#### Non-local real-space diffusion-driven models for microstructural evolution of irradiated tungsten.

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Francesco Ferroni, Xiaoou Yi, Kazuto Arakawa *et al.*, High temperature annealing of ion irradiated tungsten, Acta Mater. **90** (2015) 380–393





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Francesco Ferroni, Xiaoou Yi, Kazuto Arakawa *et al.*, High temperature annealing of ion irradiated tungsten, Acta Mater. **90** (2015) 380–393





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Francesco Ferroni, Xiaoou Yi, Kazuto Arakawa *et al.*, High temperature annealing of ion irradiated tungsten, Acta Mater. **90** (2015) 380–393. The movie shows the dynamics of recovery of defects in tungsten at 1100°C.





## OUTLINE

- 1. Production of defects in collision cascades in tungsten.
- 2. High and low-temperature mobility of radiation defects.
- 3. Diffusion-mediated models for microstructural evolution:
  - 1. Self-diffusion of dislocations
  - 2. Vacancy-diffusion-mediated evolution
- 4. Anomalous phase decomposition of W-Re alloys





#### Defect production in tungsten



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#### Defect production: fundamentals

- 1. Given arbitrarily high energy of the initial ion/neutron impact, is it possible to produce a defect cluster of arbitrarily large size directly in a cascade event?
- 2. The "dark matter" question: how many defects produced in cascades remain invisible to transmission electron microscopy and other high-resolution methods, and what is their effect on microstructure?

A.E. Sand *et al.* EPL **103** (2013) 46003; D.R. Mason *et al.*, JPCM **26** (2014) 375701; X. Yi *et a*l., EPL, **110** (2015) 36001; J. Marian *et al.*, Nuclear Fusion **57** (2017) 092008





#### Defect production in tungsten

Average interstitial cluster distributions: cascades at 100 K Fraction of interstitials in cluster size 0.5 100 K, 10 keV 50 keV 22222 4 Clusters of defects formed in iron in high 0.3 energy cascades 0.2 0.1 0 9 10 2 3 5 ≥11 Number of interstitials in cluster R.E. Stoller (2012) in: Comprehensive Nuclear Materials

Prior to 1991 it was assumed that defects were produced as Frenkel pairs (individual vacancies and self-interstitials). C.H. Woo and B.N. Singh (1991) noted that clustering of defects in collision cascades may have a significant effect on the evolution of radiationinduced microstructure. Similar findings were reported derived from MD simulations.

T. Diaz de la Rubia, M.W. Guinan, PRL **66** (1991) 2766; C.H. Woo, B.N. Singh, Phil. Mag. **65** (1992) 889-912

thority



Distribution of defect cluster sizes follows a power law

$$F(n) = \frac{A}{n^{s}}; n < n^{*} \approx 600$$
$$A \approx 7.45; S = 1.63$$

A.E. Sand et al., EPL 103 (2013) 46003



#### Power law of defect clustering





Energy

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#### Temperature dependence of defect production



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#### Comparison to experiment: loop sizes



Explaining experimental observations require taking into account interaction between the defects. Fewer but larger defects remain in the material at higher temperatures. Experimental data correspond to the low dose limit (0.01 dpa) where cascades do not overlap. Simulated distributions correspond to t=1 s.



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on D.R. Mason *et al.*, JPCM 26 (2014) 375701; J. Marian *et al.*, Nuclear Fusion 57 (2017) 092008



A 150 keV cascade in tungsten, Derlet - Nguyen-Manh - Dudarev interatomic potential

Modelling the evolution of complex cascade configurations still remains one of the most challenging topics in the treatment of radiation damage phenomena.

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#### Diffusion of defects: vacancies

	Al	Cu	Au	Ni	Pd	Pt	Pu
$E_f$	$0.580^{i}$	1.04 <sup>d</sup>	$0.782^{i}$	1.37, <sup>e</sup> 1.43, <sup>r</sup>	1.70 <sup>j</sup>	1.18 <sup>j</sup>	1.31, 1.36, 1.08 <sup>t</sup>
				1.65 <sup>r</sup>			
$E_m$	0.57 <sup>m</sup>	0.72 <sup>d</sup>	_	1.285, <sup>e</sup> 1.08 <sup>r</sup>	—	1.51 <sup>j</sup>	_
	V	Nb	Ta	Cr	Мо	W	Fe
$E_f$	$2.51^{1}$	2.99 <sup>1</sup>	3.14 <sup>1</sup>	2.64 <sup>1</sup>	2.96, <sup>j</sup> 2.96 <sup>l</sup>	3.56 <sup>1</sup>	2.02, <sup>b</sup> 2.07, <sup>k</sup> 2.15 <sup>l</sup>
$E_m$	0.62 <sup>1</sup>	0.91 <sup>1</sup>	1.48 <sup>1</sup>	0.91 <sup>1</sup>	1.28 <sup>1</sup>	$1.78^{l}$	0.65, <sup>b</sup> 0.67, <sup>k</sup> 0.64 <sup>l</sup>
	С	Si	Ge	Be	Ti	Zr	Hf
$E_{f}$	8.2 <sup>f</sup>	3.17, <sup>c</sup> 3.29 <sup>g</sup>	2.3 <sup>h</sup>	0.81, <sup>n</sup> 1.09 <sup>o</sup>	1.97, <sup>p</sup> 2.13 <sup>q</sup>	2.17, <sup>q</sup> 1.86 <sup>s</sup>	2.22 <sup>q</sup>
$E_m$	$1.7^{\mathrm{f}}$	0.4 <sup>g</sup>	_	0.72B,	0.47B,	0.51B,	0.79B, 0.91NB <sup>q</sup>
				0.89NB <sup>o</sup>	0.61NB <sup>p</sup>	$0.67 \mathrm{NB}^{\mathrm{q}}$	

It is possible, by means of a DFT calculation, to accurately predict vacancy migration and formation energies in a variety of materials, even where there are no experimental data available. Values derived from DFT calculations are free from impurity effects. It is possible to determine the strength of interaction between vacancies and impurities, also by means of a DFT calculation.



Annual Review of Materials Research 43 (2013) 35-61



### Diffusion of defects: self-interstitials

	(111)	(110)	(100)	Tetrahedral	Octahedral	$E_m$
Fe	4.66, <sup>b</sup> 4.45 <sup>c</sup>	3.94, <sup>b</sup> 3.75 <sup>c</sup>	5.04, <sup>b</sup> 4.75 <sup>c</sup>	4.26 <sup>c</sup>	4.94 <sup>c</sup>	0.34 <sup>c</sup>
V	3.37, <sup>d</sup> 3.14 <sup>e</sup>	3.65, <sup>d</sup> 3.48 <sup>e</sup>	3.92, <sup>d</sup> 3.57 <sup>e</sup>	3.84, <sup>d</sup> 3.69 <sup>e</sup>	3.96, <sup>d</sup> 3.62 <sup>e</sup>	
Nb	5.25 <sup>d</sup>	5.60 <sup>d</sup>	5.95 <sup>d</sup>	5.76 <sup>d</sup>	6.06 <sup>d</sup>	
Ta	5.83 <sup>d</sup>	6.38 <sup>d</sup>	7.00 <sup>d</sup>	6.77 <sup>d</sup>	7.10 <sup>d</sup>	
Cr	5.66 <sup>d</sup>	5.68 <sup>d</sup>	6.64 <sup>d</sup>	6.19 <sup>d</sup>	6.72 <sup>d</sup>	
Mo	7.42, <sup>d</sup> 7.34 <sup>e</sup>	7.58, <sup>d</sup> 7.51 <sup>e</sup>	9.00, <sup>d</sup> 8.77 <sup>e</sup>	8.40, <sup>d</sup> 8.20 <sup>e</sup>	9.07, <sup>d</sup> 8.86 <sup>e</sup>	
W	9.55 <sup>d</sup>	9.84 <sup>d</sup>	11.49 <sup>d</sup>	11.05 <sup>d</sup>	11.68 <sup>d</sup>	
Al	1.959 <sup>f</sup>	1.869 <sup>f</sup>	1.579 <sup>f</sup>	1.790 <sup>f</sup>	1.978 <sup>f</sup>	0.084 <sup>f</sup>
Ni	4.69 <sup>g</sup>	4.99 <sup>g</sup>	4.07 <sup>g</sup>	4.69 <sup>g</sup>	4.25 <sup>g</sup>	0.14 <sup>g</sup>
Si	3.84 <sup>h</sup>	3.80 (hexagonal)	3.85 (caged)	4.07 <sup>h</sup>	4.8	0.18 <sup>h</sup>

DFT calculations prove particularly useful in the treatment of self-interstitial atom (SIA) defects. The formation energies of SIA defects are much larger than the formation energies of vacancies, and SIAs do not form thermally at temperatures below 1000°C. SIAs do form under irradiation (a Frenkel pair = a vacancy + a SIA), making DFT an essential tool for modelling radiation damage phenomena. Values in blue boxes refer to the lowest energy most stable configurations.



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#### Diffusion of self-interstitial defects in tungsten.



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TABLE I. Fitted parameters and derived quantities for the metals of groups V and VI. Also given are the estimated migration temperatures  $T_m$  in kelvin, and their experimental values taken from Ref. [2].

Metal	$V_0$ (eV)	$\beta$ (eV/ $a^2$ )	α	$\mu$	$T_m$ est.	$T_m$ [2]
V	0.689	41.1	1.31	0.575	$\sim 8$	<6
Nb	0.835	69.1	1.41	0.488	$\sim 0.3$	$<\!\!6$
Ta	0.940	81.6	1.36	0.477	$\sim 0.1$	$<\!\!6$
Cr	1.03	63.1	1.73	0.568	$\sim 100$	$\sim 40$
Mo	1.41	130	1.66	0.463	$\sim 30$	35
W	1.90	177	1.64	0.460	$\sim \! 30$	27

S.P. Fitzgerald and D. Nguyen-Manh, PRL **101** (2008) 115504



Potential barrier for migration of self-interstitial defects can be estimated analytically by fitting parameters of the Frenkel-Kontorova model to DFT data.

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Diffusion of self-interstitial defects in tungsten.





Interatomic potentials calculations show that the potential barrier for the diffusion of self-interstitial atom defects in tungsten is of the order of 0.017 eV. DFT calculations suggest that the barrier for migration may be even lower, of the order of 0.002 eV. This has implications for diffusion of defects at low temperatures.

#### Diffusion of defects



Left: diffusion of a self-interstitial dislocation loop in Fe at 500K, classical molecular dynamics simulations, energy filtering has been applied. Right: diffusion of a single self-interstitial defect in tungsten at 300K, full lattice view.





#### Diffusion of defects at very low temperatures.



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New J. Phys. (2017) in press

#### Diffusion of defects at very low temperatures.



Due to an exceptionally low defect migration barrier, interstitial defects exhibit very high diffusivity of order  $10^3 \,\mu m^2 s^{-1}$  over the entire range of temperatures from 10 K to 300K.

The origin of high diffusivity is the same as that of zero atomic vibrations, well visible in diffraction experiments as non-zero Debye-Waller factors. No tunnelling is involved, as defects remain heavy classical particles at all temperatures above 1K.











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#### Self-climb of dislocations

#### The Coalescence of Dislocation Loops by Self Climb

By J. A. TURNBULL

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Illustration of the geometry used in § 3.3 when considering the vacancy flux in the segment of pipe PQ on loop B.

Turnbull (1970) showed that interacting dislocation loops coalesce as a result of migration, at loop perimeters, of <u>virtual</u> vacancy-interstitial pairs formed due to thermal fluctuations. No <u>real</u> defects are formed in this process. Loops drift towards each other in the negative direction of gradient dE/dx of elastic interaction energy.





#### Self-climb of dislocations



Dislocation self-climb occurs due to diffusion around the perimeter of dislocation loops, independent of the vacancy atmosphere. At relatively low temperatures this vacancy-free climb is much faster than conventional vacancy-diffusion-mediated climb.







#### Real space models for microstructure

Three-dimensional formulation of dislocation climb

Yejun Gu<sup>a</sup>, Yang Xiang<sup>b,\*</sup>, Siu Sin Quek<sup>c</sup>, David J. Srolovitz<sup>d,e</sup> Journal of the Mechanics and Physics of Solids 83 (2015) 319–337



$$\frac{\partial c(\mathbf{x},t)}{\partial t} = -\Omega \nabla J(\mathbf{x},t) - \Omega I(\mathbf{x},t) \delta(\Gamma)$$
$$J(\mathbf{x},t) = -\frac{D_{v}c(\mathbf{x},t)}{\Omega k_{B}T} \nabla \mu_{v}(\mathbf{x},t)$$

Here  $\Gamma$  defines a dislocation line, so that  $\int \delta[\Gamma] f(\mathbf{x}) d^3 x = \int_{\Gamma} f(\mathbf{x}) ds$ .

In the dilute gas approximation for the chemical potential of vacancies, we arrive at the boundary value problem for a moving dislocation line. A dislocation line moves due to elastic forces acting on it, which stimulate absorption or emission of vacancies:

$$\mu_{v}(\mathbf{x},t) = k_{B}T \ln c(\mathbf{x},t); \qquad \qquad D_{v}\nabla^{2}c = b_{e}v_{cl}\delta(\Gamma)$$
$$c(|\mathbf{x}| \to \infty) = c_{\infty}$$





#### Real space models for microstructure

Three-dimensional formulation of dislocation climb

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The central step is the conversion of the boundary value problem into an integral equation

$$c(\mathbf{x}) = \frac{1}{4\pi D_{\nu}} \oint_{\Gamma} \frac{\mathbf{b} \cdot (\mathbf{v} \times d \mathbf{l}')}{|\mathbf{x} - \mathbf{x}'|} + c_{\infty}.$$

Assume that a dislocation line forms a closed loop. At large distances from the loop, where  $|\mathbf{x}-\mathbf{x}'|$ >> loop size, this equation acquires a simple form:

$$c(\mathbf{x}) \approx \frac{1}{4\pi D_{v} |\mathbf{x}|} \oint_{\Gamma} \mathbf{b} \cdot (\mathbf{v} \times d \mathbf{l}') + c_{\infty}.$$

Here

$$\mathbf{b} \cdot (\mathbf{v} \times d\mathbf{l}') = \frac{d\Omega_{rel}}{dt}$$
, and  $\Omega_{rel}(t)$  is the volume of the dislocation loop.





#### Relaxation volume of a dislocation loop



Molecular dynamics simulation of thermal Brownian motion of a  $\frac{1}{2}(111)$  dislocation loop in iron at 500K.



$$\frac{d\Omega_{rel}}{dt} = \frac{d}{dt} (\mathbf{b} \cdot \mathbf{A}(t)) = 0.$$

Formula for the relaxation volume of a dislocation loop  $\Omega_{\it rel}(t) = ({\bf b} \cdot {\bf A}(t))$ 

shows that the volume of a loop remains constant even though the direction and magnitude of the loop vector area changes. <u>Left</u>: simulation of Brownian motion of a dislocation loop in Fe. <u>Below</u>: experimental observation of Brownian motion of a dislocation loop, courtesy of Prof. K. Arakawa.



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#### Real space models for microstructure

The field of vacancies changes adiabatically, following the evolution of dislocation loops (centres of loops are at  $\mathbf{X}_i$ )

$$c(\mathbf{x}) \approx c_{\infty} + \frac{1}{4\pi D_{v}} \sum_{i} \frac{1}{|\mathbf{x} - \mathbf{x}_{i}|} \frac{d\Omega_{rel}^{i}}{dt}$$

Volume  $\Omega_{rel}$  of a dislocation loop with Burgers vector  $\mathbf{b}$  and area vector  $\mathbf{A}$  is given by the scalar product  $(\mathbf{b} \cdot \mathbf{A})$ . Volume is positive for an interstitial loop and negative for a vacancy loop.



Above equations for  $c(\mathbf{x})$  can also be formulated as a set of ODEs for the velocities of nodal points on dislocation lines.



#### Diffusion to/from surfaces

The computational efficiency of the treatment developed by Y. Gu, Y. Xiang *et al.*, JMPS (2015) is fundamentally due to the use of "free-space" Green's function

$$G_0(\mathbf{x},\mathbf{x}') = -\frac{1}{4\pi D_v |\mathbf{x}-\mathbf{x}'|}.$$

This computational advantage is lost if, in order to take into account the boundary conditions, we attempt to modify these Green's functions. An alternative approach is the Kirchhoff integral approximation, which retains the use of <u>free</u> Green's functions



$$\int_{V} dV \left[ \Phi_{a}(\mathbf{x}) \frac{\partial^{2} \Phi_{b}(\mathbf{x})}{\partial \mathbf{x}^{2}} - \Phi_{b}(\mathbf{x}) \frac{\partial^{2} \Phi_{a}(\mathbf{x})}{\partial \mathbf{x}^{2}} \right]$$
$$= \int_{S} d\mathbf{S} \left[ \Phi_{a}(\mathbf{x}) \frac{\partial \Phi_{b}(\mathbf{x})}{\partial \mathbf{x}} - \Phi_{b}(\mathbf{x}) \frac{\partial \Phi_{a}(\mathbf{x})}{\partial \mathbf{x}} \right]$$

This formula is known as Green's theorem (G. Green, 1828). It provides the means for treating surfaces and retains the advantages offered by the free Green's function formalism.



#### Diffusion to/from surfaces

We choose one of the functions in Green's theorem as the vacancy concentration field. The other is free Green's function. This formula below shows that vacancy field can be evaluated everywhere, if  $c(\mathbf{x})$  and its normal derivatives at surfaces are known.

$$\int_{V} dV' \left[ c(\mathbf{x}') \frac{\partial^2 G_0(\mathbf{x}, \mathbf{x}')}{\partial \mathbf{x}'^2} - G_0(\mathbf{x}, \mathbf{x}') \frac{\partial^2 c(\mathbf{x}')}{\partial \mathbf{x}'^2} \right] = \int_{S} dS' \left[ c(\mathbf{x}') \left( \mathbf{n} \cdot \frac{\partial G_0(\mathbf{x}, \mathbf{x}')}{\partial \mathbf{x}'} \right) - G_0(\mathbf{x}, \mathbf{x}') \left( \mathbf{n} \cdot \frac{\partial c(\mathbf{x}')}{\partial \mathbf{x}'} \right) \right]$$





United Kingdom Atomic Energy In the right-hand side of this equation, vacancy concentration at a point  $\mathbf{x}$ ', situated at a surface, can be evaluated using the same approach as the one developed for the dislocation loops.

Evaporation of vacancies from dislocation loops is driven by elastic self-stress. In the case of surfaces, it is driven by surface tension.

Arrive at a system of coupled ODEs for the velocities of nodes on dislocation lines <u>and</u> at surfaces. This fully defines the dynamics of diffusion-mediated evolution of loops and cavities/surfaces.

Journal of the Mechanics and Physics of Solids 103 (2017) 121–141 CCFE is the fusion research arm of the **United Kingdom Atomic Energy Authority** 



#### Diffusion to/from surfaces

Equations, describing the vacancy diffusion-mediated evolution of dislocation loops, cavities *and* the external surface, have the form:

$$\omega(\mathbf{x})c(\mathbf{x}) = D_{v} \int_{S} dS' \left[ c(\mathbf{x}') \left( \mathbf{n} \cdot \frac{\partial G_{0}(\mathbf{x}, \mathbf{x}')}{\partial \mathbf{x}'} \right) - G_{0}(\mathbf{x}, \mathbf{x}') \left( \mathbf{n} \cdot \frac{\partial c(\mathbf{x}')}{\partial \mathbf{x}'} \right) \right]$$

Here  $\omega(\mathbf{x}) = 1$  in the bulk,  $\omega(\mathbf{x}) = 1/2$  at surfaces (this comes from the integration of a delta-function at the surface) and  $\omega(\mathbf{x}) = 0$  in the vacuum. 'Surfaces' also include the toroidal surfaces wrapped around dislocation lines.





This animation shows evolution of voids, interstitial and vacancy dislocation loops, evolving through the evaporation and exchange of vacancies in tungsten at 1750K.

#### Applications: evolution timescales



Evolution of 20 cavities, 20 interstitial loops and 20 vacancy loops randomly distributed with the average number density  $5x10^{-6}$  nm<sup>-3</sup>, in a spherical sample of radius R=142 nm. Objects' radii are initially normally distributed: with the mean of 3.2 nm and standard deviation of 1 nm (loops); with the mean of 1 nm and standard deviation of 0.1 nm (18 smaller cavities); with the mean of 2.2 nm and standard deviation of 0.22 nm (for the two larger cavities).



Vacancy concentration profiles found in a typical simulation. Vacancy loops (red) and voids (blue) generate <u>local</u> zones with high concentration of diffusing vacancies, exceeding the background concentration by over two orders of magnitude. Interstitial loops produce local vacancy depleted zones.

Journal of the Mechanics and Physics of Solids 103 (2017) 121-141



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#### Decomposition of W-Re alloys under irradiation





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#### Transmutations due to exposure to fusion neutrons



Initially pure natural tungsten, exposed to neutrons with the spectrum of a DEMO fusion reactor, transforms into other elements, including rhenium, osmium, helium and hydrogen. Accumulation of rhenium gives rise to the formation of Re-rich precipitates, which embrittle tungsten and reduce its thermal conductivity.



M.R. Gilbert et al., Nucl. Fusion 57 (2017) 044002



### Anomalous segregation in W-Re alloys



X & Y



W-2Re

Re Atom Map

Atom probe observation of segregation of Re in W-2%Re alloy under ion irradiation.

Time of flight

measurement

The puzzling aspect of this phenomenon is that under irradiation, rhenium forms precipitates in highly dilute alloys that, according to equilibrium thermodynamics, should exhibit full solubility.



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thority

DC

Voltage

Local Electrode

Tip cooled to ~50K

A. Xu et al., Acta Materialia 87 (2015) 121



#### Anomalous segregation in W-Re alloys





omic



J. Wrobel et al., J. Phys.: Condens. Matter 29 (2017) 145403

Model for binary W-Re alloys + vacancies as ternary W-Re-vacancy alloys. This

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#### Anomalous segregation in W-Re alloys

J. Phys.: Condens. Matter 29 (2017) 145403

J S Wróbel et al

**Table 1.** Monte Carlo results as functions of Re and vacancy concentration for alloys quenched down from high temperatures. MC simulations were performed starting from 2500 K. Alloys were cooled down with the temperature step of 100 K to the temperature of 100 K with 3000 MC steps per atom performed both at thermalization and accumulation stages.



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# Recent advances in modeling and simulation of the exposure and response of tungsten to fusion energy conditions

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#### Abstract

Under the anticipated operating conditions for demonstration magnetic fusion reactors