

Technical Meeting

Hydrogen Supersaturation and Defect Stabilization

**Thermodynamics Models based on DFT data for Hydrogen
Supersaturation and Defects Stabilization**

Yves Ferro



11-12 April 2022 Aix-en-Provence, France



Outline

1 . The basic ingredients



- Density Functional Theory
- Statistic Thermodynamics (Gibbs free energy)

2 . Thermodynamic models for vacancies

3 . Supersaturation and vacancy stabilization

4 . Discussion

1. The Basic Ingredient

Density Functional Theory – *electronic energy*



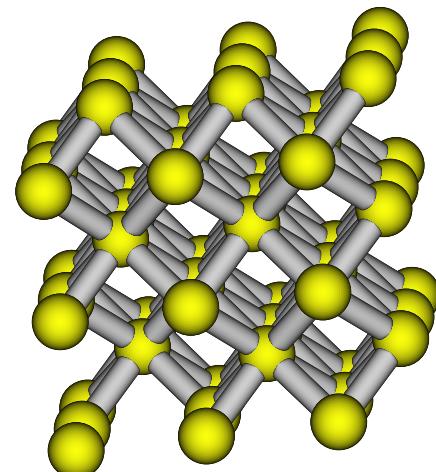
Calculating the **electronic energy** of a system of electrons and nuclei

- Should be done using [Quantum Mechanics](#)
- Achieved through solving the [Schrödinger equation](#)
- Solutions not known, approximation, Hartree-Fock
- [Limitation](#): the wave-function depends on too many variables
 $\Psi(r_1, r_2, \dots, r_N)$ for a system of N electrons



An alternative: the **Density Functional Theory**

- The [electronic density \$\rho\(r\)\$](#) only depends on three space variables
- The idea is to compute $E[\rho]$
- The question is how ?



1. The Basic Ingredient

Density Functional Theory – total energy

$$\rightarrow E^{elec}[\rho] = E_{kin}[\rho] + E_{electron-nuclei}[\rho] + E_{electron-electron}^{Coulmob}[\rho] + E_{electron-electron}^{XC}[\rho]$$

Classical terms

Quantum terms :

$E_{kin}[\rho]$ – Known for *non-interacting* electrons

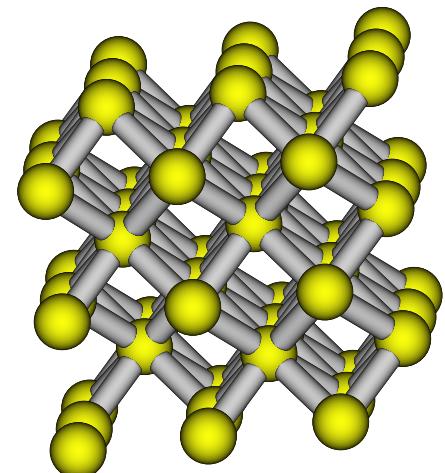
$E_{electron-electron}^{XC}[\rho]$ – approximation
eXchange-Correlation functional

Total energy:

$$E^{DFT} = E^{elec}[\rho] + E_{nuclei-nuclei}$$

Ground state energy

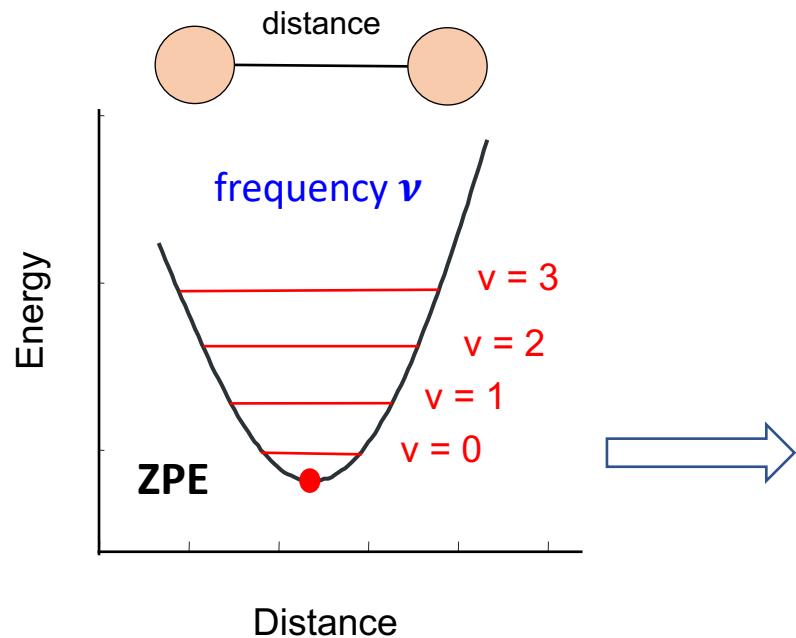
Does not include the Temperature



1. The Basic Ingredient

Density Functional Theory

– *vibrational frequencies*



At T = 0K, only $v=0$ is populated.

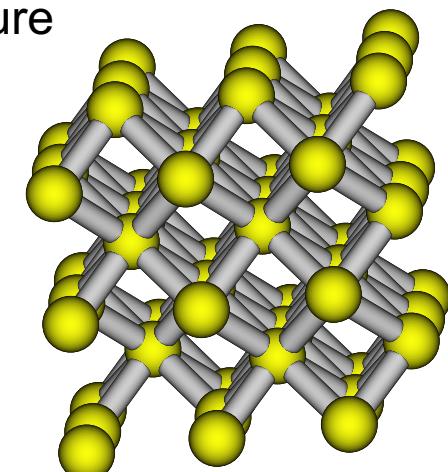
Then, energy levels v populated with increasing temperature.

Bulk system of N atoms

$3N - 3$ frequencies ν_j (phonons)

Energy levels are populated with increasing temperature

Vibrational energy depending on the temperature



The energy of the system is made temperature dependent

$$E_{tot}(T) = E^{DFT}(0K) + E_{vib}(T)$$

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1 . The basic ingredients

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- Statistic Thermodynamics



2 . Thermodynamic models for vacancies creation

3 . Supersaturation and vacancy stabilization

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1. The Basic Ingredient

Statistic Thermodynamics

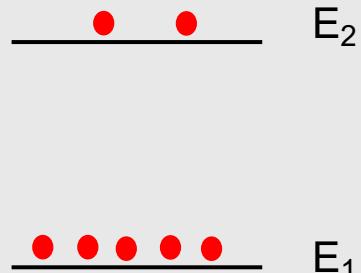
– State function Energy

Large number of particles $\sim 10^{23}$

$$E_{tot}(T) = E^{DFT}(0K) + E_{vib}(T) + \cancel{E_{elec}(T)} + E_{trans}(T) + E_{rot}(T) + \dots$$

Bulk materials

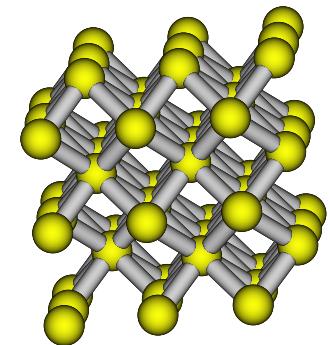
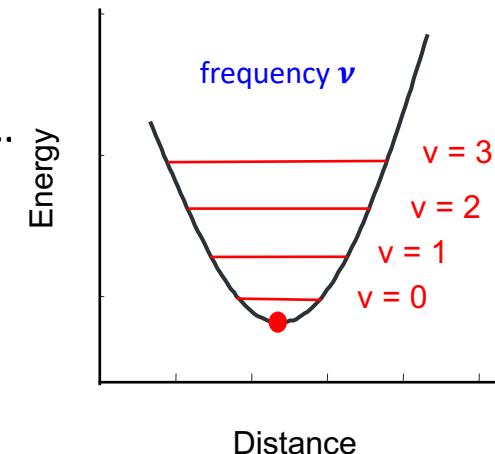
Two levels



$$E_{mean}(T) = p_1(T) E_1 + p_2(T) E_2$$

$p_1(T)$ Boltzmann statistic

$$E_{mean}(T) = \sum_j p_j(T) \cdot E_j$$



$$E^{vib}(T, \mathbf{v}_j) = \sum_{j=1}^{n_{vib}} h\mathbf{v}_j \left(\frac{1}{2} + \frac{1}{\exp\left(\frac{h\mathbf{v}_j}{k_B T}\right) - 1} \right)$$

$$E_{tot}(\textcolor{blue}{T}) = E_{tot}^{DFT}(0K) + E_{vib}(T)$$

1. The Basic Ingredient

Statistic Thermodynamics

– *Toward equilibria*

Criterion for stability ?

$$p_1(T) > p_2(T)$$



$$p_1(T) ? p_2(T)$$



Is E the criterion for stability ?

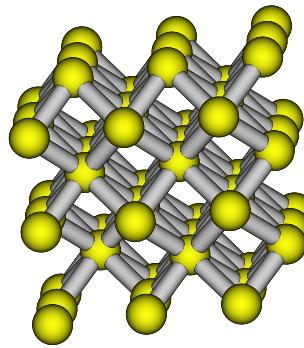
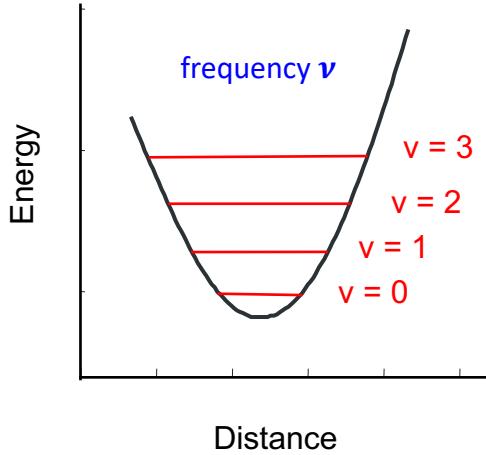
Because of the degeneracy, E₂ might be most populated depending on T

Entropy $S(T) = -k_B \sum_j p_j(T) \ln p_j(T)$

1. The Basic Ingredient

Statistic Thermodynamics

– State function Entropy



$$S(T) = -k_B \sum_j p_j(T) \ln p_j(T)$$

Vibrational entropy

$$S^{vib}(T, \mathbf{v}_j) = k_B \sum_{j=1}^{n_{vib}} \left[\frac{h\mathbf{v}_j}{k_B T} \frac{1}{\exp\left(\frac{h\mathbf{v}_j}{k_B T}\right) - 1} - \ln \left(1 - \exp\left(-\frac{h\mathbf{v}_j}{k_B T}\right) \right) \right]$$

Configurational entropy

Creating vacancies

N lattice sites

N_{at} atoms at lattice sites

n_V vacancies at lattice sites

$$N = N_{at} + n_V$$

Number of configuration

$$\Omega = \frac{(N_{at} + n_V)!}{N_{at}! n_V!}$$

Entropy (Boltzmann definition)

$$S(T) = k_B \ln \Omega$$

1. The Basic Ingredient

Statistic Thermodynamics

– Equilibrium conditions

Helmoltz Free Energy

$$F(T) = E(T) - T \cdot S(T)$$

Bulk: $F(T) \approx G(T)$

Gibbs Free Energy

$$G(T) = H(T) - T \cdot S(T)$$

Combines criterion on **energy** and **entropy**

Potential

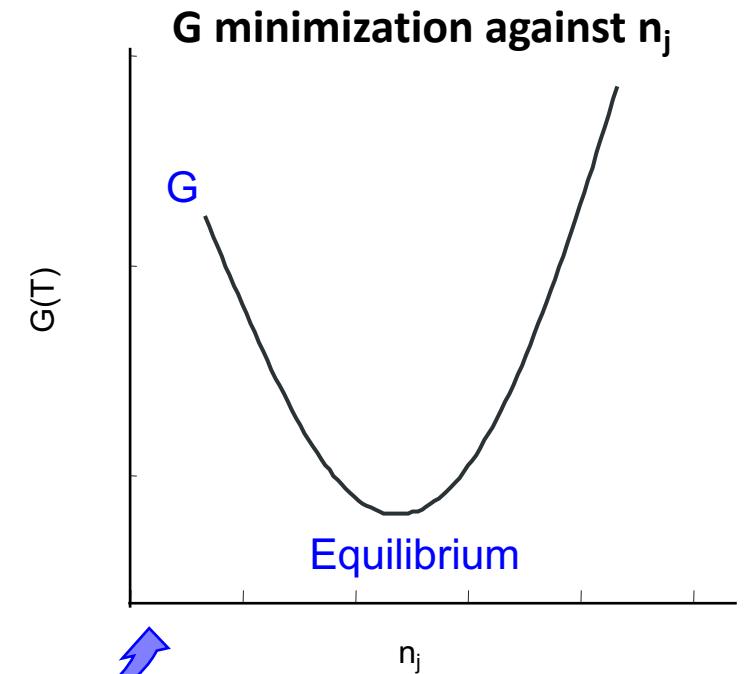
Conditions for equilibrium - system of N components

Gibbs free energy per particle for each j sub-system

$$g_j = e_j - T \cdot s_j \quad e_j(T) = e_j^{DFT} + e_j^{\text{vib}}(T) \quad s_j(T) = s_j^{\text{vib}}(T)$$

$$G(T, p, n_1, n_2, \dots, n_N) = \sum_j n_j \cdot g_j(T) - T \cdot S^{\text{conf}}(T)$$

μ_j chemical potential



Minimization

Provides $n_1^{eq}, n_2^{eq}, \dots, n_N^{eq}$

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2 . Thermodynamic models for vacancies



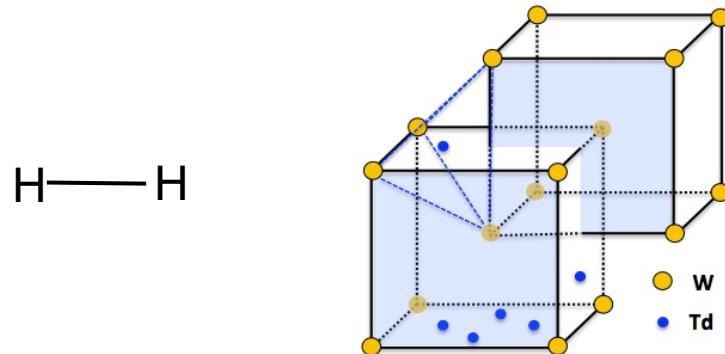
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- Results of the model
- Chemical potential and flux

3 . Supersaturation and vacancy stabilization

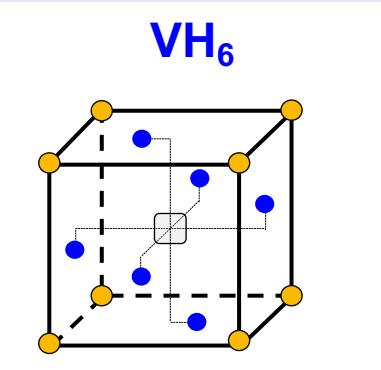
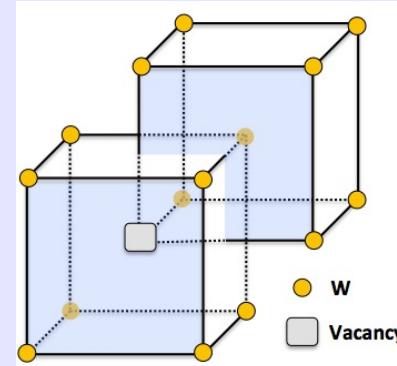
4 . Discussion

2. Thermodynamics model for Vacancies

Perfect



Defects



Electronic structure DFT calculations

Molecule H_2

$$e_{H_2}^{DFT}$$

Interstitial H_i

$$e_{H_i}^{DFT}$$

Vacancy V

$$e_V^{DFT}$$

VH_j with $j = 0 - 12$

$$e_{VH_j}^{DFT}$$

$$\nu_{H_2}$$

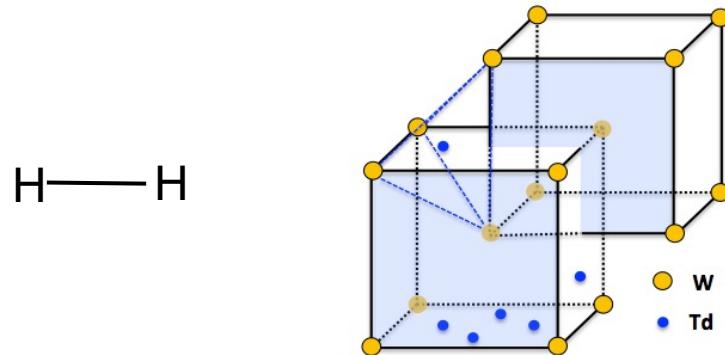
$$\sum_{k=1}^3 \nu_k$$

Vibrational frequencies DFT calculations

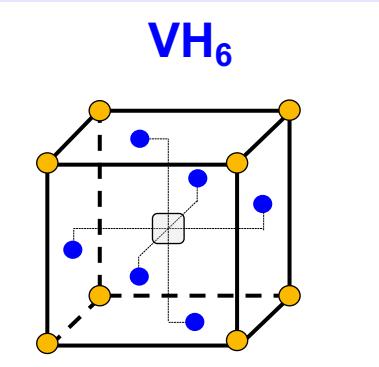
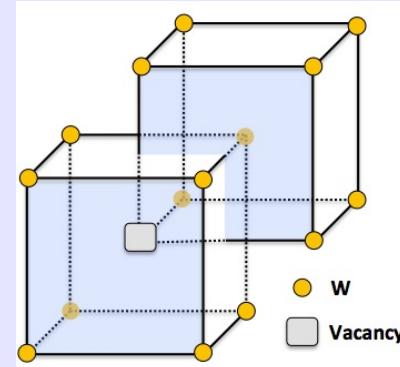
$$\sum_{k=1}^{3j} \nu_k$$

2. Thermodynamics model for Vacancies

Perfect



Defects



$$g_j = e_j - T \cdot s_j$$

$$G(T, p, n_{H_2}, n_{H_i}, n_V, n_{VH_1} \dots, n_{VH_{12}}) = \sum_j n_j \cdot g_j(T) - T \cdot S^{conf}(T)$$

H₂ Gas ideal gas

$$g_{H_2} = g_{H_2}^\circ + k_B T \ln \frac{P}{P^\circ}$$

$$g_{H_2}^\circ = (e_{H_2}^{DFT} + e_{H_2}^{vib} + e_{H_2}^{rot} + e_{H_2}^{trans} + PV) - T(s_{H_2}^{vib} + s_{H_2}^{rot} + s_{H_2}^{\circ trans})$$

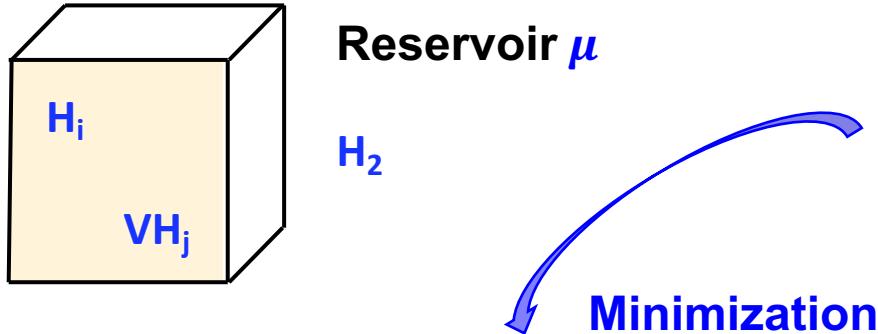
High pressure : Tkacz and Litwiniuk, J. Alloys Compounds 330-332 (2002) 89-92

The minimizing against

$$n_{H_2}, n_{H_i}, n_V, n_{VH_1} \dots, n_{VH_{12}}$$

2. Thermodynamics model for Vacancies

Composition of the system at equilibrium



$$G = \frac{1}{2} \left(N_H - n_{int} - \sum_{j=0}^{12} j n_j \right) \mu_{H_2} + n_{int} g_{int} + \left(\sum_{j=0}^{12} j n_j g_j \right) - T S_{conf}$$

$$x_{H_i}(T) \approx \gamma \exp \left[- \frac{g_{H_i} - \mu}{k_B T} \right]$$

H at interstitial

$$x_{VH_j}(T) \approx \omega_j \exp \left[- \frac{g_{VH_j} - j \mu}{k_B T} \right]$$

H in VH_j vacancies

$$\mu = \frac{1}{2} g_{H_2} = \frac{1}{2} (g_{H_2}^\circ + k_B T \ln \frac{P}{P^\circ})$$

Chemical potential H_2 ideal gas

High pressure : Tkacz and Litwiniuk, J. Alloys Compounds 330-332 (2002) 89-92

The chemical potential defines

- The fraction of H interstitial
- The fraction of VH_j vacancies

Reversely H_{int} defines

- The chemical potential
- The fraction of VH_j vacancies

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2 . Thermodynamic models for vacancies

- The model
- • Results of the model
- Chemical potential and flux

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2. Thermodynamics model for Vacancies

Formation of vacancies induced by interstitial H atoms

N. Fernandez, Y. Ferro, D. Kato, Acat Mater 94 (2015) 307-318

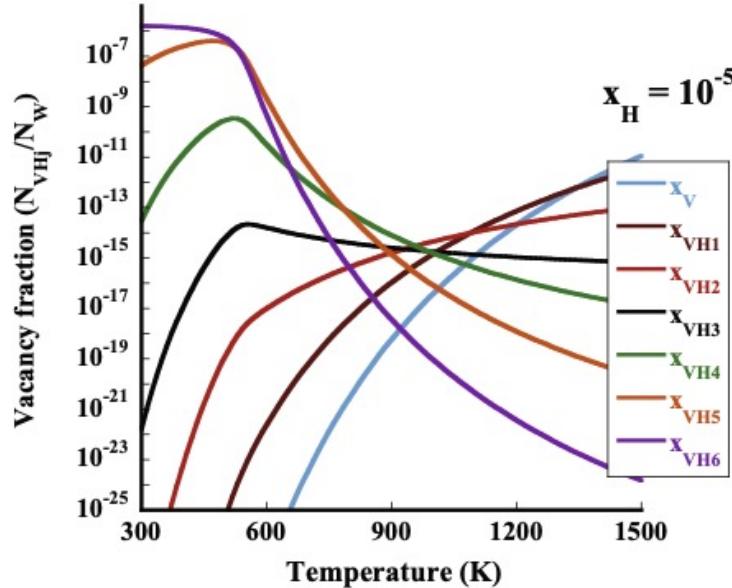
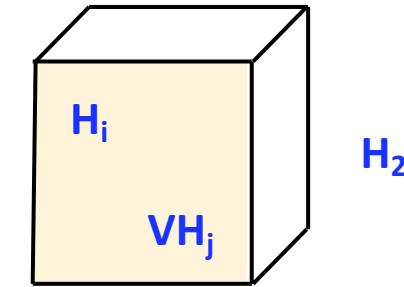


Fig. 8. Fractions x_j of vacancy type VH_j in tungsten at thermodynamic equilibrium for a total fraction of hydrogen $x_H = 10^{-5}$.



$$x_{H_i}(T) \approx \gamma \exp \left[-\frac{g_{H_i} - \mu}{k_B T} \right]$$
$$x_{VH_j}(T) \approx \omega_j \exp \left[-\frac{g_{VH_j} - j \mu}{k_B T} \right]$$

Interstitial H atoms impose a high chemical potential
This induces a high fraction of VH_j vacancies

High temperature entropy favors interstitials
→ Vacancies are depopulated

2. Thermodynamics model for Vacancies

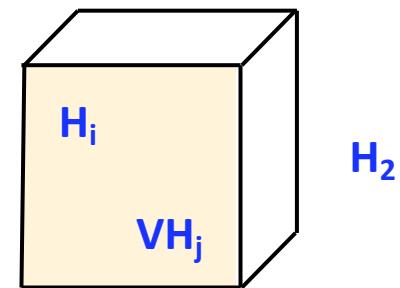
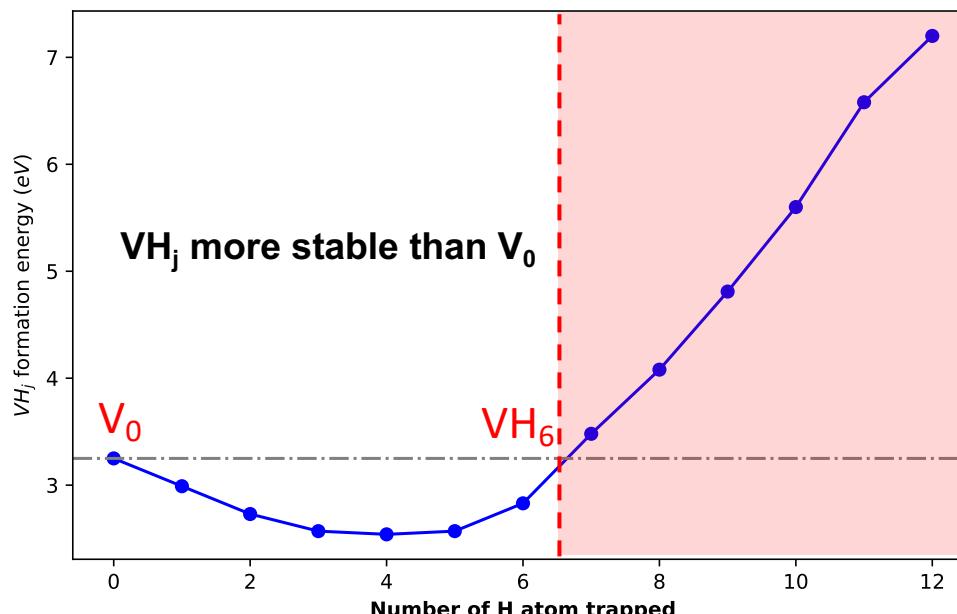
Driving forces for the formation of Super Abundant Vacancies

Sites	Energies (eV)
e_{int}	0.93
e_0	3.25
e_1	2.99
e_2	2.73
e_3	2.57
e_4	2.54
e_5	2.57
e_6	2.83
e_7	3.48
e_8	4.08
e_9	4.81
e_{10}	5.60
e_{11}	6.58
e_{12}	7.20

E. A Hodille et al. PRMat 2 (2018) 093802

SAV in Pd under High pressure

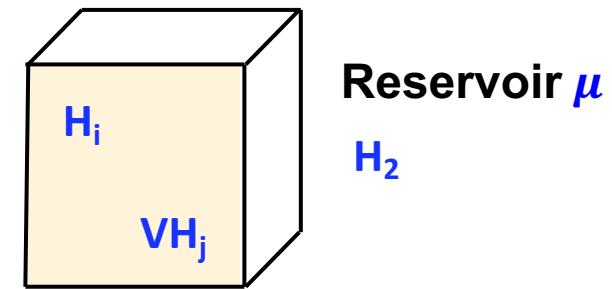
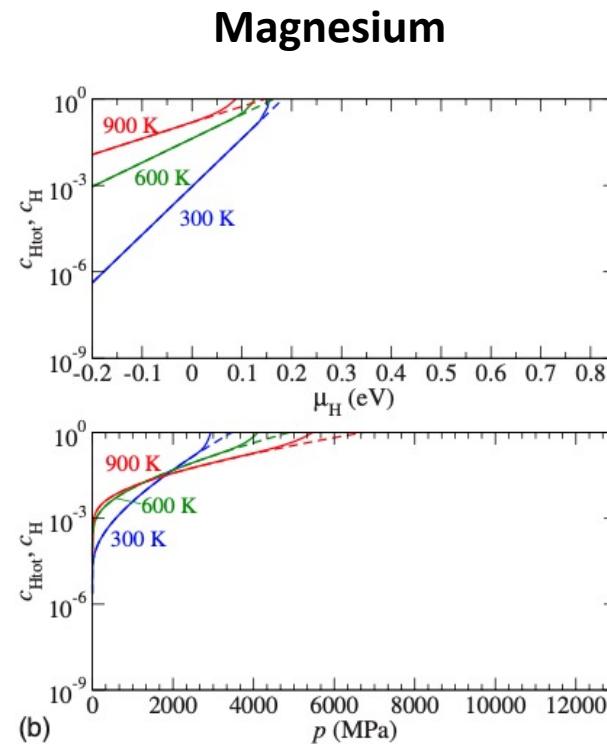
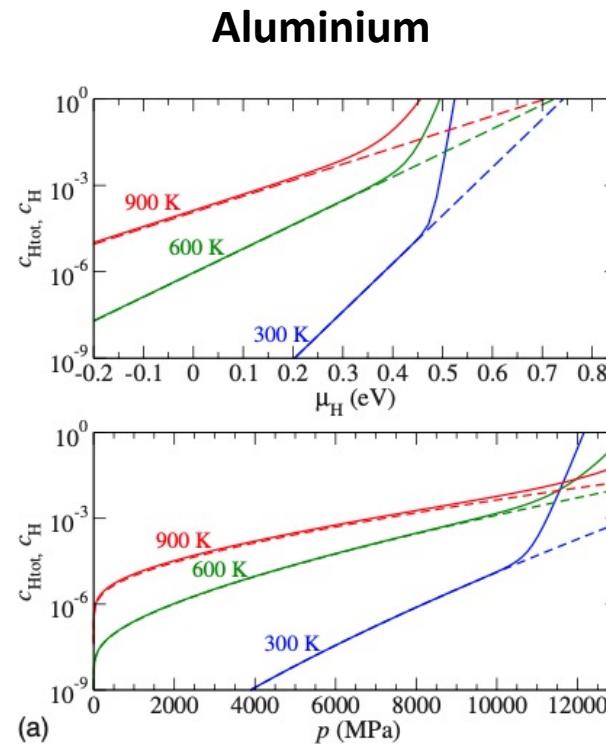
Y. Fukai and N. Okuma, PRL 73 (1994) 1640



Formation energy of VH_j is lower than empty V up to j=6

2. Thermodynamics model for Vacancies

Pioneering works on Mg and Al - Ismer et al. PRB 80 (2009) 184110



Dotted lines x_{H_i}
Bold lines $x_{H_{tot}} = x_{H_i} + \sum_{j=0}^{12} j ; x_{VH_j}$

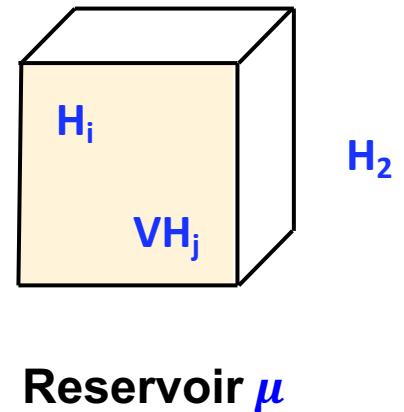
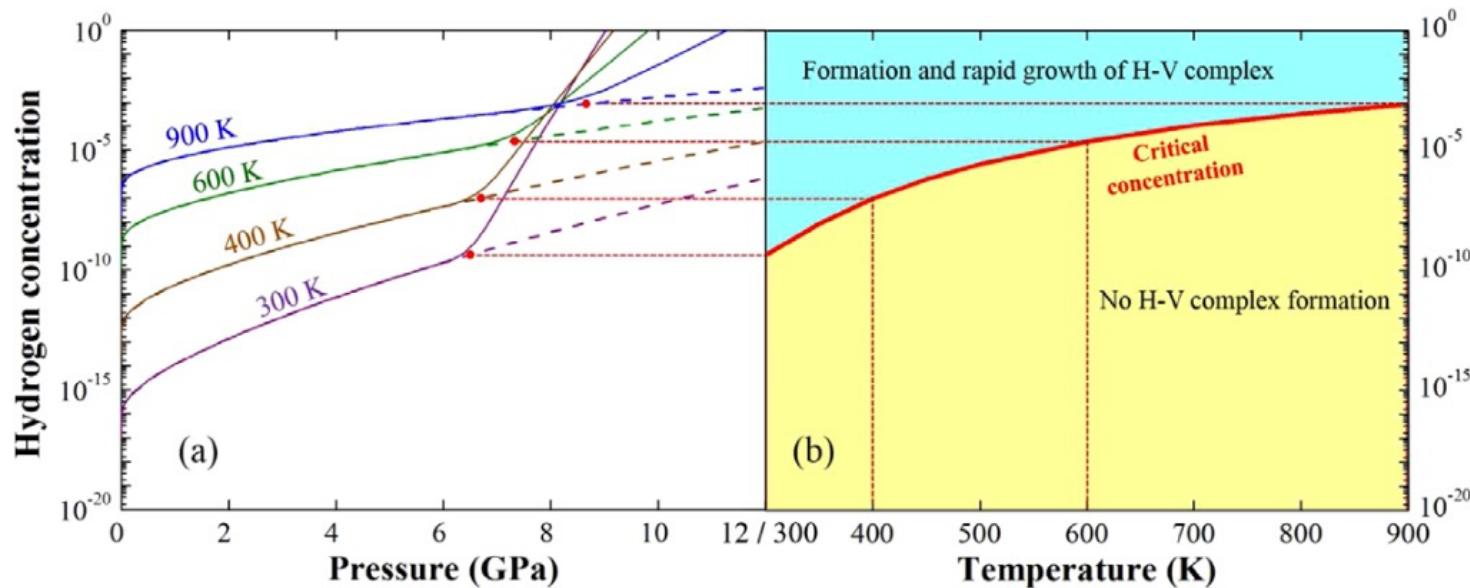
Ismer et al. PRB 80 (2009) 184110

Chemical potential from Sugimoto & Fukai, Acta. Metal. Mater 40 (1992) 2327

2. Thermodynamics model for Vacancies

VH_j formation in W

Lu Sun et al. J. Phys: Condensed Matter 26 (2014) 395402



Dotted lines x_{H_i}

Bold lines $x_{H_{tot}} = x_{H_i} + \sum_{j=0}^{12} j ; x_{VH_j}$

Chemical potential from Sugimoto et Fukai, Acta. Metal. Mater 40 (1992) 2327

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- The model
- Results of the model
- • Chemical potential and flux

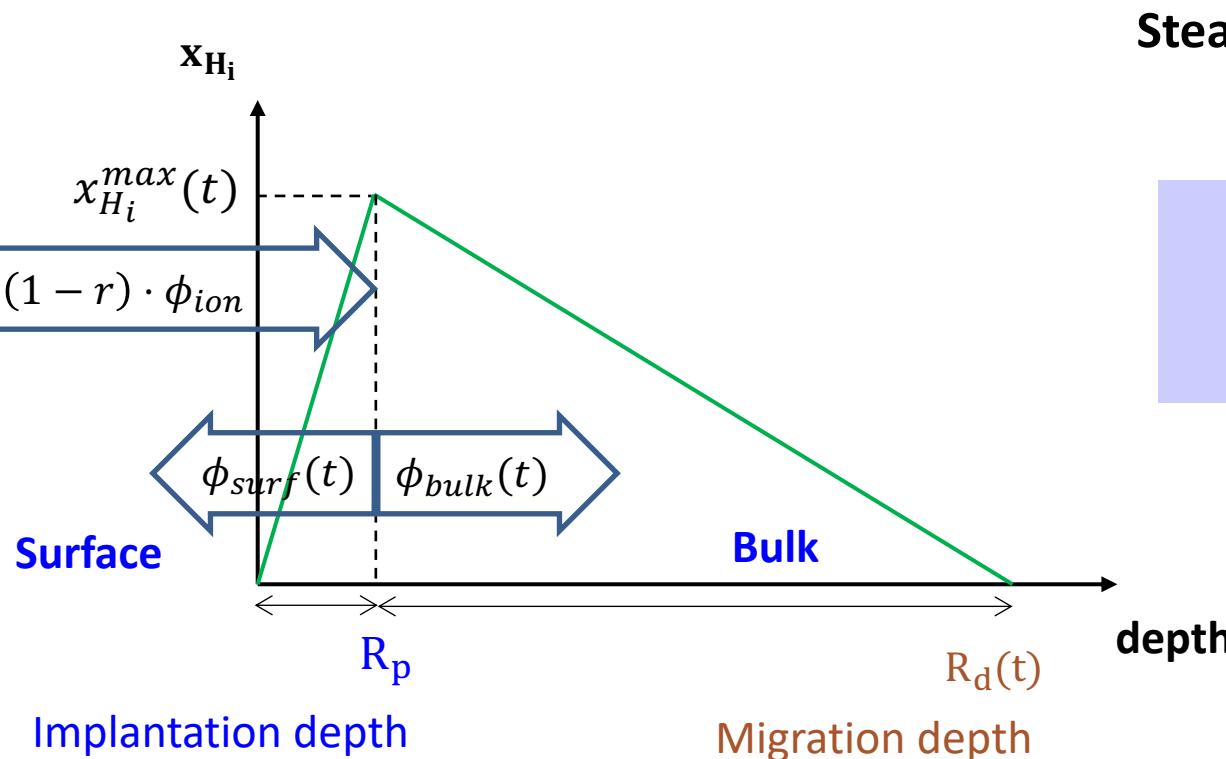
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2. Thermodynamics model for Vacancies

Chemical potential fixed by the flux in the sub-surface

E. A Hodille, N. Fernandez, Z. A. Piazza, M. Ajmalghan, Y. Ferro et al. PRMat 2 (2018) 093802

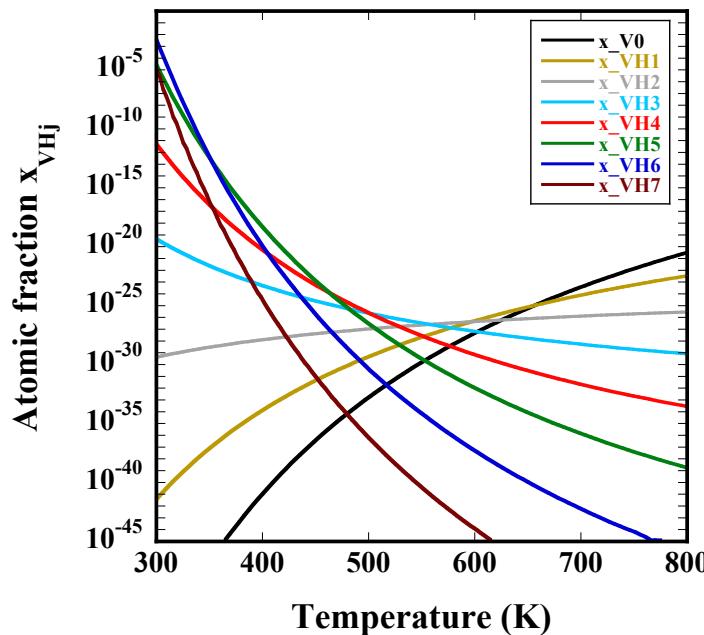


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E. A Hodille, N. Fernandez, Z. A. Piazza, M. Ajmalghan, Y. Ferro et al. PRMat 2 (2018) 093802

Atomic fraction of VH_j vacancies in the 10 nm the sub-surface



Incident flux $\phi_{\text{inc}} = 10^{19} \text{ m}^{-2} \text{s}^{-1}$
Incident ion energy $E_{\text{inc}} = 500 \text{ eV/ion}$.

The flux fixes H_{int} ...

- H_{int} fixes the chemical potential...
- ... and the fraction of VH_j vacancies

$$x_{H_i} = R_p \cdot (1 - r) \cdot \frac{\phi_{\text{ion}}}{\rho_w} \cdot \frac{1}{D(T)}$$

$$x_{H_i}(T) \approx \gamma \exp \left[- \frac{g_{H_i} - \mu}{k_B T} \right]$$

$$x_{VH_j}(T) \approx \omega_j \exp \left[- \frac{g_{VH_j} - j \mu}{k_B T} \right]$$

Vacancy depopulation with increasing temperature

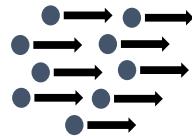
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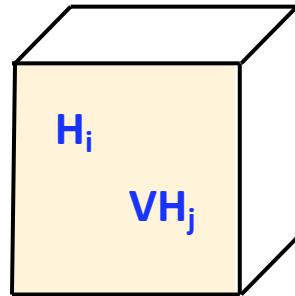
Flux

$$x_{H_i} = R_p \cdot (1 - r) \cdot \frac{\phi_{ion}}{\rho_W} \cdot \frac{1}{D(T)}$$

H/D



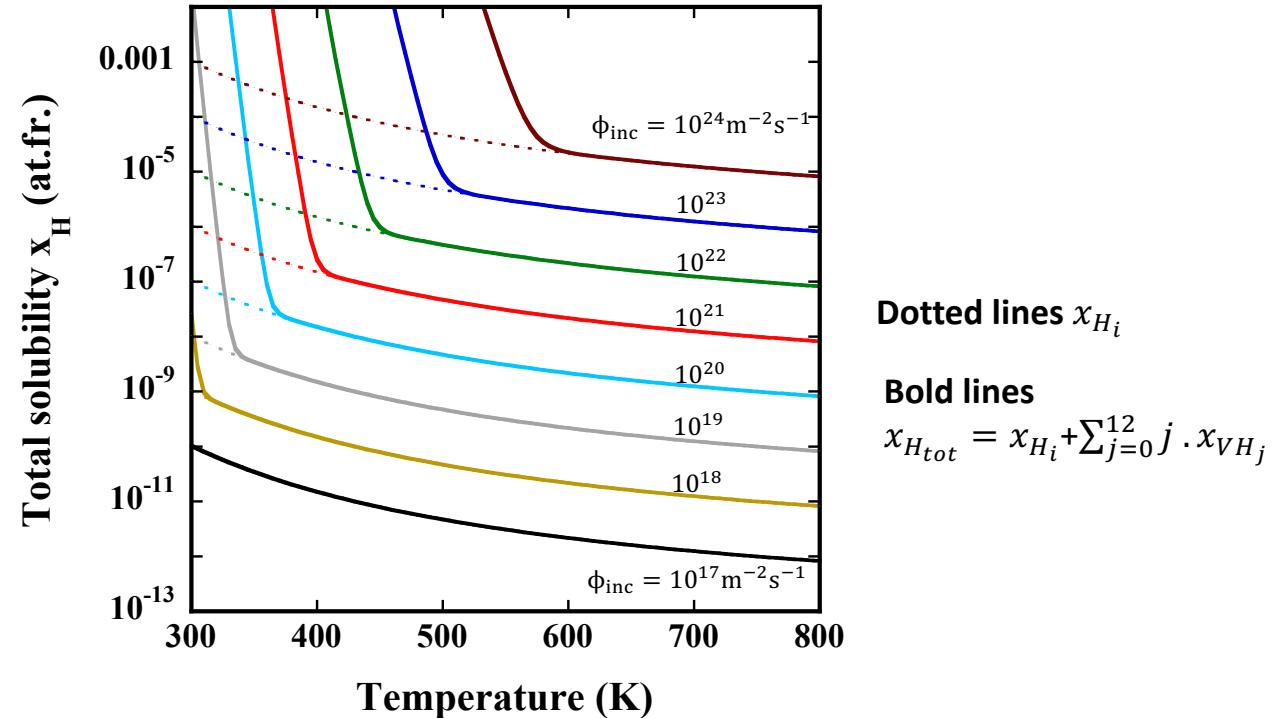
μ



Response of the sub-surface

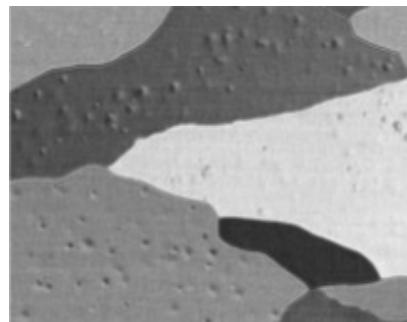
$$x_{H_i}(T) \approx \gamma \exp \left[-\frac{g_{H_i} - \mu}{k_B T} \right]$$

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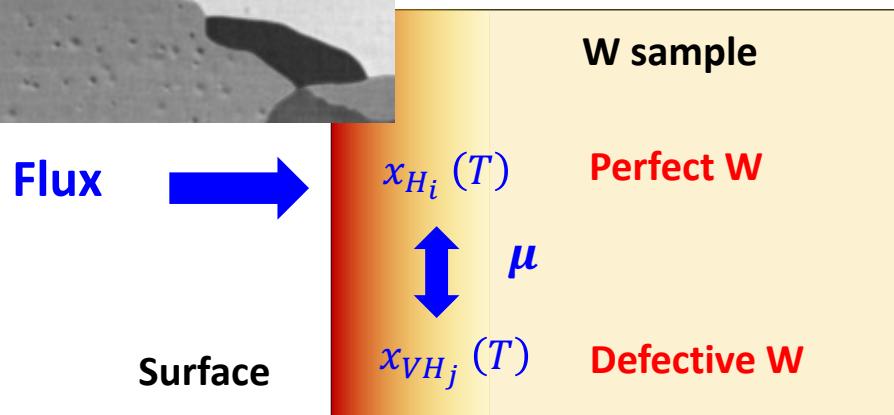


Incident fluxes ranging from $\phi_{inc} = 10^{17} \text{ m}^{-2} \text{s}^{-1}$ to $\phi_{inc} = 10^{24} \text{ m}^{-2} \text{s}^{-1}$
 Incident energy of $E_{inc} = 500 \text{ eV/ion}$.
 The fraction of hydrogen **interstitial** sites is plotted in dotted lines

3 –Super-Abundant Vacancies

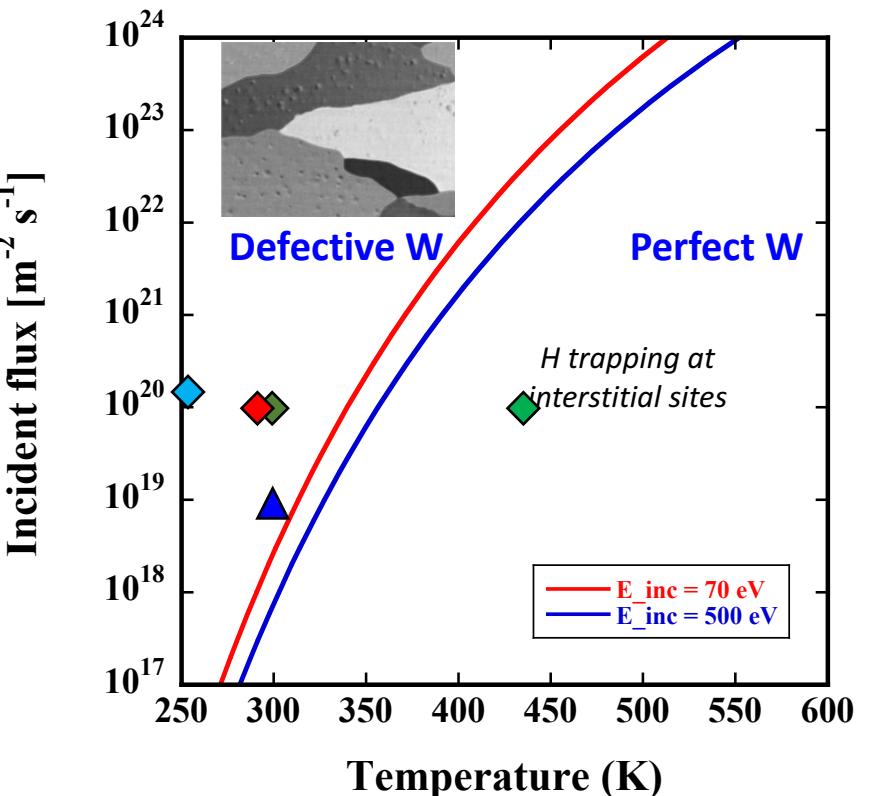


Gao et al., Nucl. Fus. 57 (2017) 016026



No Impact of E_i
Nishijima et al. NF 61 (2021) 116028

Phase Diagram Temp. / Flux



- ◆ No SSL – S. Kapser et al., NF (2018)
- ◆ SSL – A. Manhard et al., NME (2018)
- ◆ SSL – S. Kapser et al., NF (2018)
- ◆ SSL - Gao et al., NF (2017)
- ▲ SSL - Alimov et al., JNM (2005)

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- Super Saturated Layers
- Vacancy Stabilization

4 . Discussion

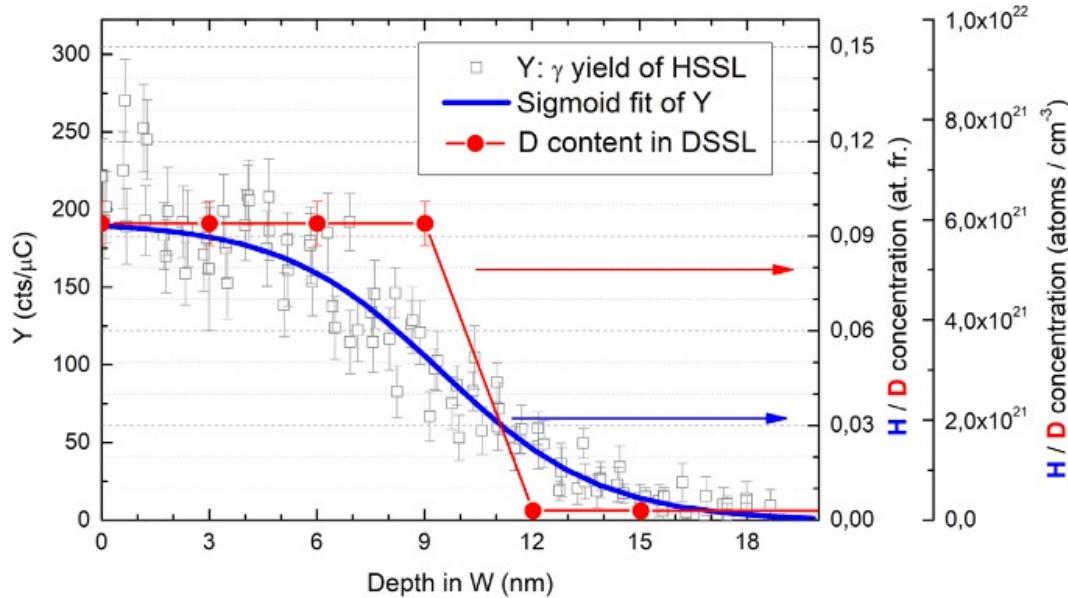
3. Super-Saturation and Vacancy Stabilization

Super-Saturated Layers

SSL forms within 10 nm

215 eV/D+ or 415 eV/H+

5eV/W at., well below 9eV/W at. (displ. Thr.)

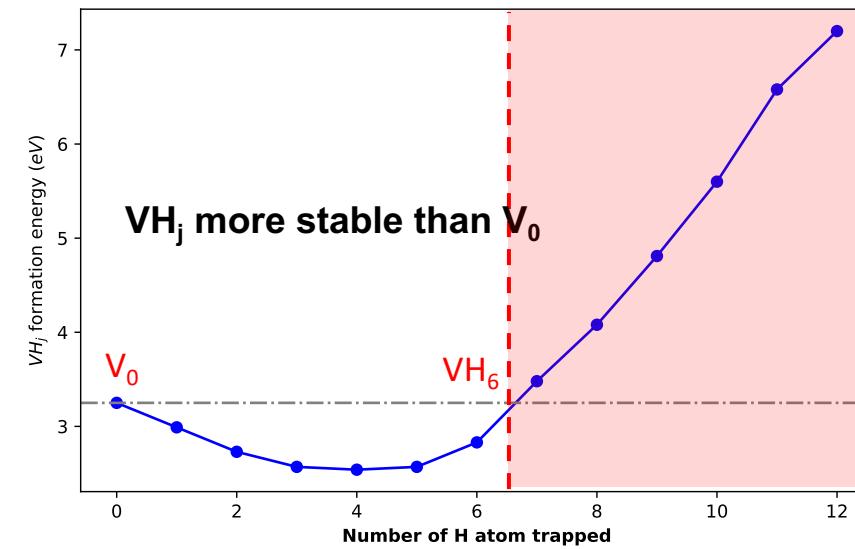


L. Gao et al. NF 57 (2017) 016026

L. Gao et al. Acta. Matter 201 (2020) 55-62

Mechanisms for vacancy stabilization ?

E. A Hodille et al. PRMat 2 (2018) 093802



Hydrogen stabilizes vacancies

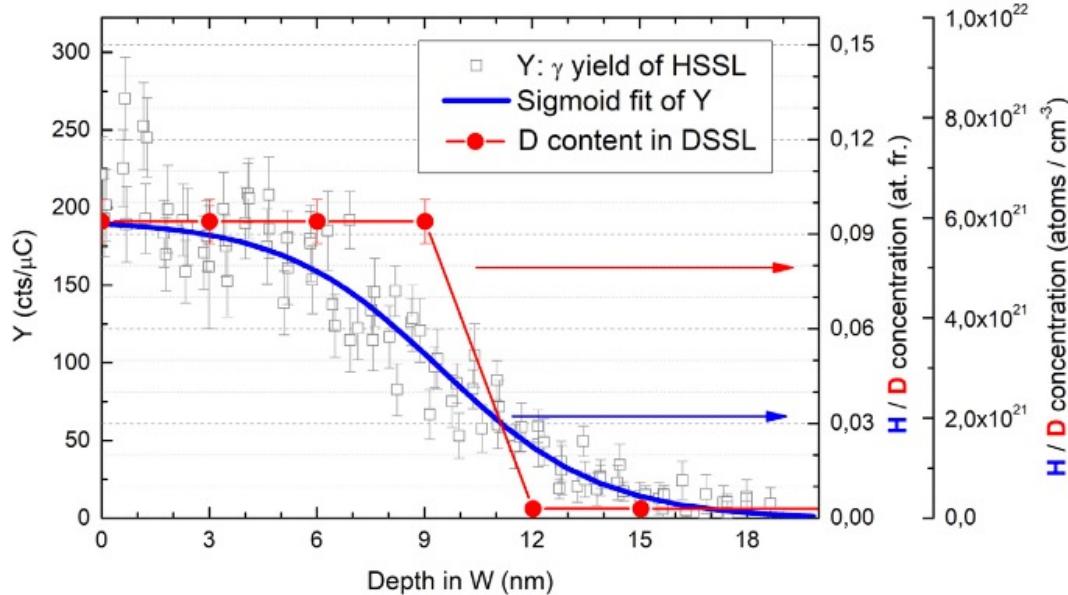
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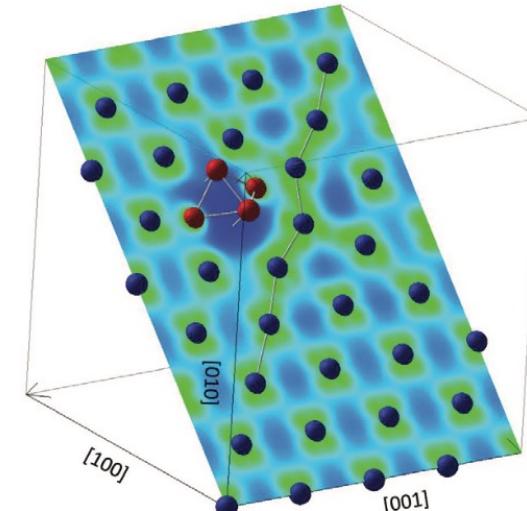
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L. Gao et al. NF 57 (2017) 016026

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Mechanisms for vacancy stabilization ?



$E_f(VH_6+SIA) = 12.1 \text{ eV}$
0.6 eV smaller than $E_f(VH_6) + E_f(SIA)$

Kato et al. NF 55 (2015) 083019

Crowdion-SIA (and others) stabilizes vacancies
Prevent them from recombining

Hydrogen stabilizes vacancies

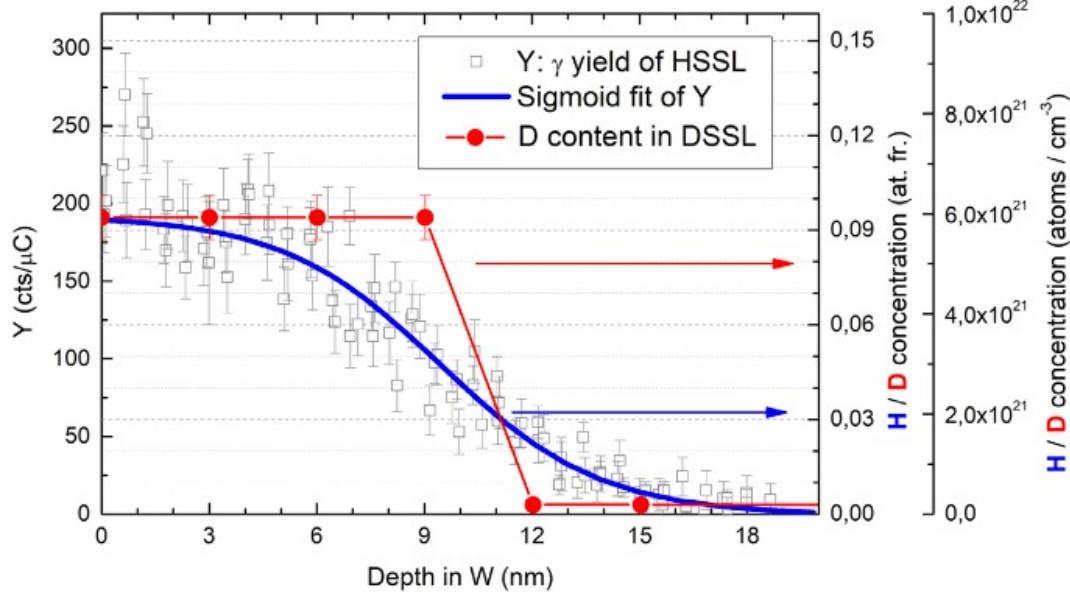
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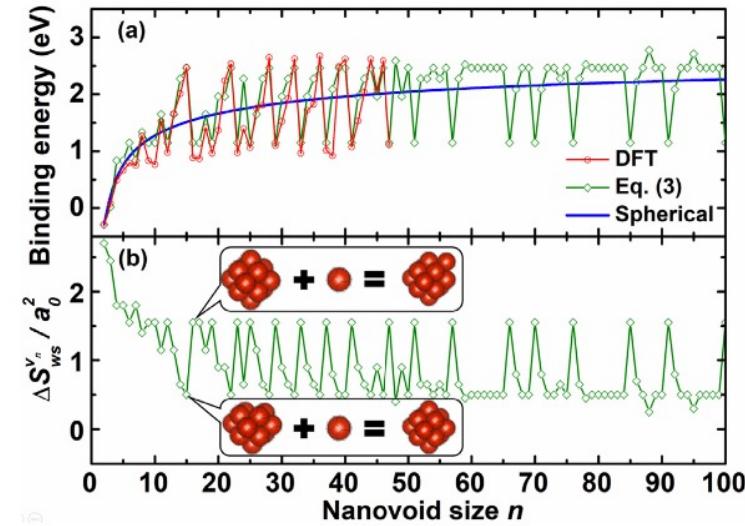
5eV/W at., well below 9eV/W at. (displ. Thr.)



L. Gao et al. NF 57 (2017) 016026

L. Gao et al. Acta Matter 201 (2020) 55-62

Mechanisms for vacancy stabilization ?



J. Hou et al.
Acta Mater 211 (2021) 116860

Binding energy of vacancies increases when vacancies grow

Crowdion-SIA (and others) stabilizes vacancies
Hydrogen stabilizes vacancies

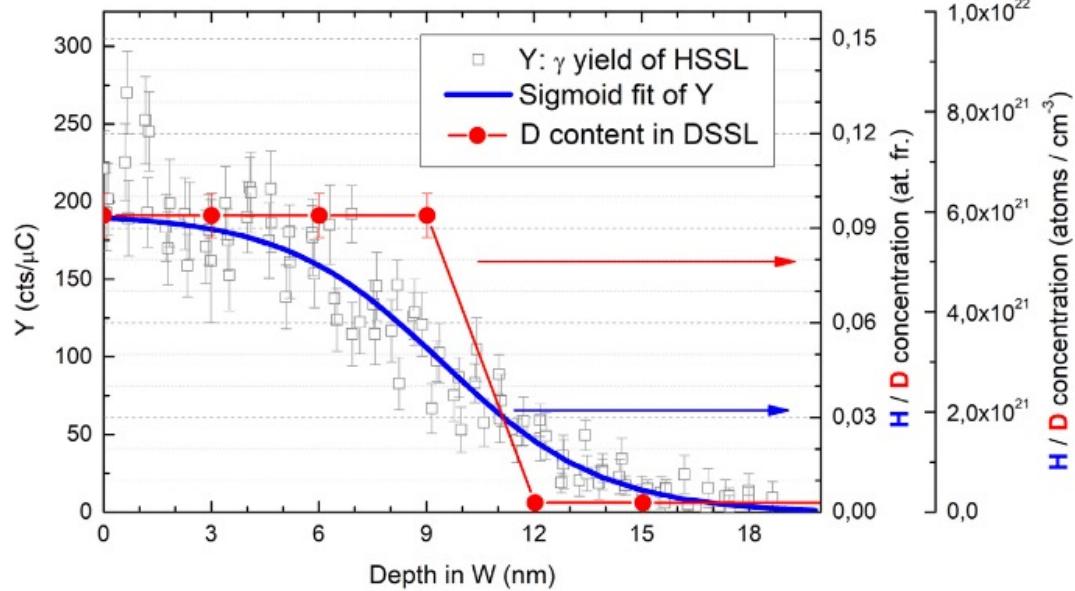
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SSL forms within 10 nm

215 eV/D+ or 415 eV/H+

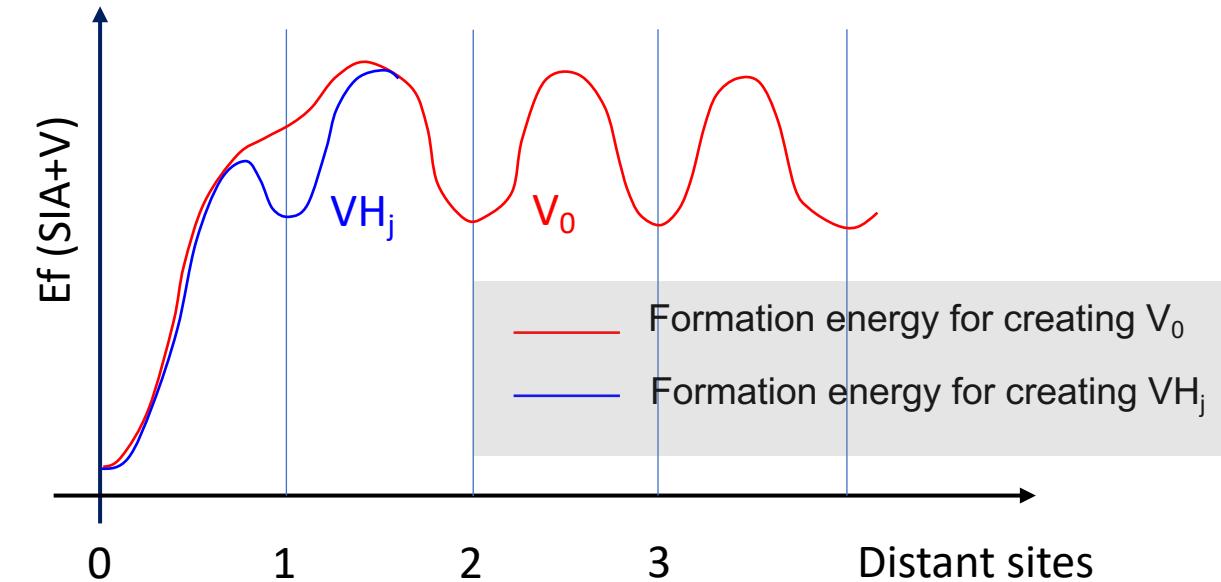
5eV/W at., well below 9eV/W at. (displ. Thr.)



L. Gao et al. NF 57 (2017) 016026

L. Gao et al. Acta. Matter 201 (2020) 55-62

Mechanisms for vacancy stabilization ?



More energy is required to dissociate the Frenkel pair in the absence of Hydrogen

Dynamic of the process ?

Outline

1 . The basic ingredients

2 . Thermodynamic models for vacancies

3 . Supersaturation and vacancy stabilization

- Super Saturated Layers
- Vacancy Stabilization

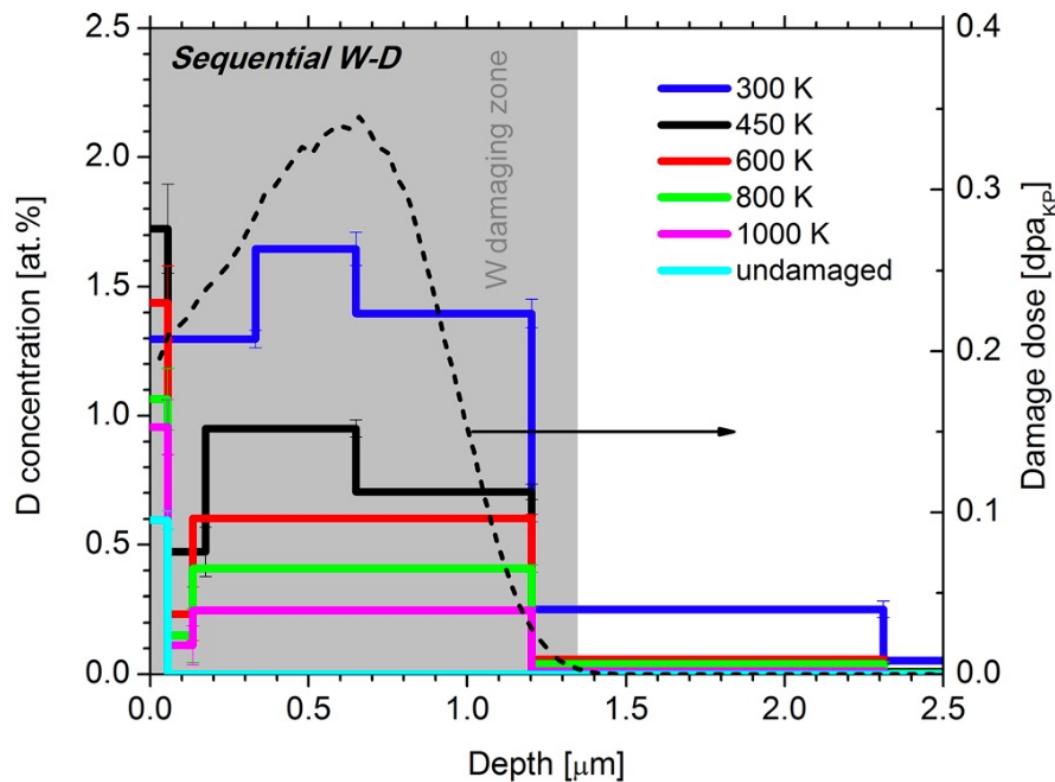


4 . Discussion

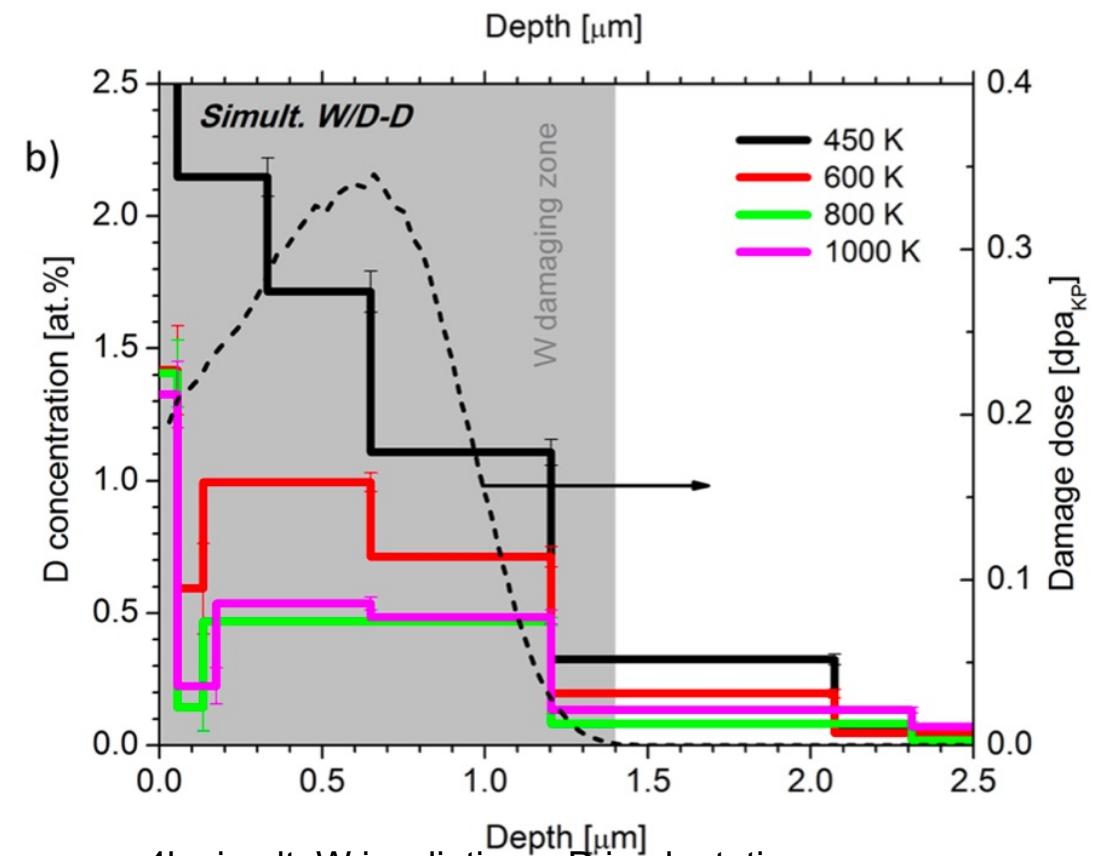
3. Super-Saturation and Vacancy Stabilization

SAV formation in damaged W – Defect Stabilization

M. Markelj et al., 59 (2019) 086050



4h W irradiation followed by 39 h D ions implantation

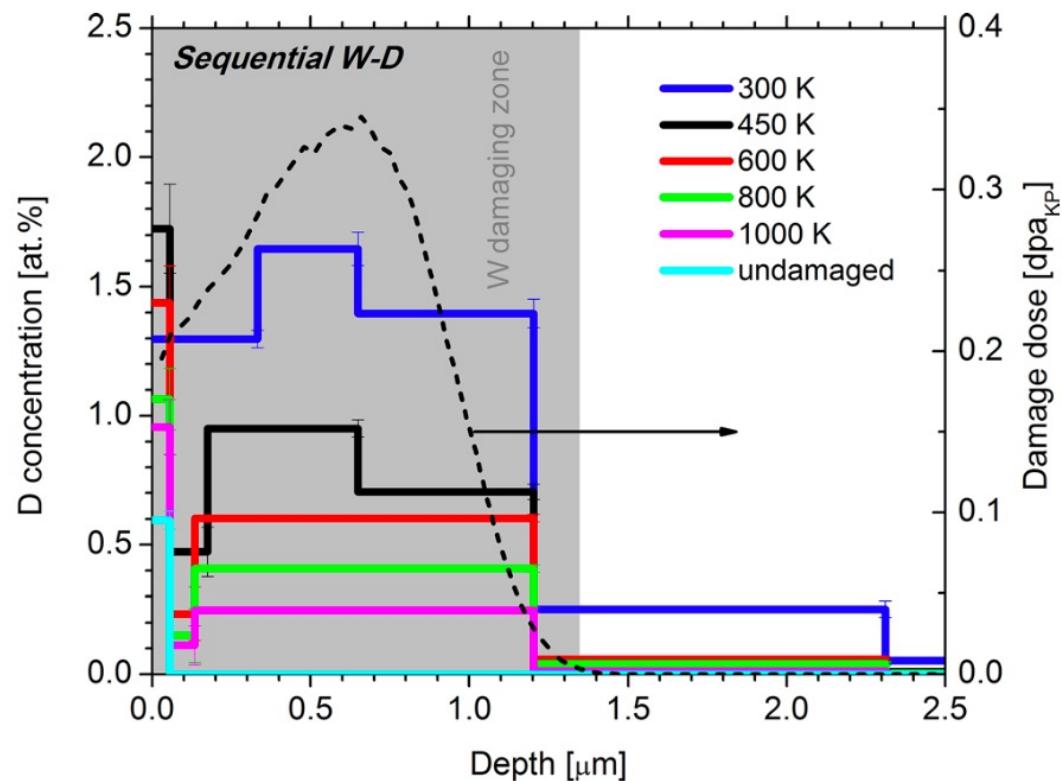


4h simult. W irradiation + D implantation followed by 35 h D ions implantation

3. Super-Saturation and Vacancy Stabilization

SAV formation in damaged W – Defect Stabilization

M. Markelj et al., 59 (2019) 086050



4h W irradiation followed by 39 h D ions implantation

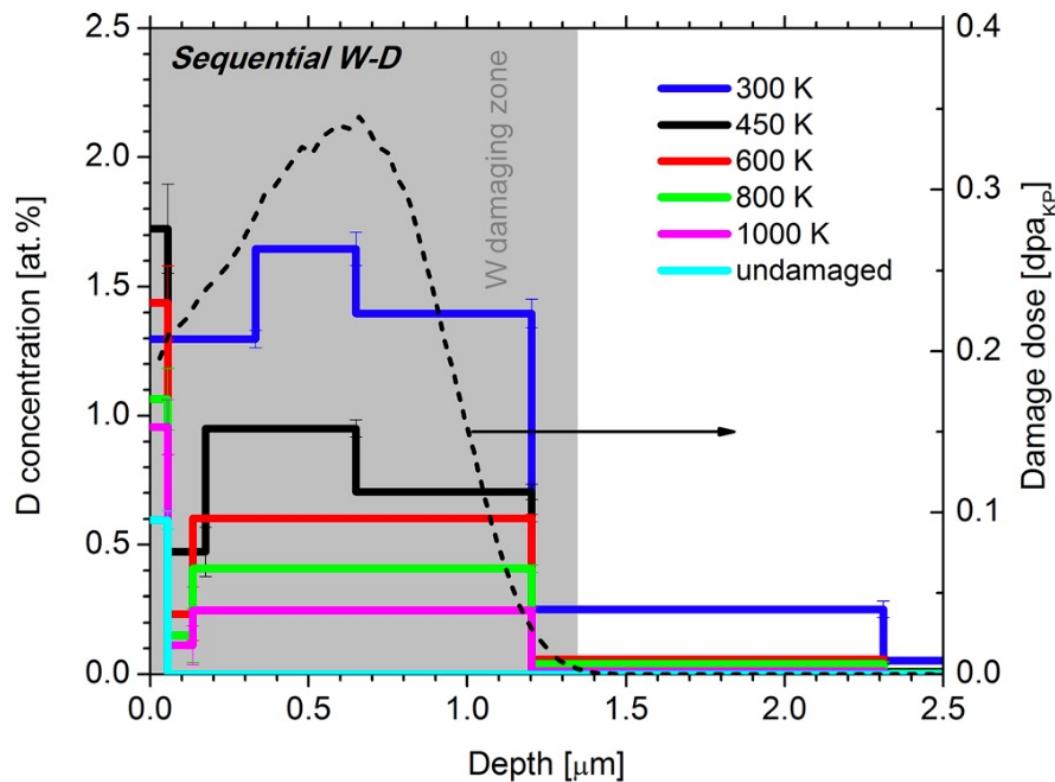
No help from the Thermo. Model

- SSL are formed in the near surface
- Vacancies annihilate with increasing T
→ higher mobility of the atom
- Decoration reveals the V remaining after damaging

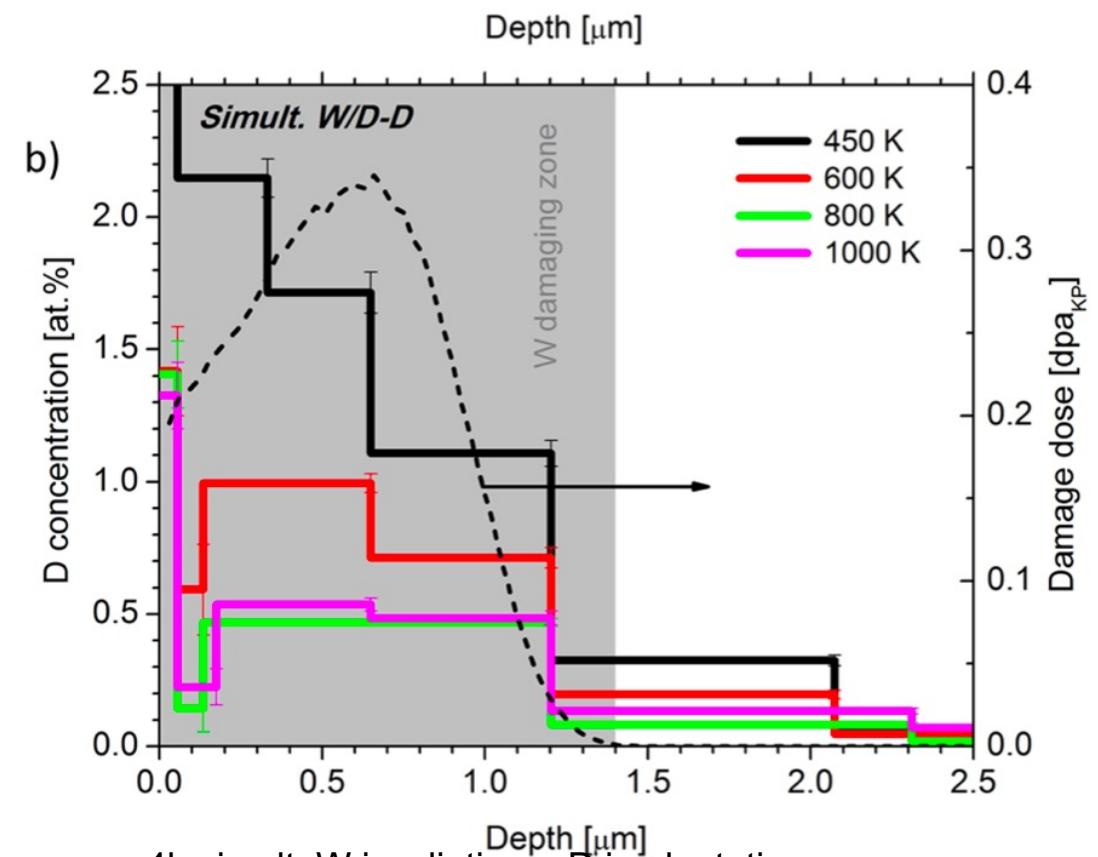
3. Super-Saturation and Vacancy Stabilization

SAV formation in damaged W – Defect Stabilization

M. Markelj et al., 59 (2019) 086050

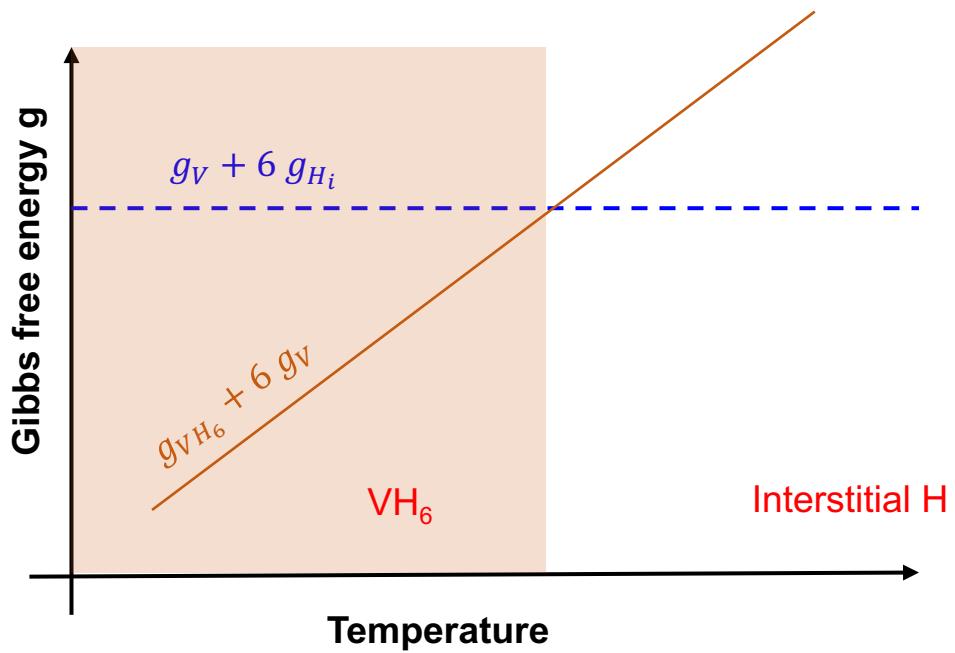


4h W irradiation followed by 39 h D ions implantation



3. Super-Saturation and Vacancy Stabilization

SAV formation in damaged W – Defect Stabilization



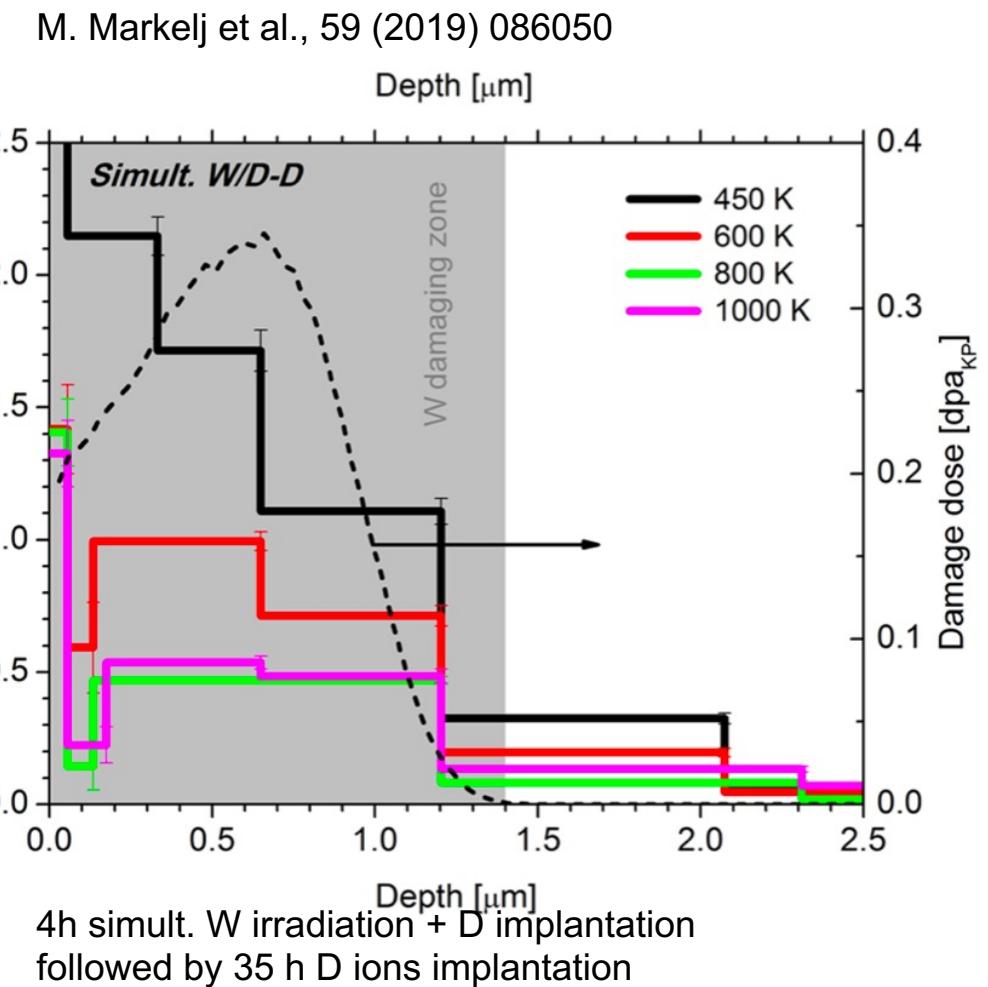
Toward VH_6 eq. during D imp. + W damage

Fluence not enough for reaching eq.

→ The near surface is more populated

After W damage, created V not filled are reveal

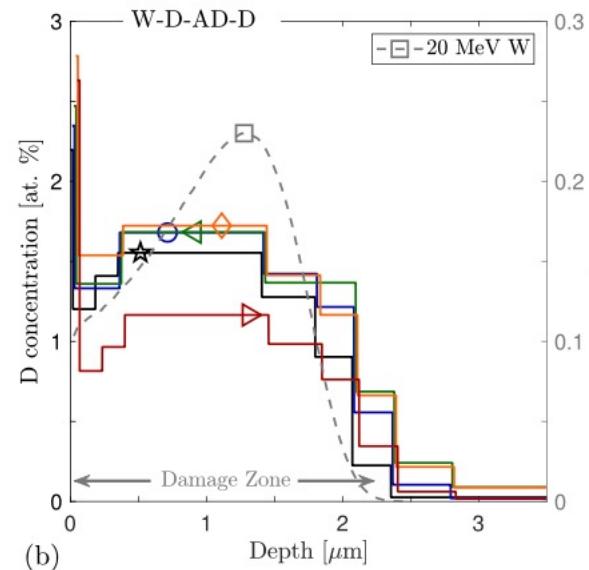
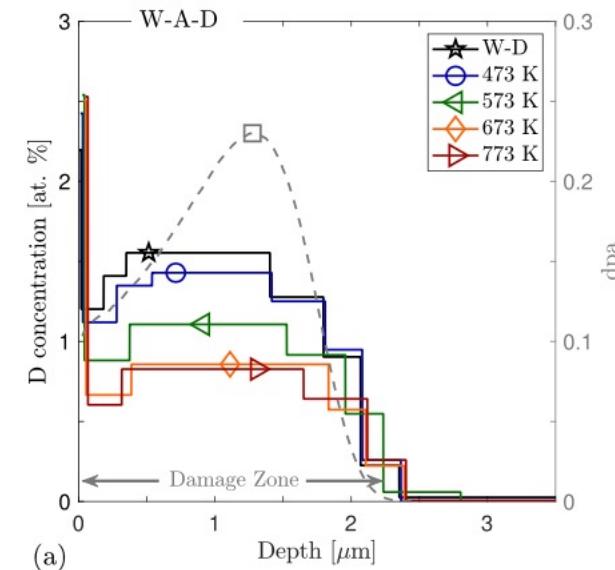
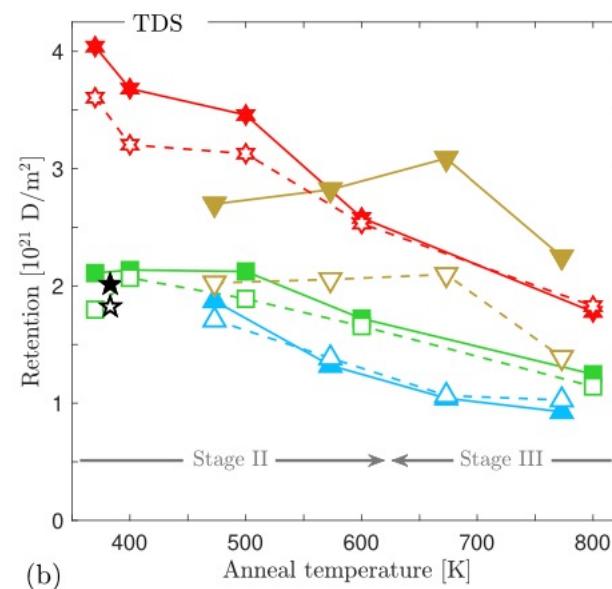
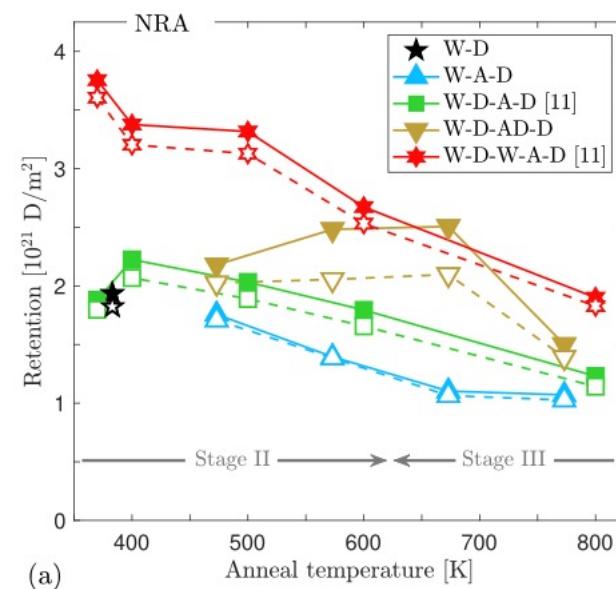
With temperature, mechanism for V stab less and less efficient



3. Super-Saturation and Vacancy Stabilization

SAV formation in damaged W – Defect Stabilization

M. Simmonds et al., 59 (2019) 086050



Complies with the Thermo model

To be discussed ...

Outline

1 . The basic ingredients

2 . Thermodynamic models for vacancies

3 . Supersaturation and vacancy stabilization

4 . Discussion

4. Discussion

- Mechanisms for SSL formation and V stab are probably the same
- H in V would stabilize a V and prevent it to recombines with SIA
- Thermal V are created at the surface. W atoms bring enough energy to create additional vacancies that would be stabilized with H. No need for collision cascade and Frankel pairs.
- The stress around VHj should be at shorter distance than around V. In addition, VHj is much less mobile the V. The cross section for VHj+SIA recombination is smaller than V + SIA.
- SSL are formed in other metals like Mo, Fe, steel, not Cu that display higher Ef for V creation
- Hy SSL are formed at T=800K. Is it because of the flux that bring μ so high ?

Thanks for your attention ...

... and sorry for being that long.

