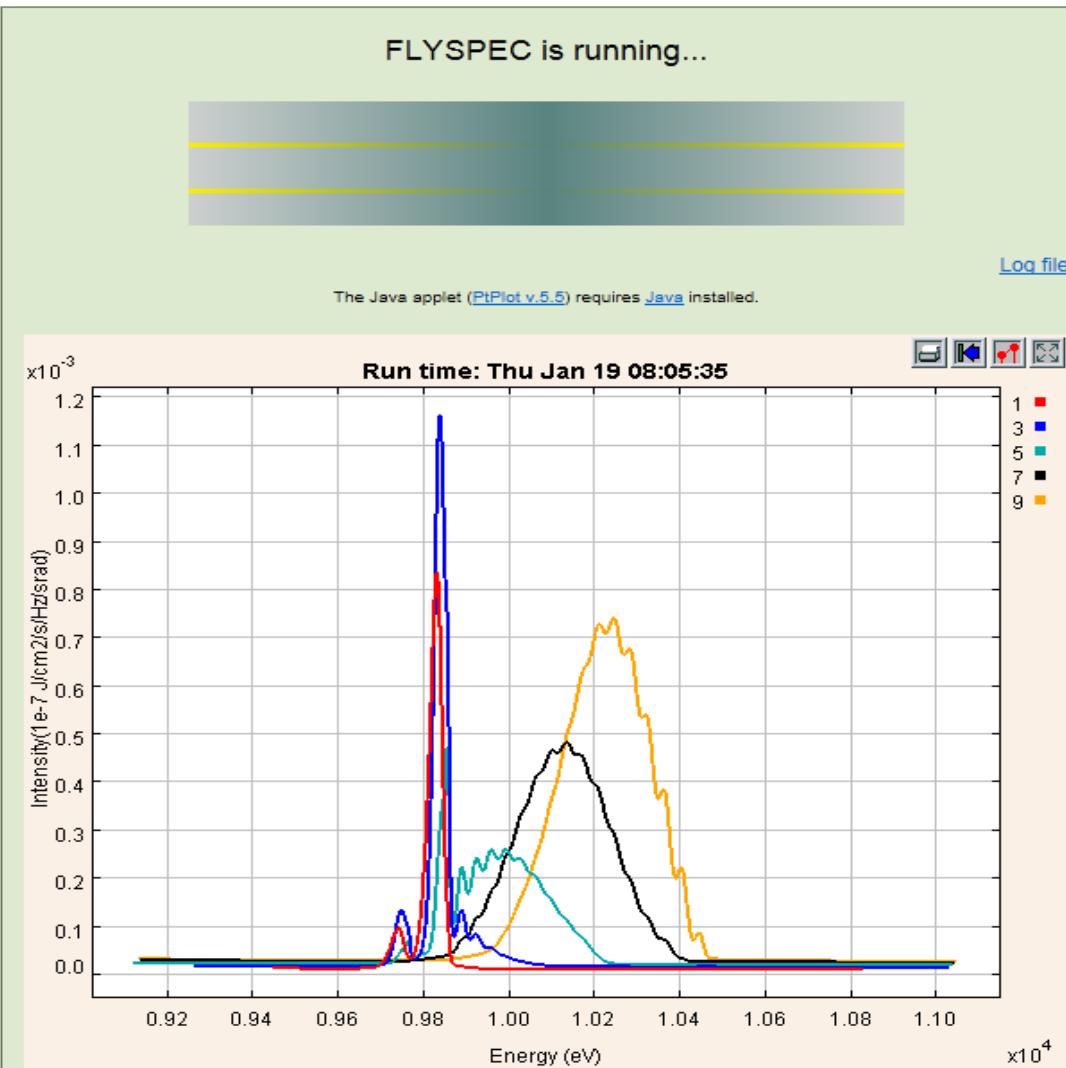
Electron Temperature [eV] (max 10 values) ? Initial: 4000 Final: 10000 Increment: 2000

Density Type Electron (max 10 values) ? Initial: 1e21 Final: 1e22 Increment: 10

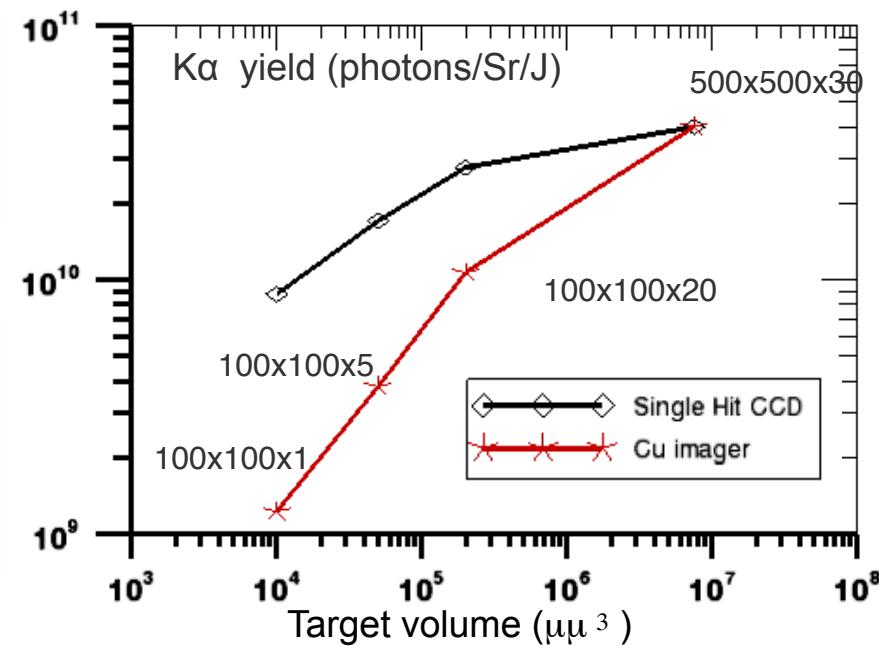
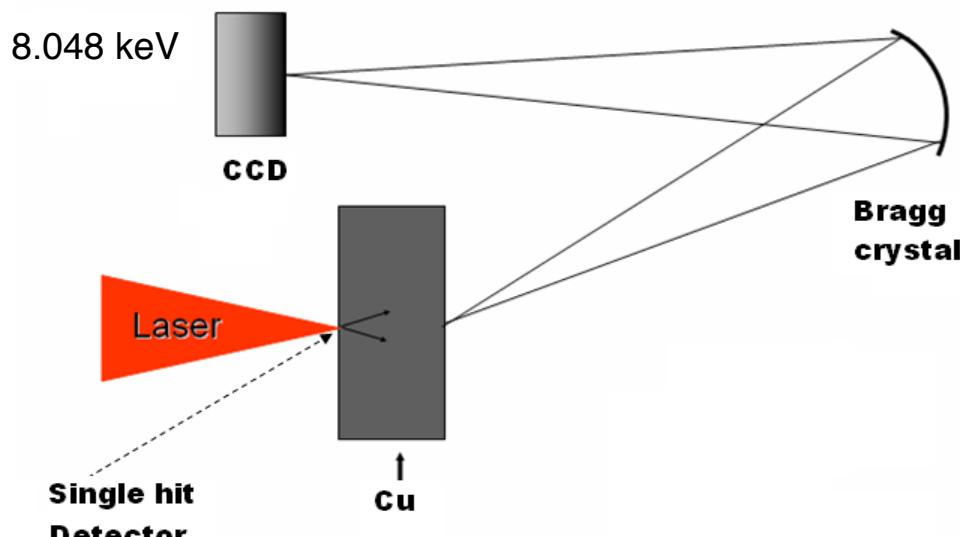
Mixture ? Z<sub>mix</sub>: Percent: Z<sub>num</sub>:  
Opacity ? Size (cm): Or history file:   
Ion T<sub>i</sub> [eV] ? T<sub>i</sub>/T<sub>e</sub>: Fixed T<sub>i</sub>: Or history file:   
2<sup>nd</sup> T<sub>e</sub> [eV] ? 2nd T<sub>e</sub>: Fraction: Or history file:   
Radiation T<sub>r</sub> [eV] ? T<sub>rad</sub>: Dilution : Or history file:   
Radiation Field ?  
EEDF ? Browse... Browse...

Run FLYCHK Clear

# STA spectra compared with configuration-average spectra



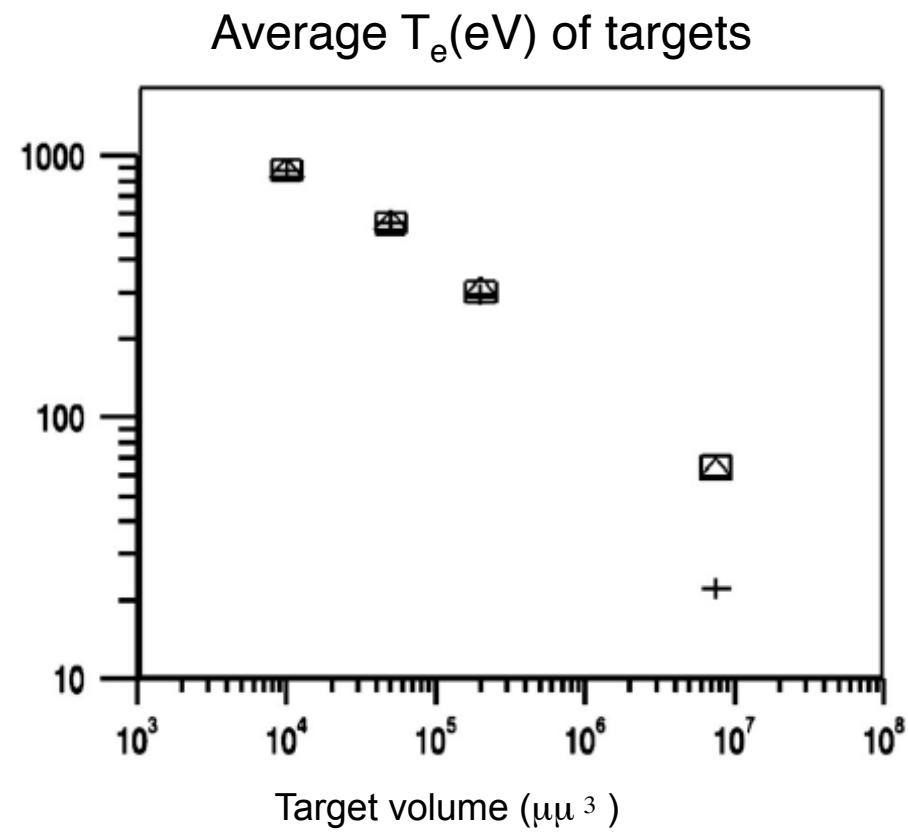
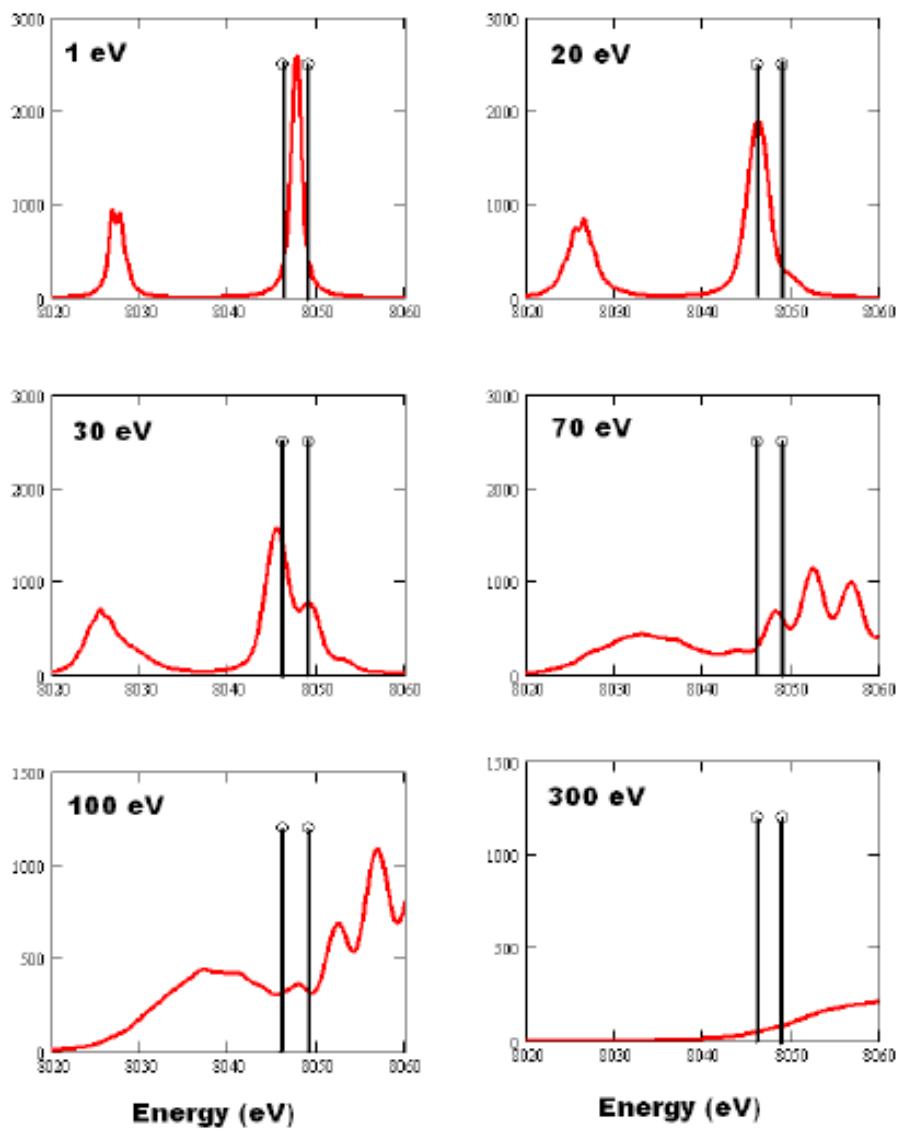
# Example: Cu K $\alpha$ radiation measured by single hit CCD spectrometer and 2-D imager for T<sub>e</sub> diagnostics



Single Hit CCD K $\alpha$  yield is higher than that of 2-D imager for smaller target volumes :  
An experimental evidence of shifting and broadening of K $\alpha$  emission lines in small targets with high temperatures

# Shifts and Broadening of K $\alpha$ emission as a function of electron thermal temperature

FLYCHK simulations



# Short pulse laser plasmas: Cu K $\alpha$ Spectroscopy

User: hchung

Runfile Input

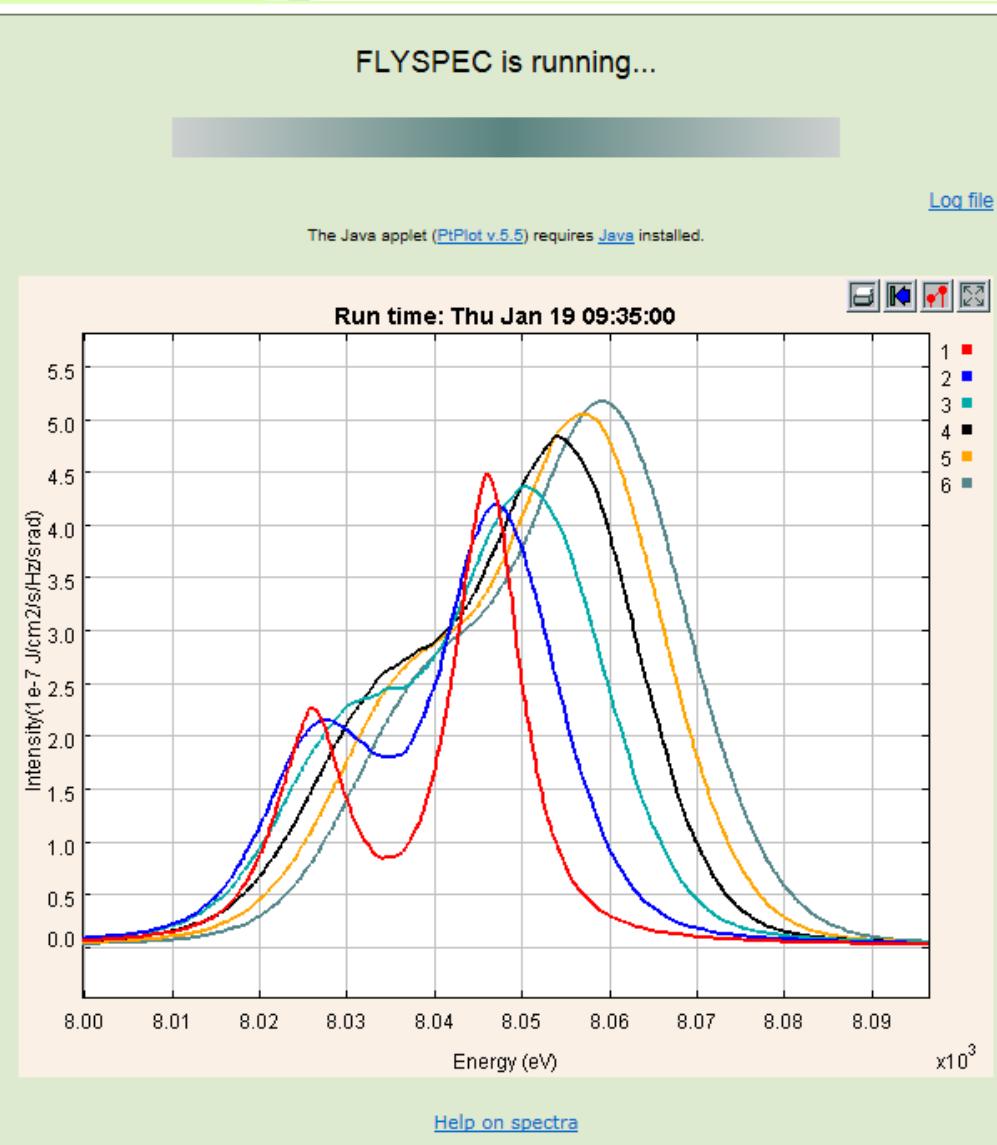
Parameter Input

- Grid
- History

Results

- Current
- Previous

[log out](#)

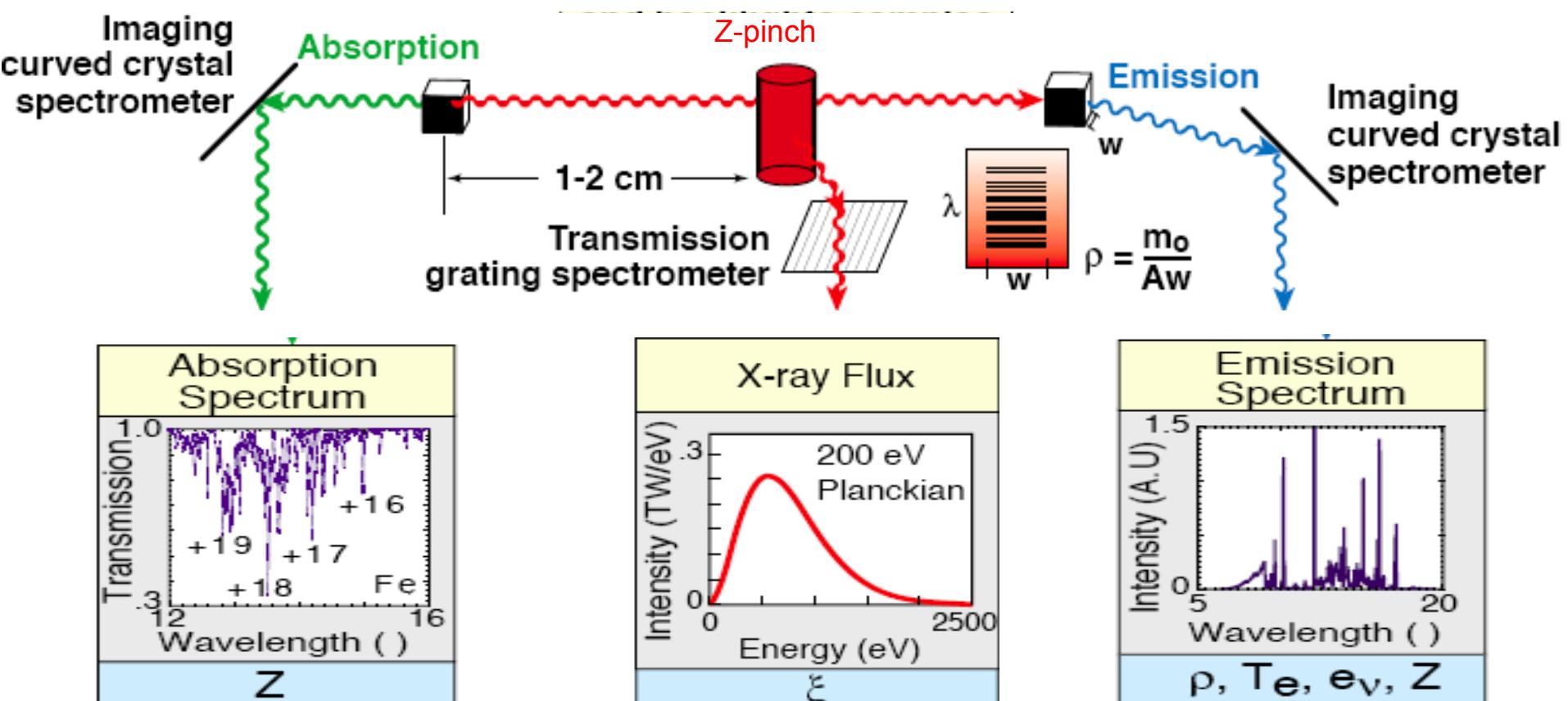


List of Selected Cases				
Case #	Temp	Dens	Spectrum	Lines
1	20.0	8.9e+00	<a href="#">file</a>	<a href="#">lines</a>
2	40.0	8.9e+00	<a href="#">file</a>	<a href="#">lines</a>
3	60.0	8.9e+00	<a href="#">file</a>	<a href="#">lines</a>
4	80.0	8.9e+00	<a href="#">file</a>	<a href="#">lines</a>
5	100.0	8.9e+00	<a href="#">file</a>	<a href="#">lines</a>
6	120.0	8.9e+00	<a href="#">file</a>	<a href="#">lines</a>

Opacities etc.      Spectra etc.

All files in an archive: [zip](#)

# Example: Photoionized plasmas produced by Z-Machines - Astrophysical model benchmark

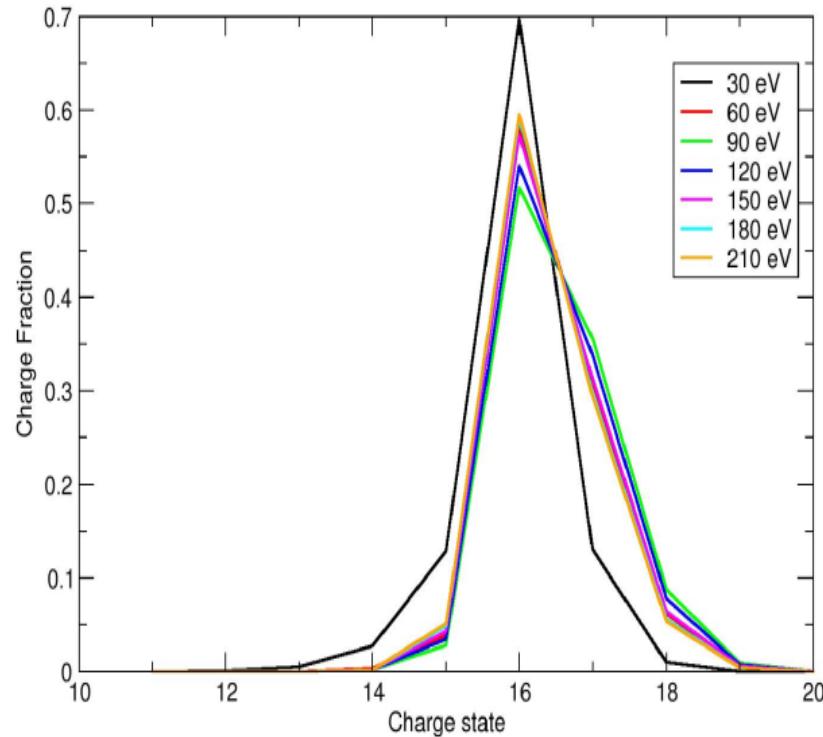
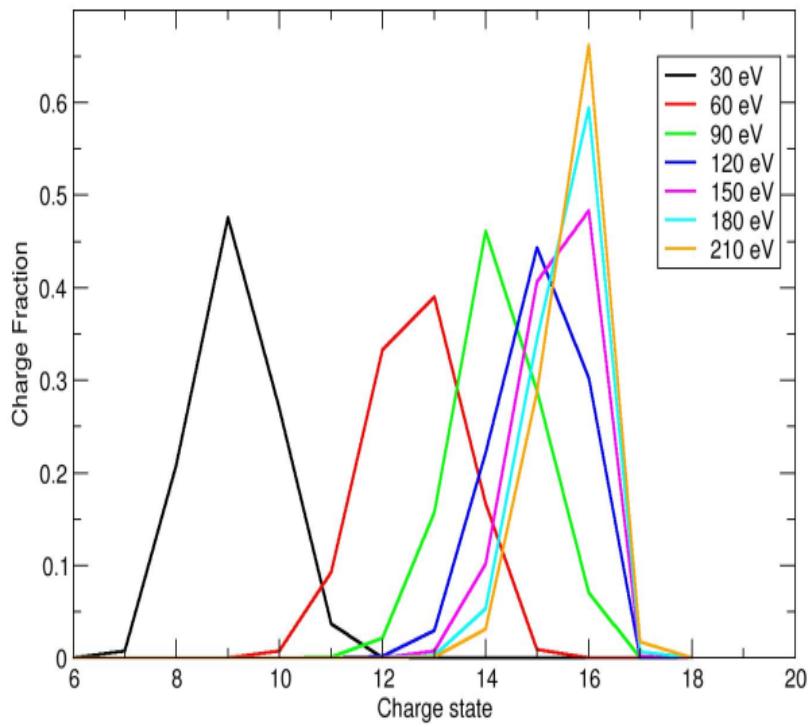


$$\xi = 20-25 \text{ ergs-cm/s}$$

# Charge state distribution is a function of $N_e$ and Radiation field strength

$N_e = 1.95 \times 10^{19} \text{ cm}^{-3}$

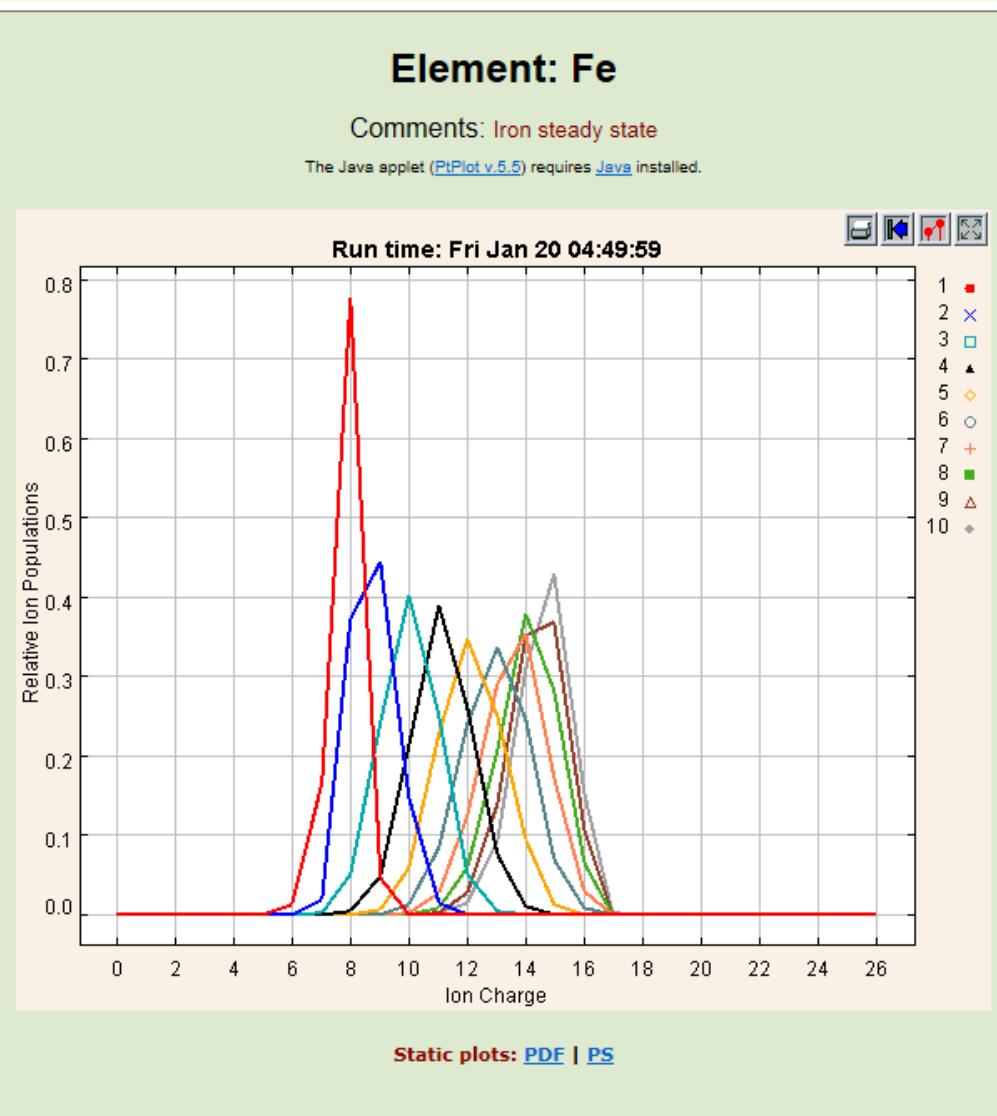
Radiation field of 165 eV and 0.01 dilution



# Photoionization equilibrium plasmas: Fe Z-Pinch Plasma

User: hchung

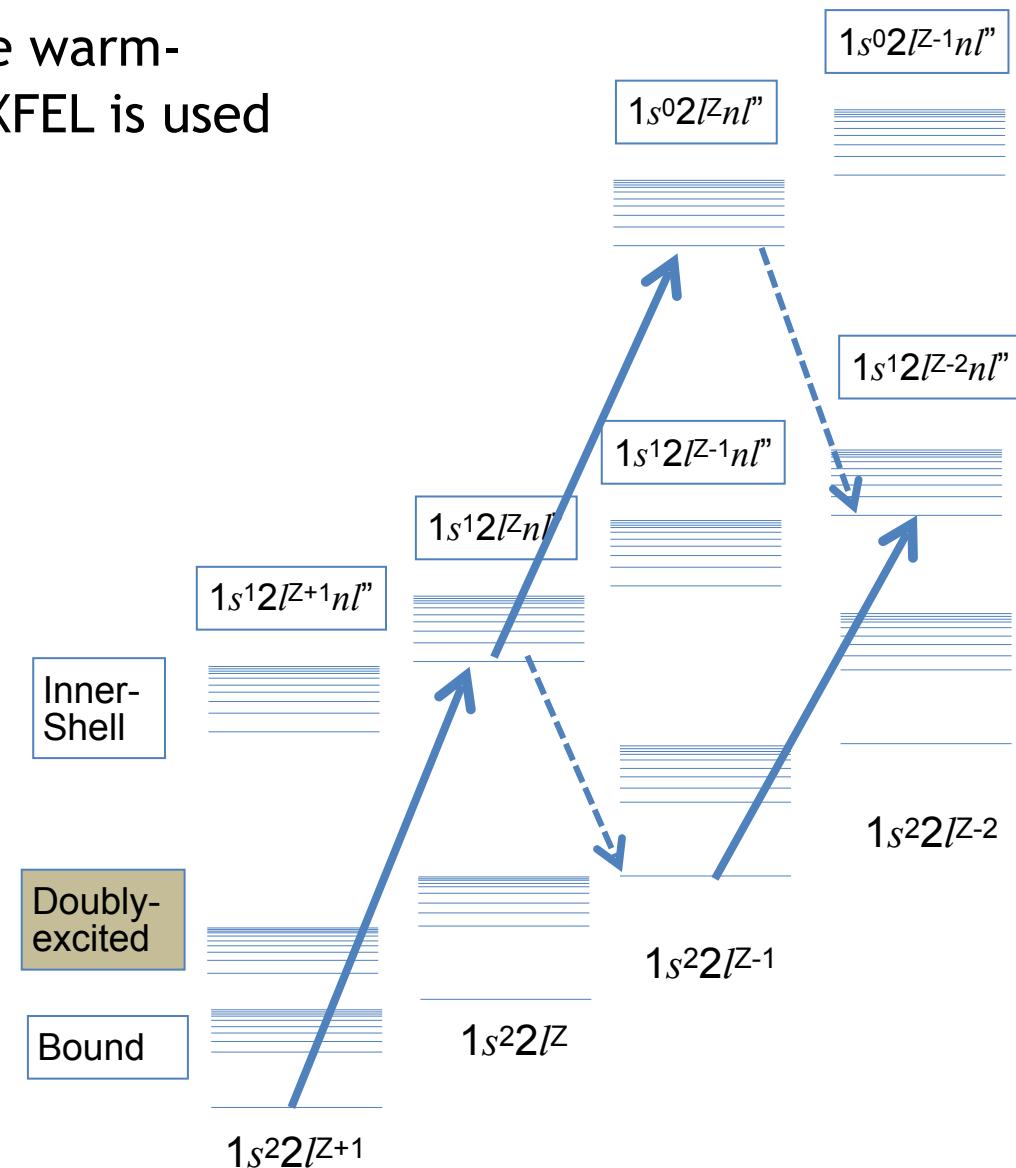
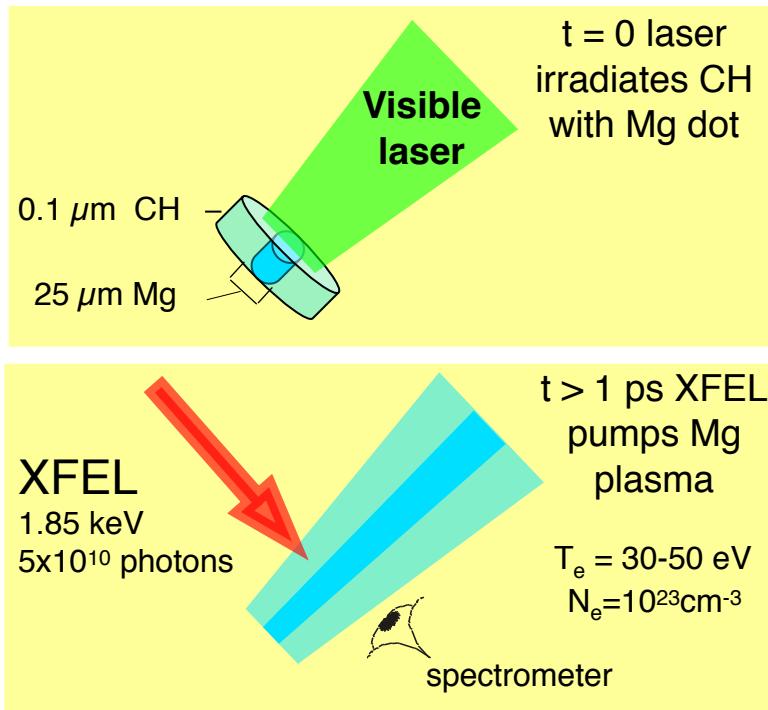
Runfile Input  
Parameter Input  
-Grid  
-History  
Results  
-Current  
-Previous  
[log out](#)



List of Selected Cases			
Case #	Temperature	Density	Data
1	30.0	1.95e+19	<a href="#">file</a>
2	50.0	1.95e+19	<a href="#">file</a>
3	70.0	1.95e+19	<a href="#">file</a>
4	90.0	1.95e+19	<a href="#">file</a>
5	110.0	1.95e+19	<a href="#">file</a>
6	130.0	1.95e+19	<a href="#">file</a>
7	150.0	1.95e+19	<a href="#">file</a>
8	170.0	1.95e+19	<a href="#">file</a>
9	190.0	1.95e+19	<a href="#">file</a>
10	210.0	1.95e+19	<a href="#">file</a>

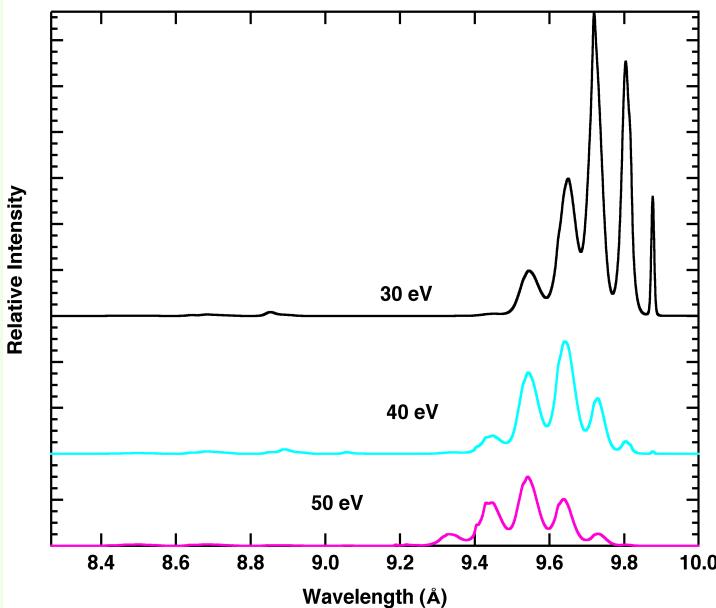
# Example: XFEL provides an opportunity for HEDS plasma spectroscopy

Long-pulse laser is used to create warm-dense-matter plasmas and then XFEL is used to probe the internal state.

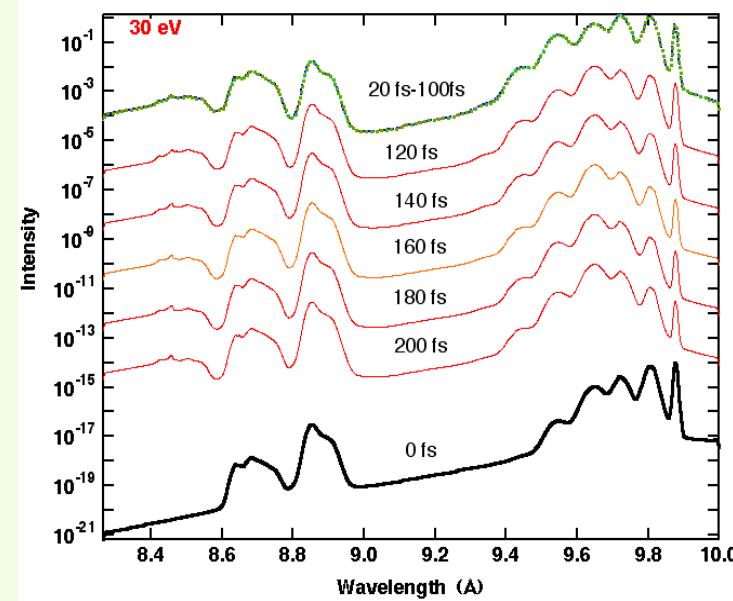


# In Warm Dense Matter regime the hollow ions provide time-resolved diagnostic information

- XFEL forms unique states *and* provides *in situ* diagnostics with ~100 fs res.
  - $5 \times 10^{10}$  1.85 keV photons in 30  $\mu\text{m}$  spot into a  $n_e = 10^{23} \text{ cm}^{-3}$  plasma
  - Strong coupling parameter,  $\Gamma_{ii}$  = Potential/Kinetic Energy  $\sim 10$

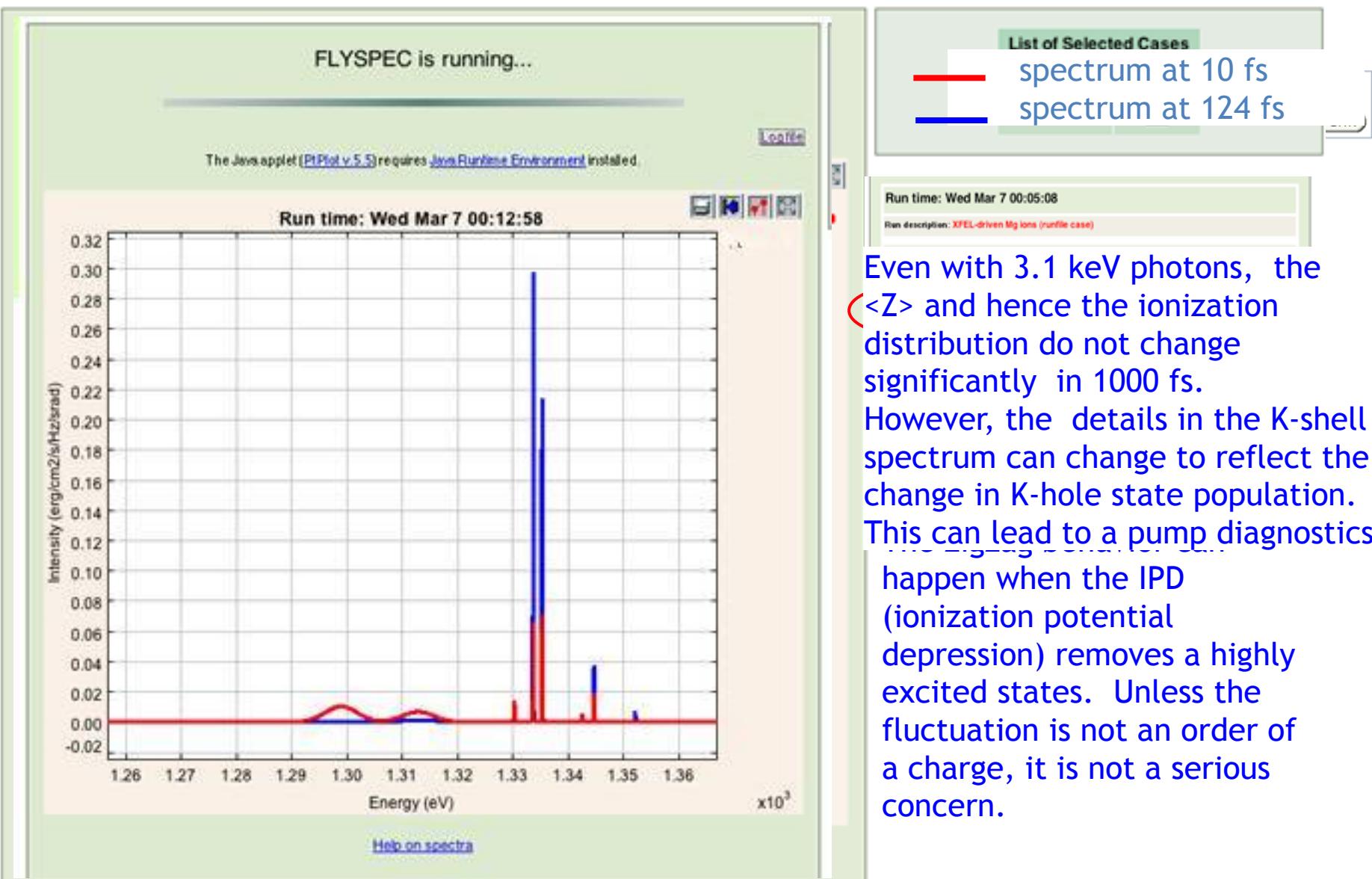


- Steady-state Spectra at various  $T_e$



- At high  $n_e$  emission lasts ~100 fs

# XFEL ionized plasma: Mg time-dependent K-shell spectroscopy



# Postprocessing electron kinetic simulation

- SiO<sub>2</sub> aerogel targets doped with Ge or Ti for X-ray backscatterer development
- 1-D e- kinetic code FPI shows Non-maxwellian energy functions due to strong laser heating and nonlocal electron heat flow -- J-P. Matte & K.B. Fournier

Title of this run: FPI silicon 002 case-diagnostics on 2

Diagnostics output:

Run FLYCHK Clear

Nuclear Charge: 12

Initial Condition: Steady State or upload file:

System Evolution: Time-dependent

Time History File: /Users/chung8/PROJECTS/FPI/tx002.d

Browse...

Density Type: Electron

Mixture: Z<sub>mix</sub>:  Percent:  Z<sub>ion</sub>:   
Or history file:

Opacity: Size (cm):   
Or history file:

Ion T<sub>i</sub> [eV]: T<sub>i</sub>/T<sub>e</sub>:   
Or history file:

2nd T<sub>e</sub> [eV]: 2nd T<sub>e</sub>:   
Fraction:   
Or history file:

Radiation T<sub>r</sub> [eV]: T<sub>rad</sub>:   
Dilution:   
Or history file:

Radiation Field:

EEDF: /Users/chung8/PROJECTS/FPI/fe002.d

For time-dependent case, set up output times: default is time steps specified in the history file

Evolution Type: Linear Start time: 0 End time: 1.e-9

linear or log grid only Time step number: 41

linear followed by log Final time for linear:  Linear step number:  Log step number:

log followed by linear Final time for log:  Log step number:  Linear step number:

Run FLYCHK Clear

History input always includes thermal T<sub>e</sub>  
EEDF is added as additional e- source

Runfile input can specify

EEDF to be the only e- source

0 0000E+00 0 0794E+00 2 1806E+20

Title of this run: FPI silicon 002 case- runfile input

Runfile upload: /Users/chung8/PROJECTS/FPI/run.tar

Diagnostics output:

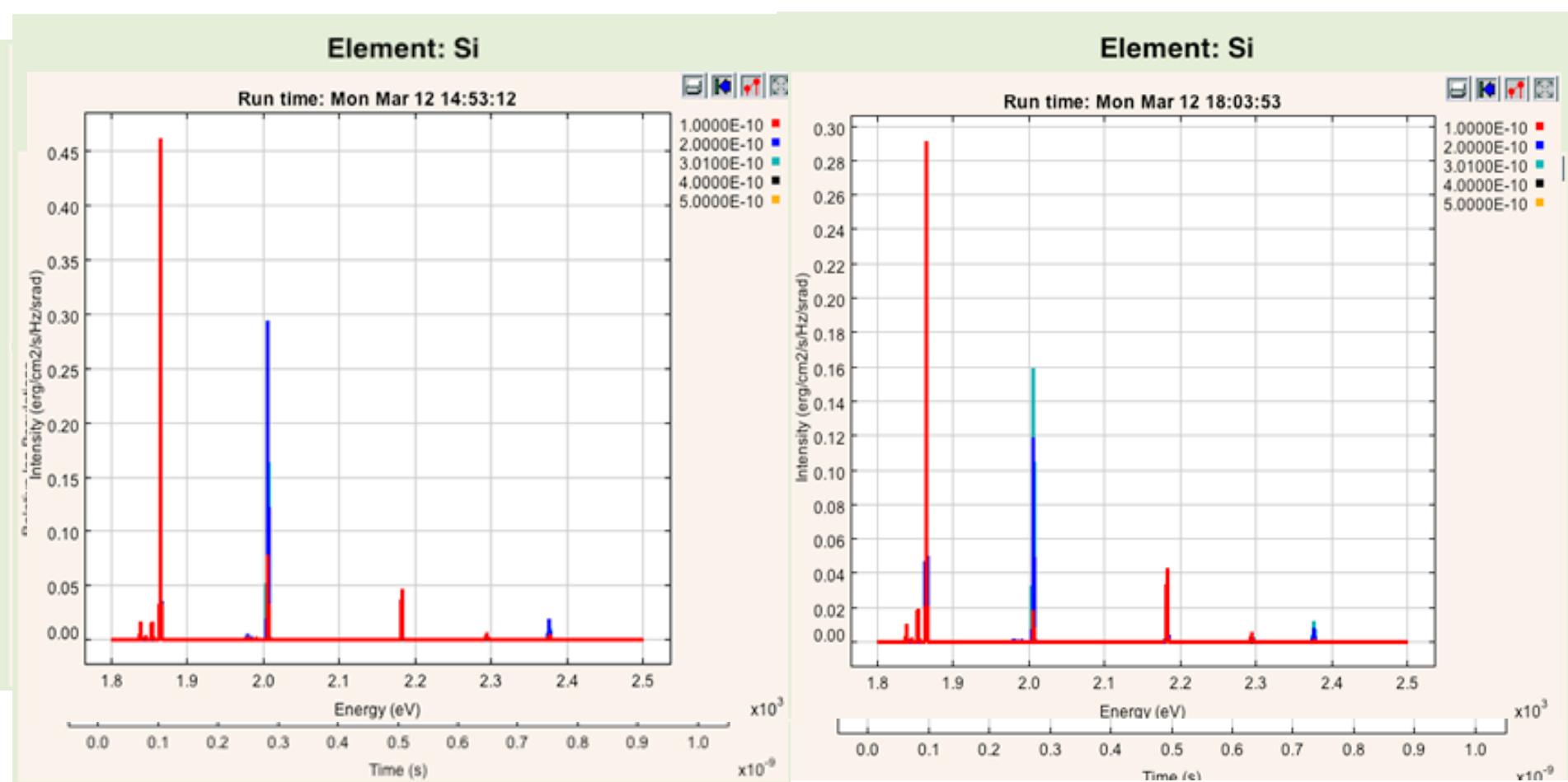
Run FLYCHK

6.89062E+018 2.6562E+019 7.6562E+011 1.3906E+02  
c Te and EEDF input always included  
1.31406E+02 4.50156E+02 1.70156E+02 1.91406E+02  
2.13906E+02 2.35705E+02  
2.62562E+02 2.80002E+02 1.68363E+02 3.1516E+20  
2.62562E+02 2.80002E+02 1.68363E+02 3.1516E+20  
3.07562E+02 3.30002E+02 1.8437E+02 3.6516E+20  
5.07656E+00 2.43006E+02 2.745E+03 8.6984E+20  
5.81406E+02 6.20156E+02 6.60156E+02 7.01406E+02  
7.043906E+02 7.187156E+02 8.32656E+02 8.78906E+02  
9.126406E+02 9.5575156E+02  
1.002516E+03 1.07641E+03 1.12891E+03 1.18260E+03  
1.123766E+03 1.20991E+03 1.26955E+03 1.31140E+03  
1.145016E+03 1.05344E+03  
.time 0. 1.e-9 41  
end

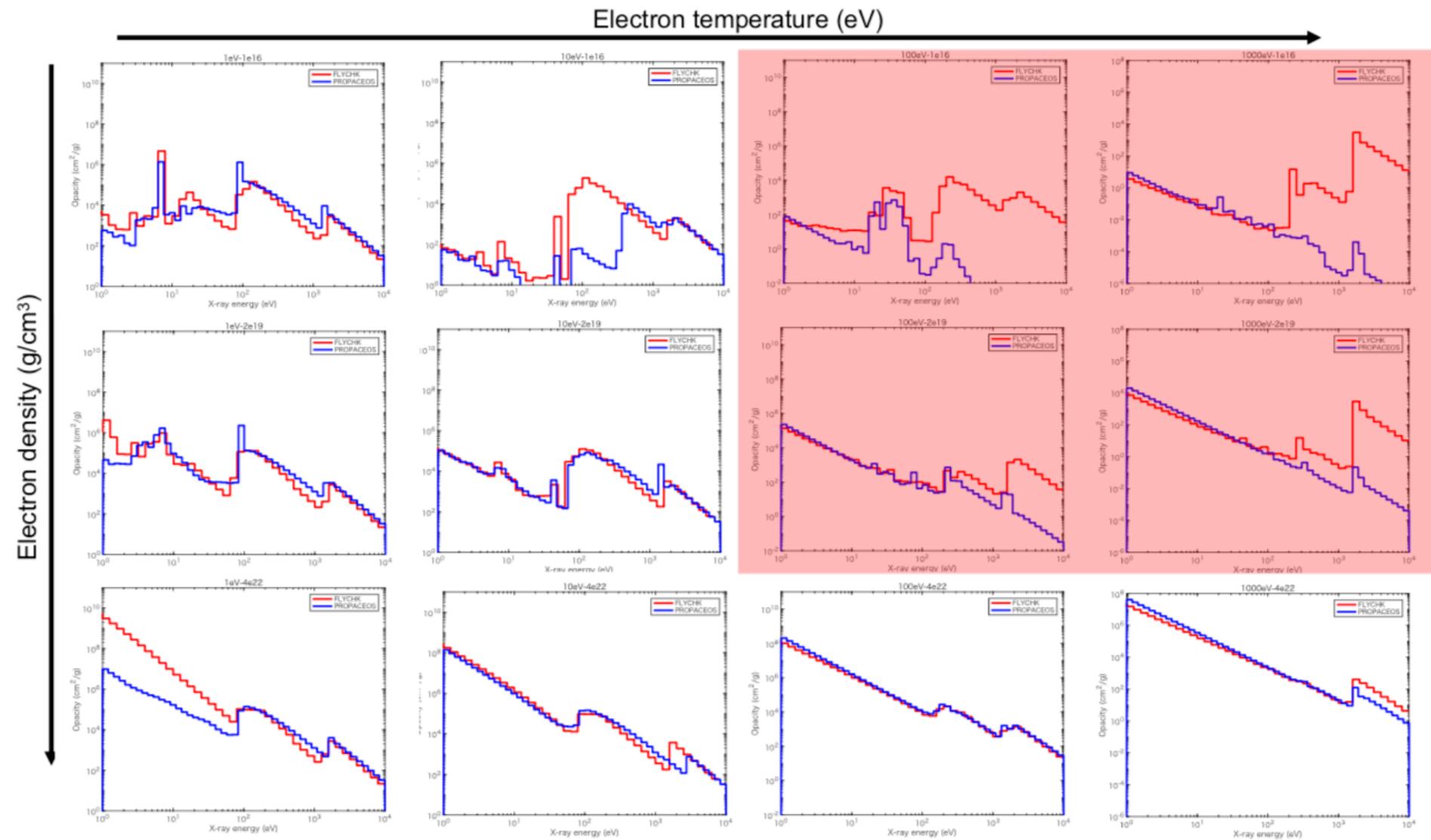
# Output: $\langle Z \rangle$ is quite similar with/without thermal e-

Using fe(E) with thermal e-

Using fe(E) only without thermal e-



# Aluminum Opacity (NIST data)



# Useful Examples

<http://nlte.nist.gov/FLY/EXAMPLE.html>

Please check the Screen shot of each case

nlte.nist.gov/FLY/EXAMPLES\_images/case1.gif

**FLYCHK**

User: hchung

Title of this run:  Run Clear

Diagnostics output:

Runfile Input

Parameter Input

-Grid  
-History

Results

-Previous

[log out](#)

Nuclear Charge  Initial Condition  or upload file:   
System Evolution

Electron Temperature  Initial:  Final:  Increment:   
Density Type  Initial:  Final:  Increment:

Mixture  Percent:  Znum:   
Opacity  Or history file:   
Ion T<sub>i</sub> [eV]  Fixed T<sub>i</sub>:  Or history file:   
2<sup>nd</sup> T<sub>e</sub> [eV]  Fraction:  Or history file:   
Radiation T<sub>r</sub> [eV]  Dilution :  Or history file:   
Radiation Field  Browse...  
EEDF  Browse...

Run Clear

FLYCHK at NIST is developed and managed by H.-K. Chung, M. Chen and R. W. Lee at LLNL and Yu. Ralchenko at NIST. This work was performed under the auspices of the U.S. Department of Energy by University of California Lawrence Livermore National Laboratory under Contract No. W-7406-Eng-48

### Theory and Modeling:

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