



Consiglio Nazionale  
delle Ricerche

*Ab-initio*  
**electron-molecule state-resolved dynamics  
for non-equilibrium plasmas modelling**

Vincenzo Laporta

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**25<sup>th</sup> Data Center Network meeting, IAEA, Vienna, Austria – 1 October 2019**

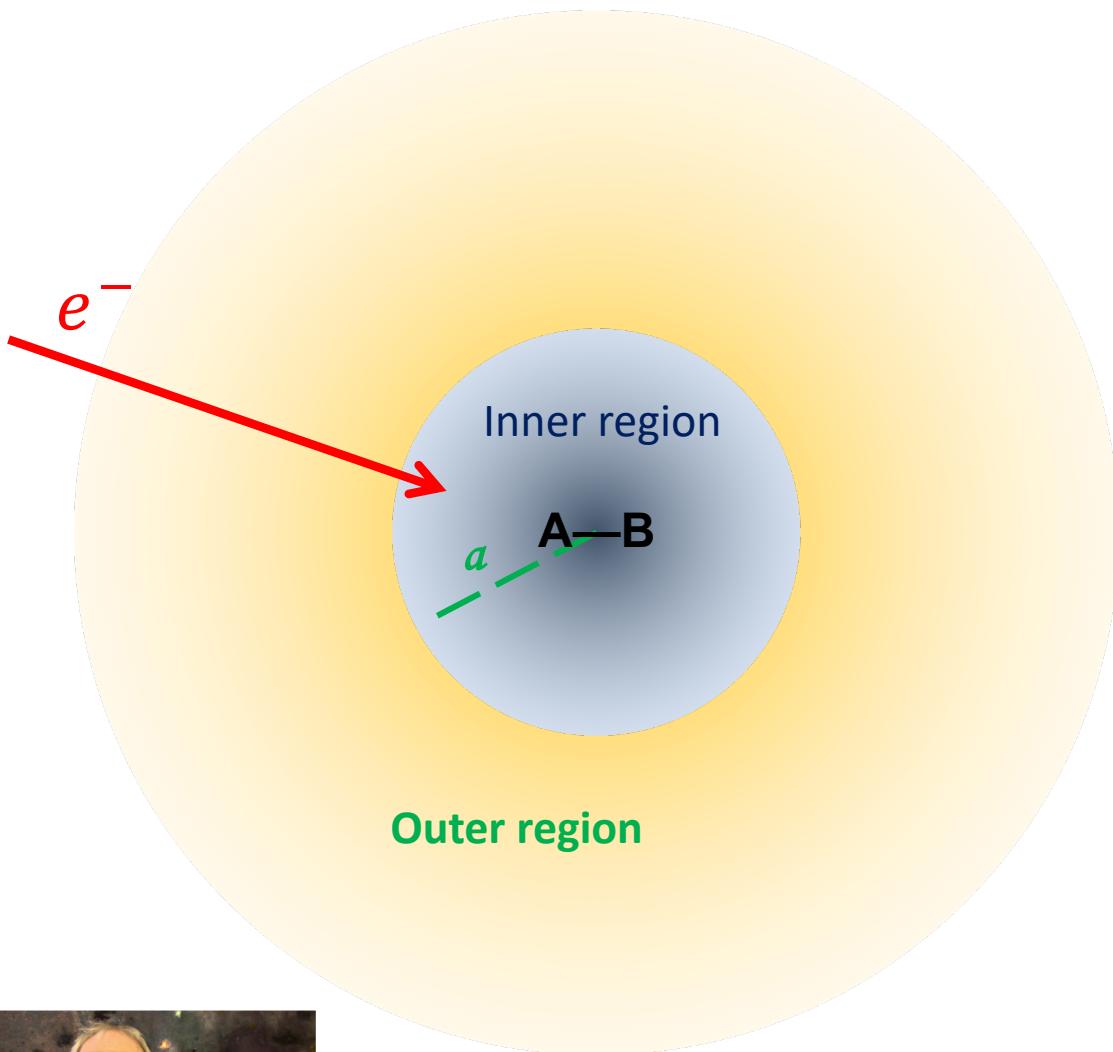
## Plan of the presentation:

1. Theory: electron-molecule scattering
2. *ab-initio* state-resolved cross sections:
  - A. **Nitrogen and Oxygen:** Atmospheric (re-)entry and hypersonic
  - B. **Carbon dioxide:** Plasma-based CO<sub>2</sub> conversion
  - C. **BeH<sup>+</sup>, H<sub>2</sub><sup>+</sup>, OH, ArH<sup>+</sup>:** I.T.E.R and controlled fusion; Astrochemistry
3. Conclusions and perspectives

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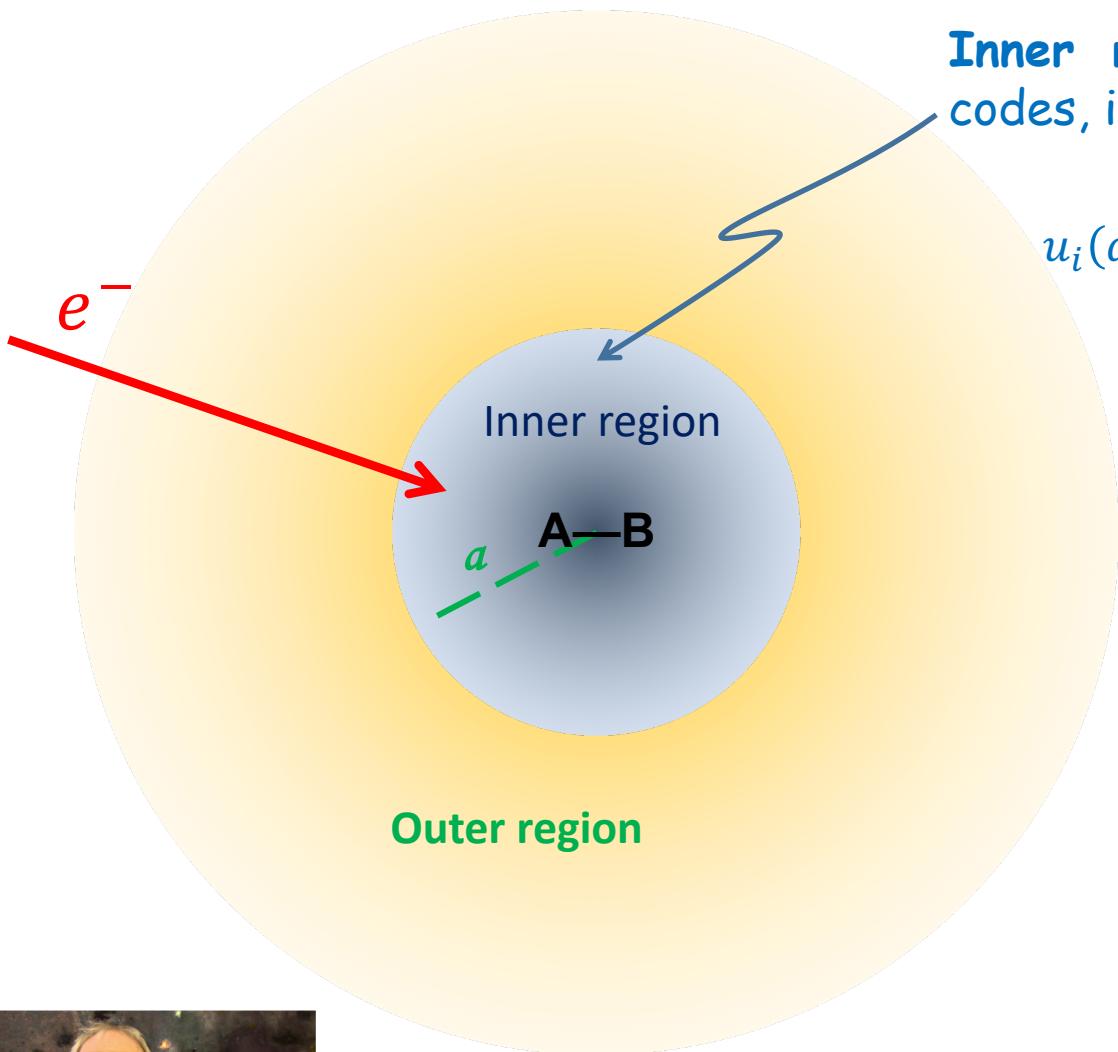
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# The R-matrix method



J. Tennyson, Phys. Rep., **491**, 29 (2010)

# The R-matrix method



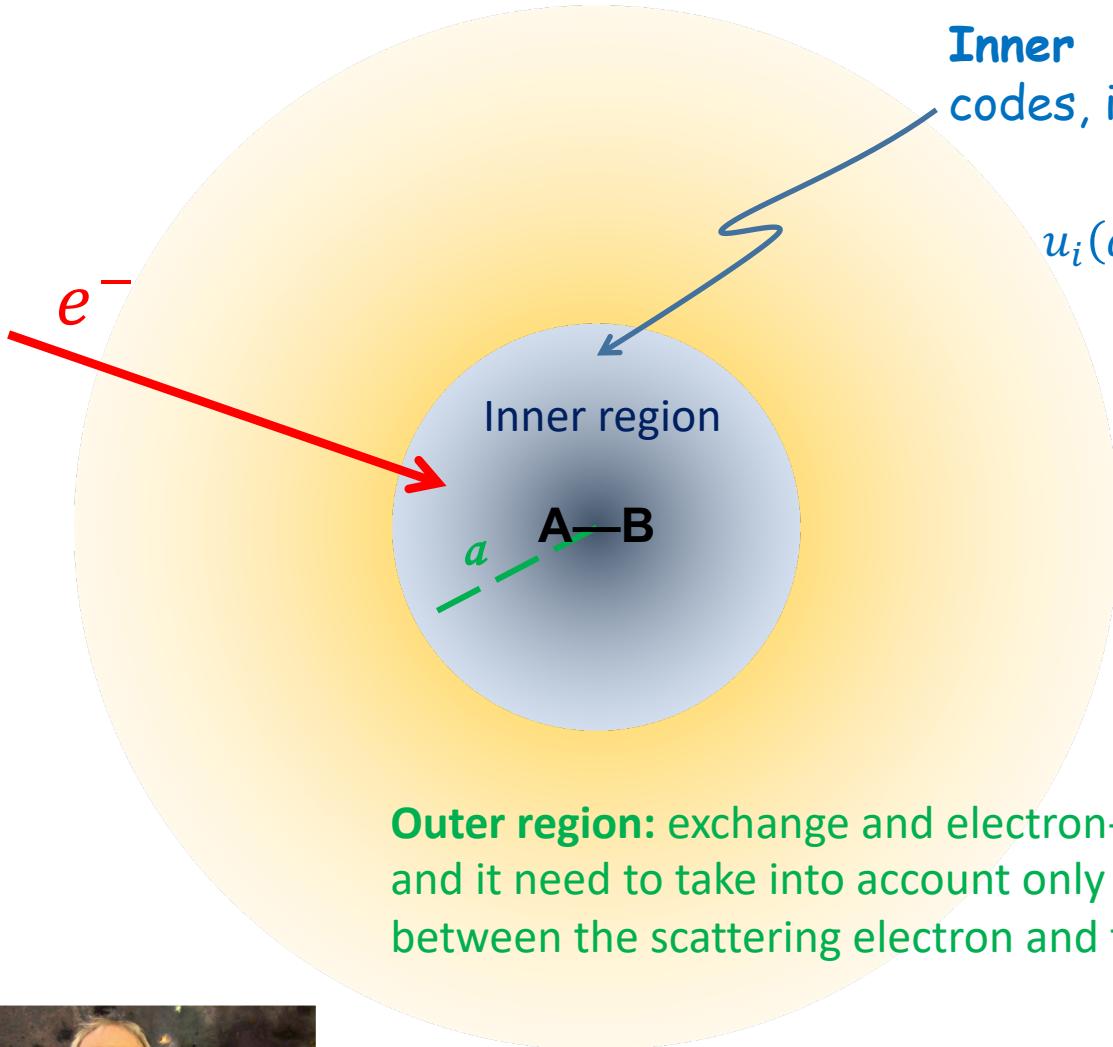
Inner region: N+1 electrons; *ab-initio* quantum chemistry codes, including exchange correlations; continuum orbitals

$$u_i(a) = \sum_j R_{ij}(a, E) [r u_j' - b u_j]_{r=a}$$

$$R_l(a, E) = \frac{1}{2} \sum_{\lambda} \frac{w_{\lambda l}(a)^2}{E_{\lambda} - E}$$



# The R-matrix method



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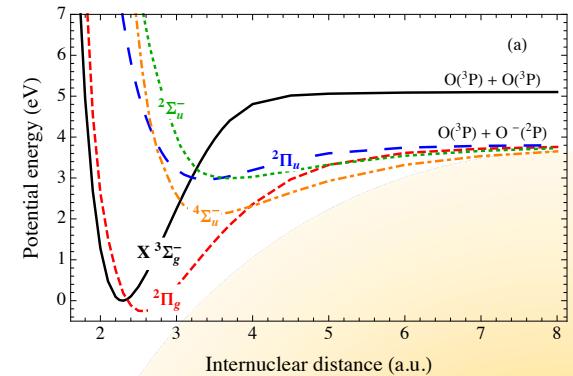
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**Outer region:** exchange and electron-electron correlations are neglected and it need to take into account only long-range multi-polar interactions between the scattering electron and the target

$$u_l(r) \sim \frac{1}{\sqrt{k}} (\sin \varphi_l + \cos \varphi_l K_l)$$



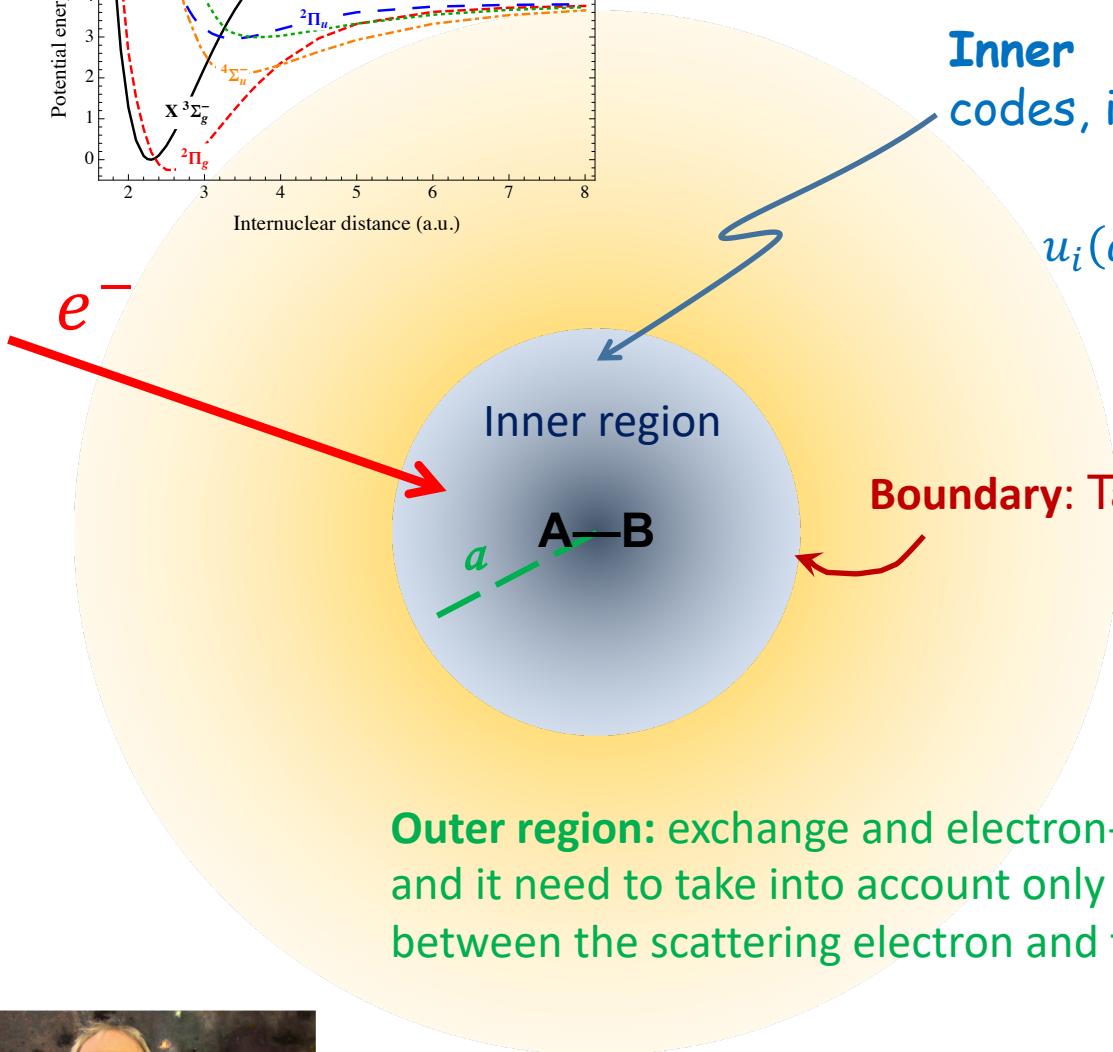


## The R-matrix method

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$$K_l = e^{-2i\varphi_l} \frac{1 - R_l(L^* - b)}{1 - R_l(L - b)},$$

$$u_l(r) \sim \frac{1}{\sqrt{k}} (\sin \varphi_l + \cos \varphi_l K_l)$$

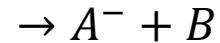


## Basic formulas for electron-molecule scattering

Processes occurring for resonant electron-molecule scattering:



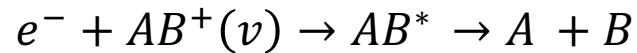
*Vibrational Excitation*



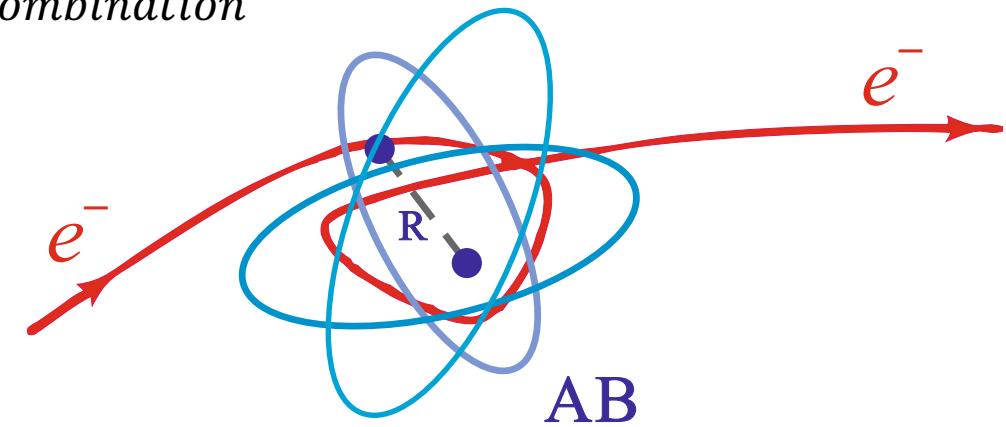
*Dissociative Attachment*



*Dissociative Excitation*

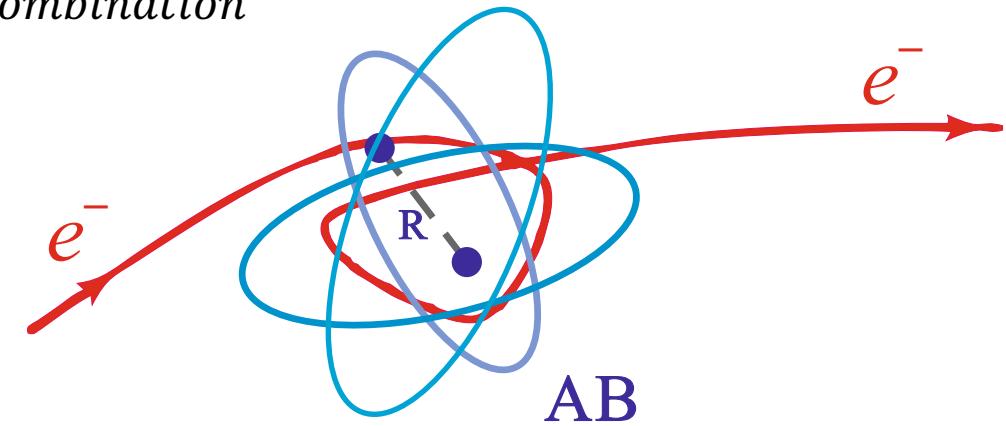
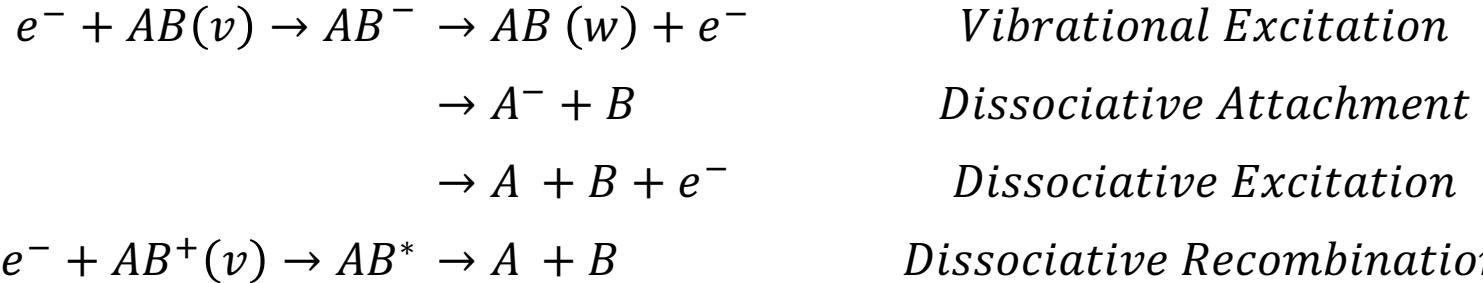


*Dissociative Recombination*



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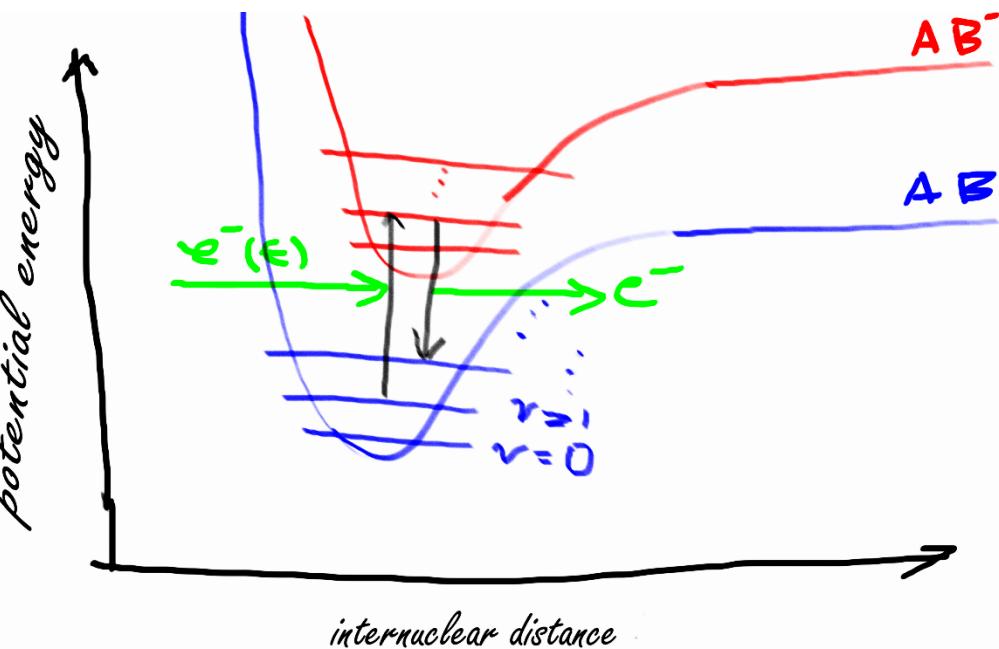
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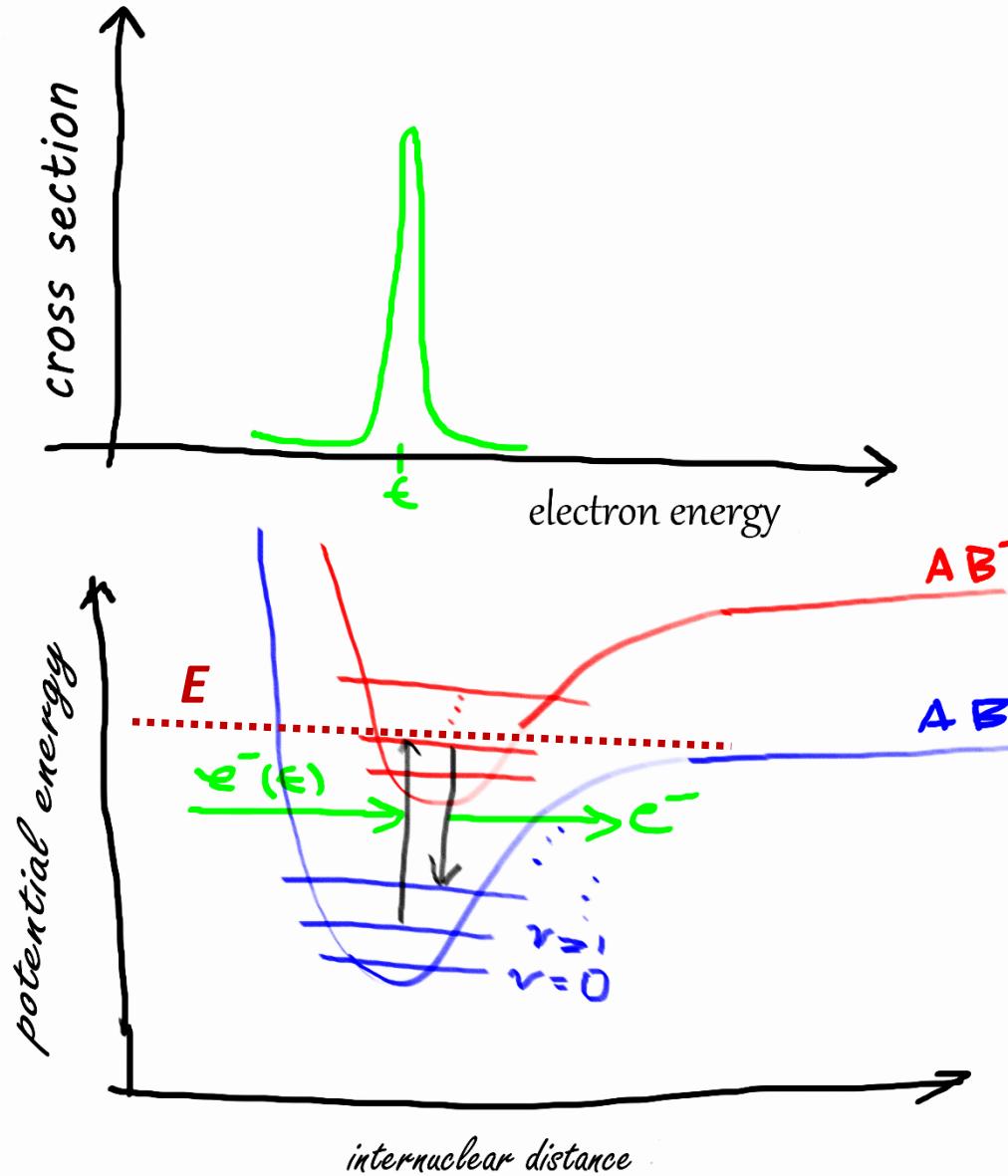


$$\left( T_N + V^- - \frac{i}{2} \Gamma - E \right) \xi(R) = -V_{dk}^*(\epsilon, R) \chi_i(R),$$

*Neutral molecule*

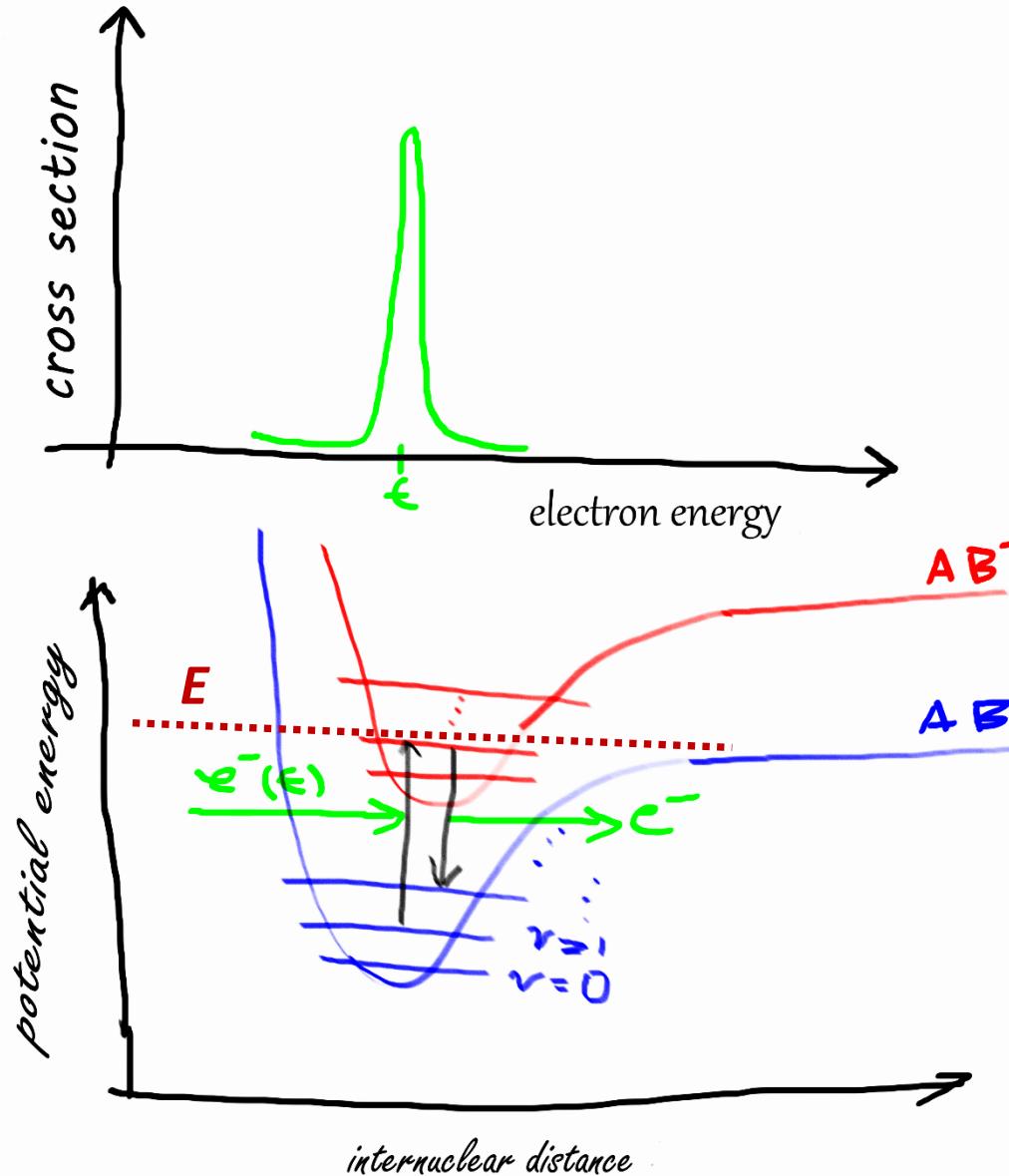
**Resonant**  
*Vibrational-excitation*  
*cross section*



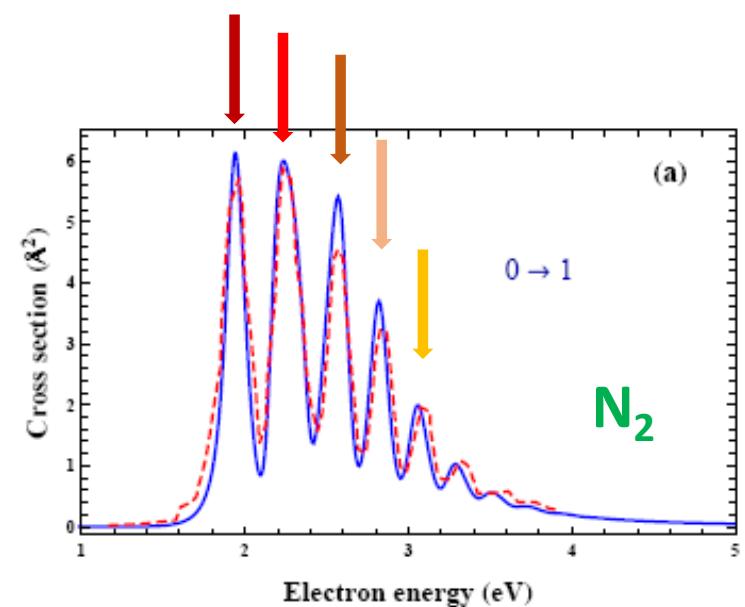


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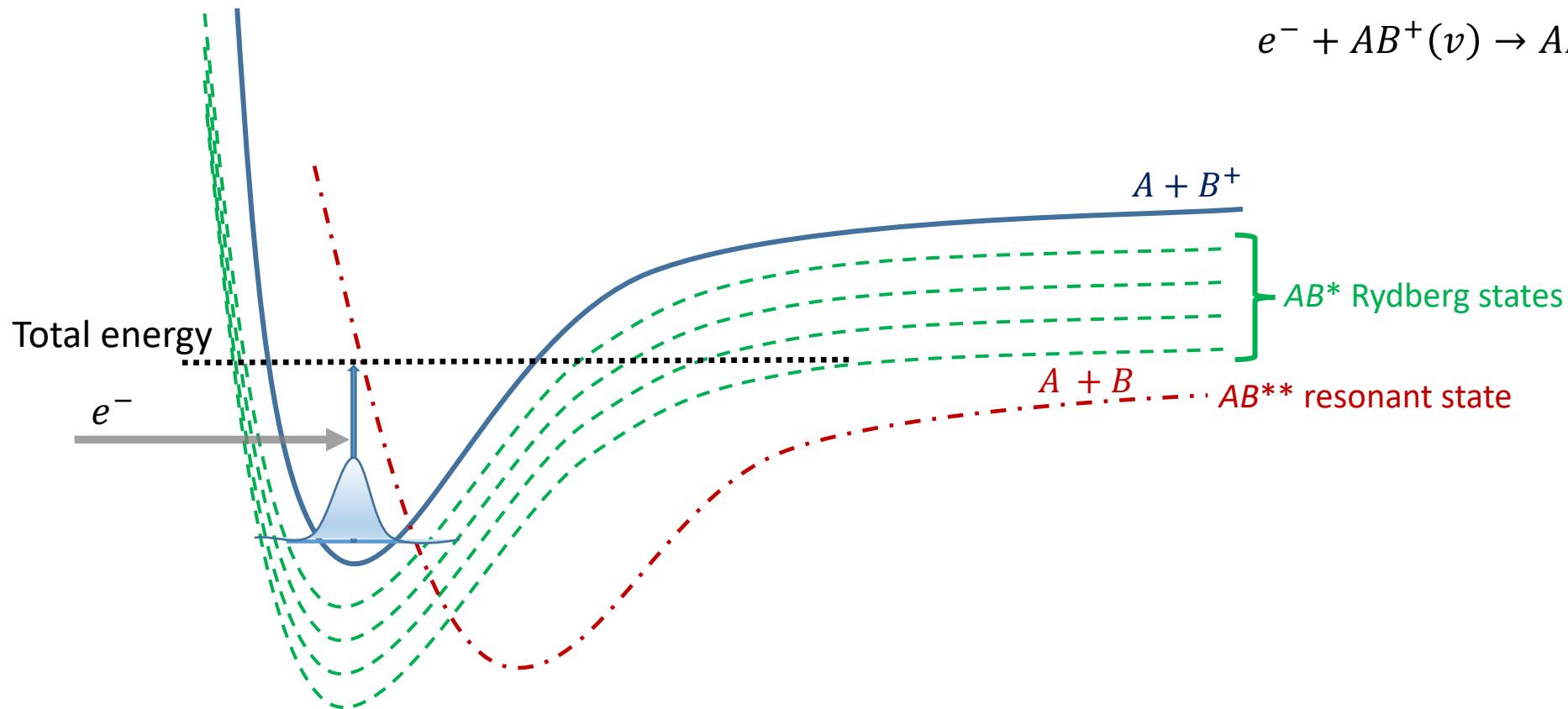




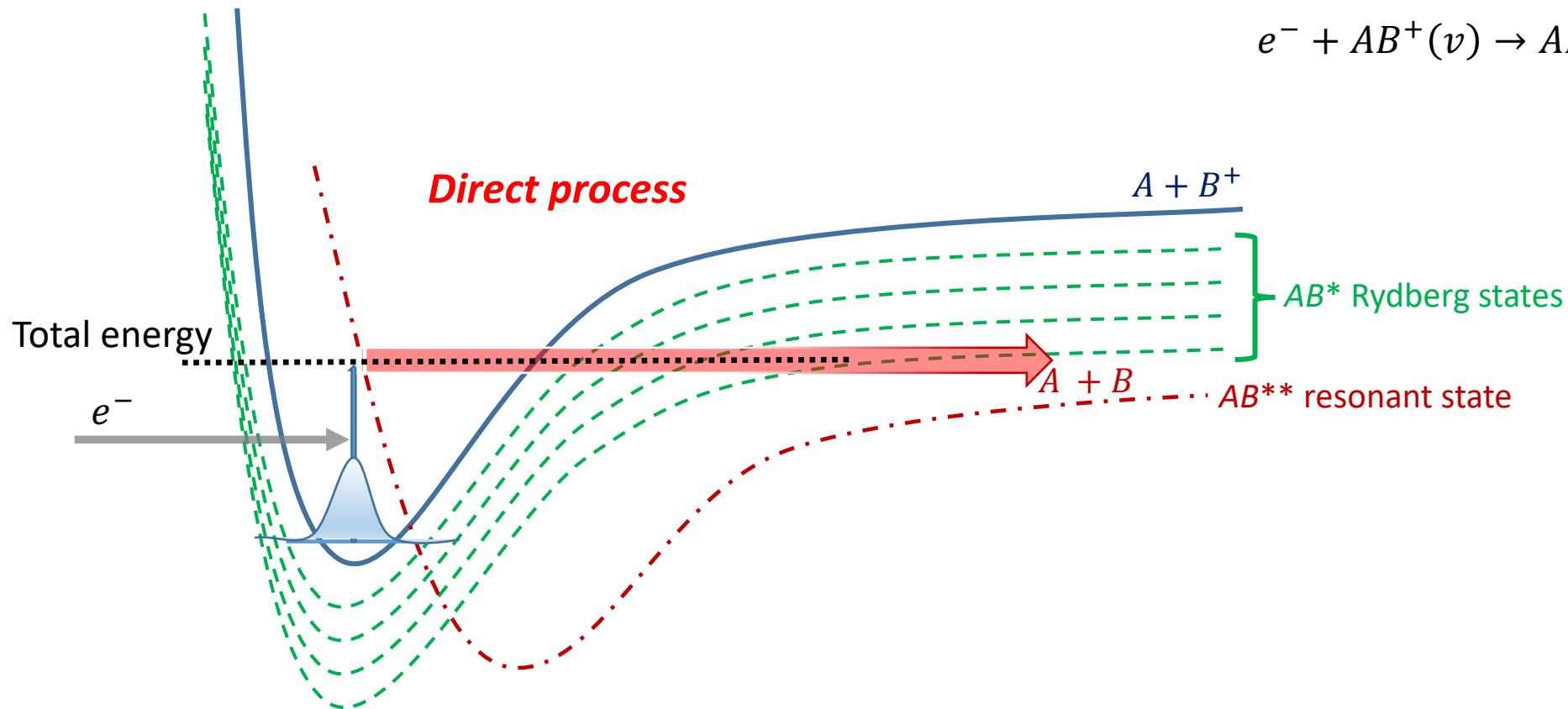
**Resonant  
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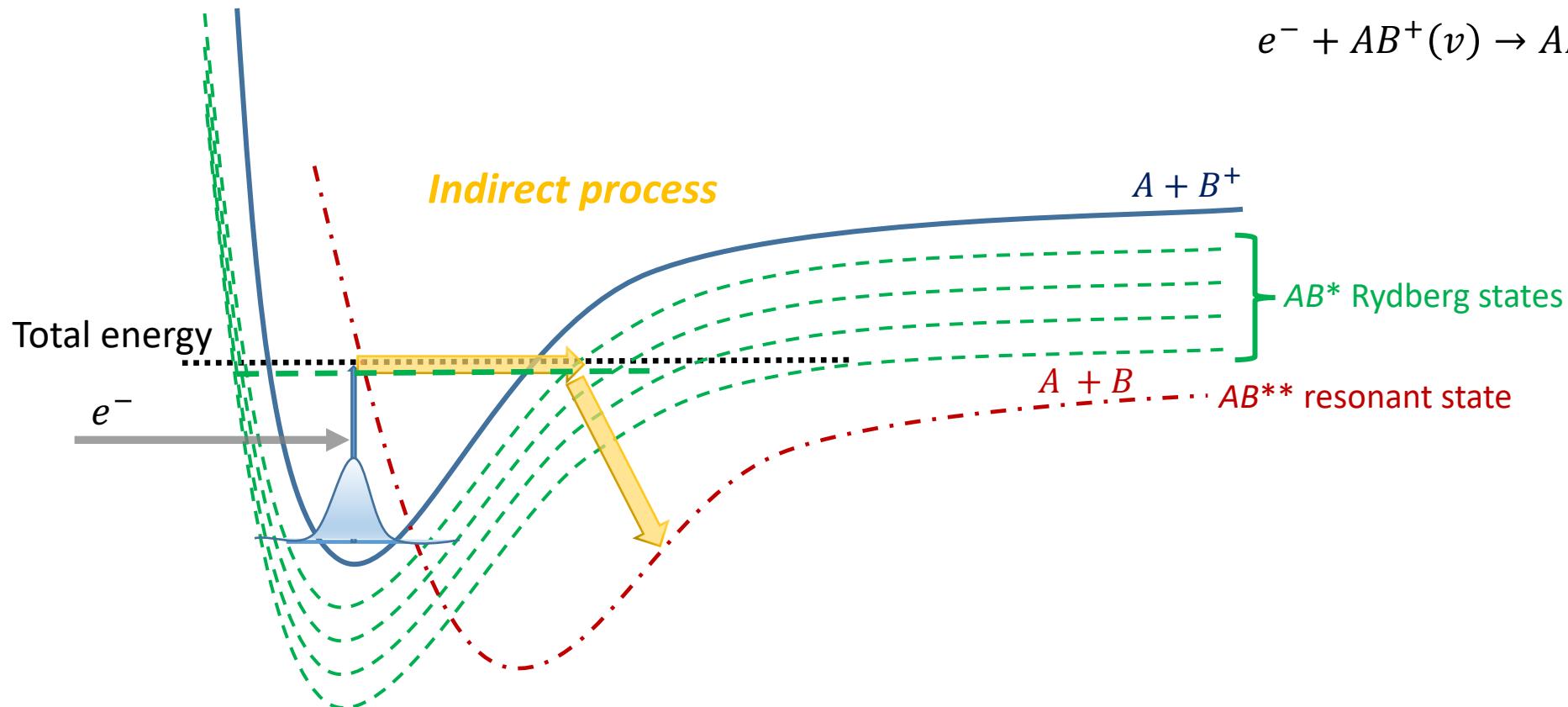
## Dissociative recombination



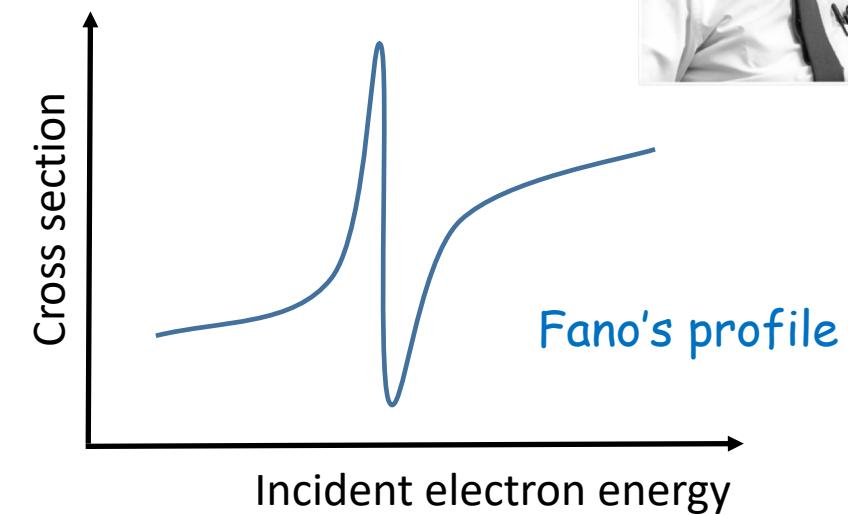
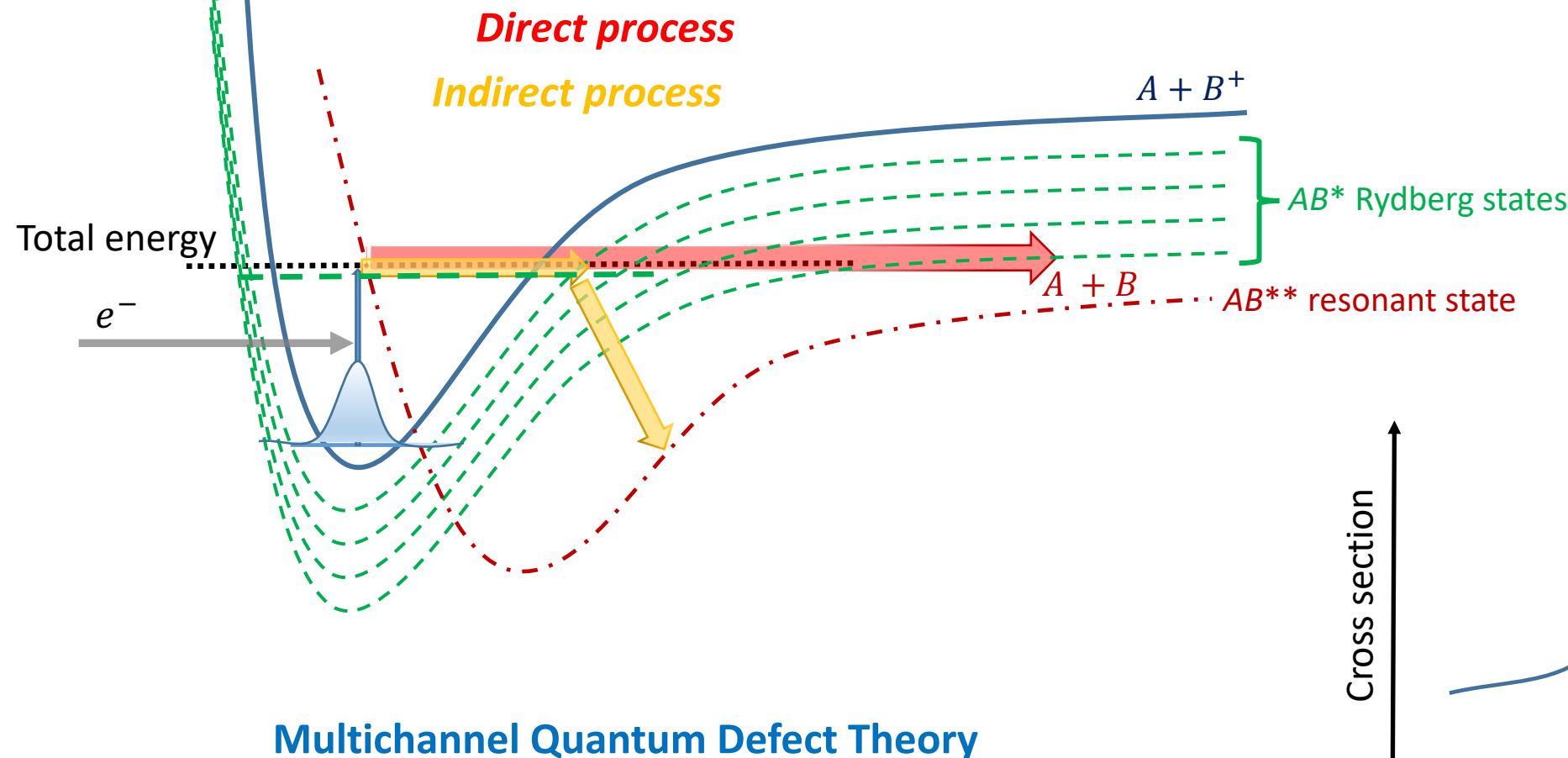
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**electron-N<sub>2</sub> resonant scattering**

## electron-N<sub>2</sub> resonant scattering

The resonance at 2.3 eV in electron-N<sub>2</sub> scattering is described in term of the resonant state N<sub>2</sub><sup>-</sup>(X <sup>2</sup>P<sub>g</sub>)

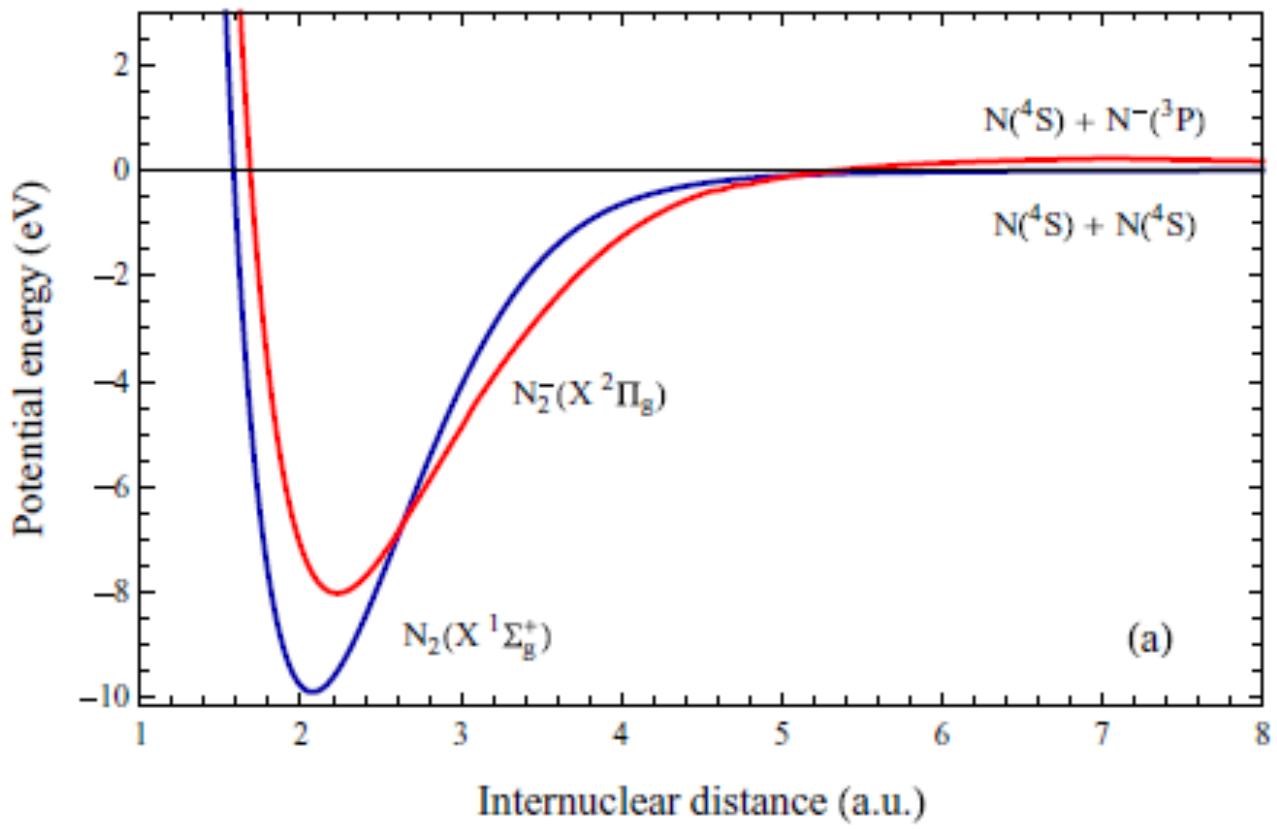
The quantum chemistry codes MOLPRO and UK-R-Matrix have been used to calculate potential energy curves, resonance width and scattering

cc-pvQZ basis set      MR-CI model

N<sub>2</sub> target: (1σ<sub>g</sub>, 1σ<sub>u</sub>)<sup>4</sup>(2σ<sub>g</sub>, 2σ<sub>u</sub>, 1π<sub>u</sub>, 3σ<sub>g</sub>, 1π<sub>g</sub>, 3σ<sub>u</sub>)<sup>10</sup>

e+N<sub>2</sub> scattering: (1σ<sub>g</sub>, 1σ<sub>u</sub>)<sup>4</sup>(2σ<sub>g</sub>, 2σ<sub>u</sub>, 1π<sub>u</sub>, 3σ<sub>g</sub>, 1π<sub>g</sub>, 3σ<sub>u</sub>)<sup>11</sup>  
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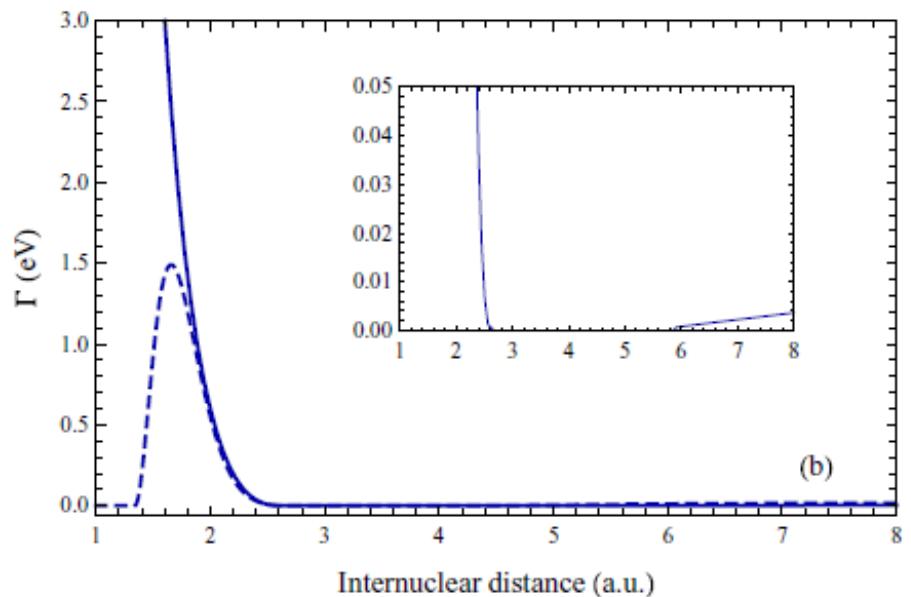
### Potential energy curves



(a)

**N<sub>2</sub>**

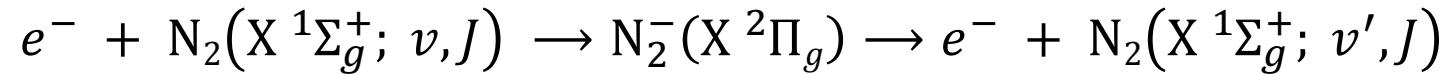
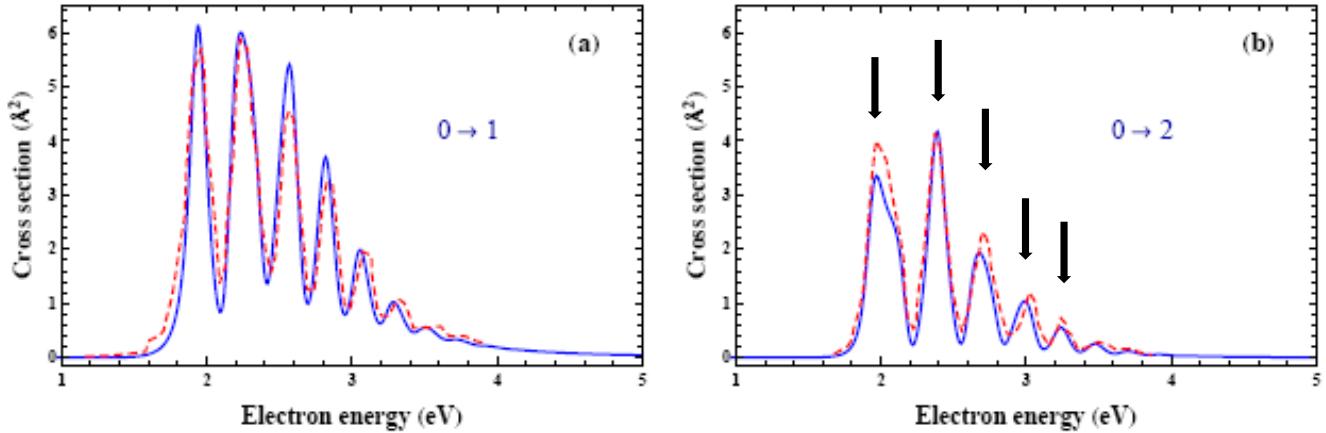
Coupling  $N_2^- / N_2$



(b)

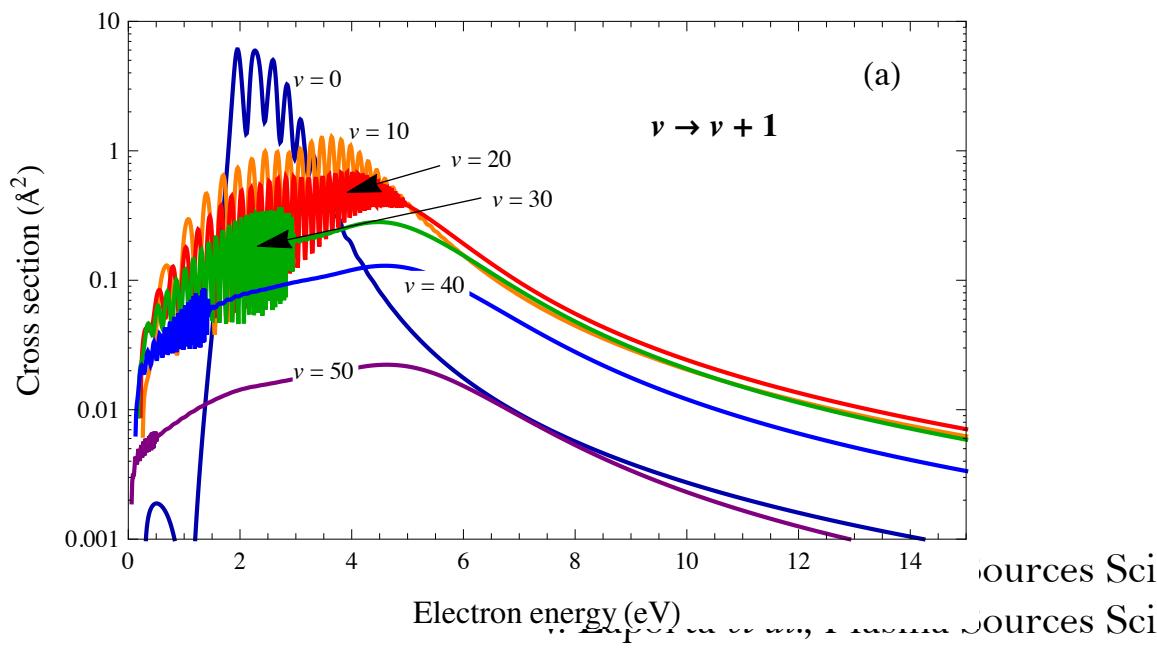
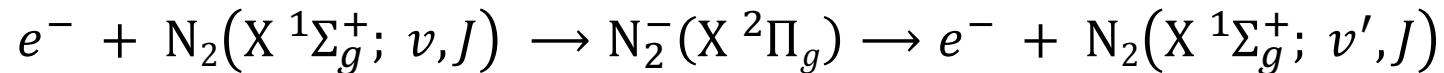
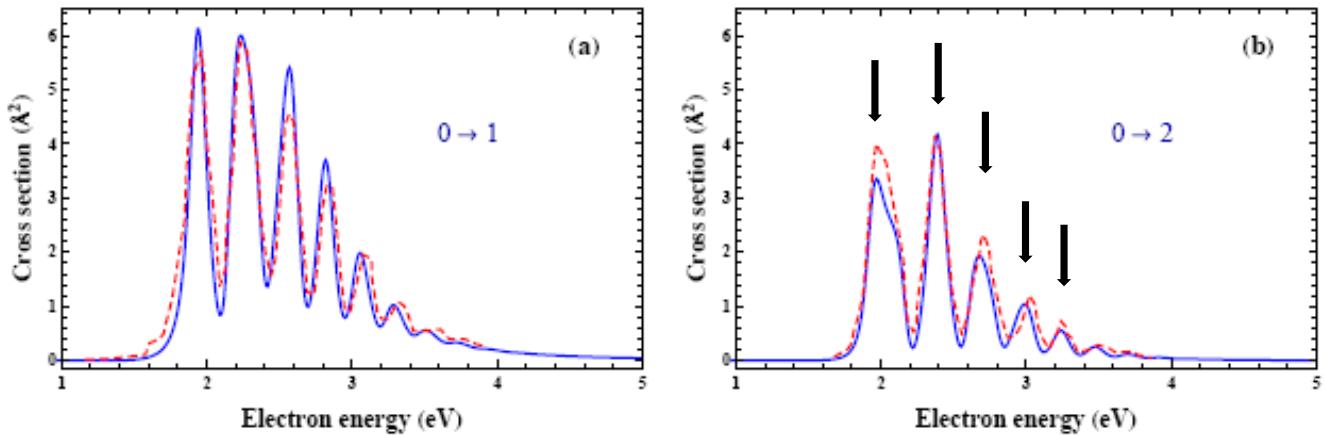
## Comparison with experiments

### Vibrational-excitation process:

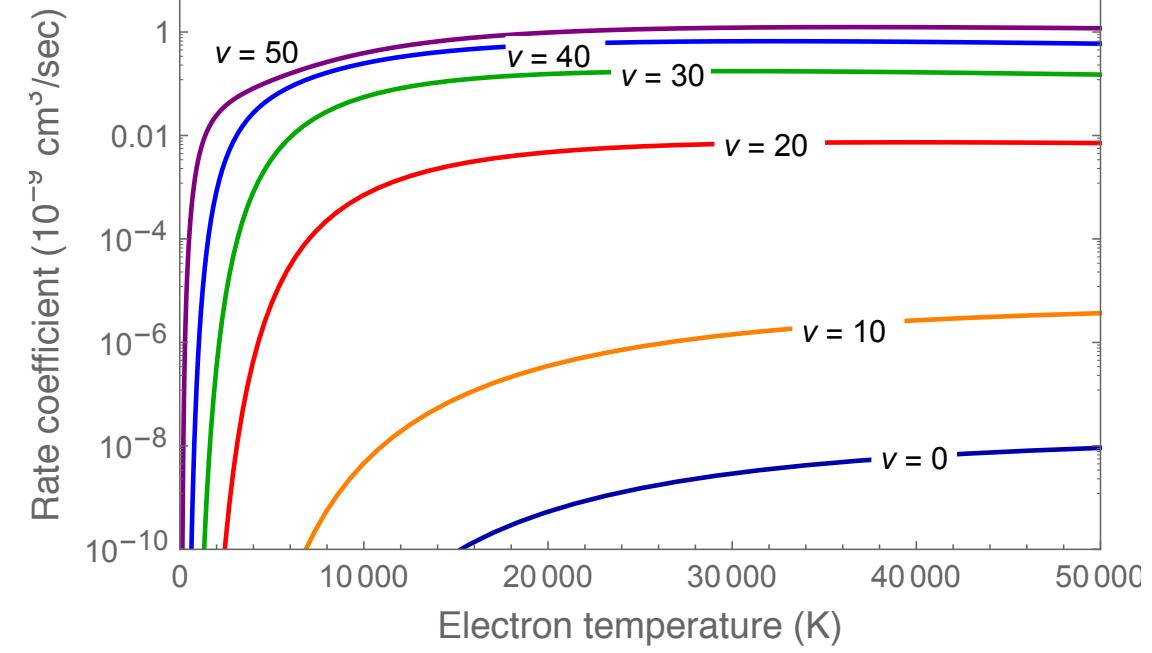
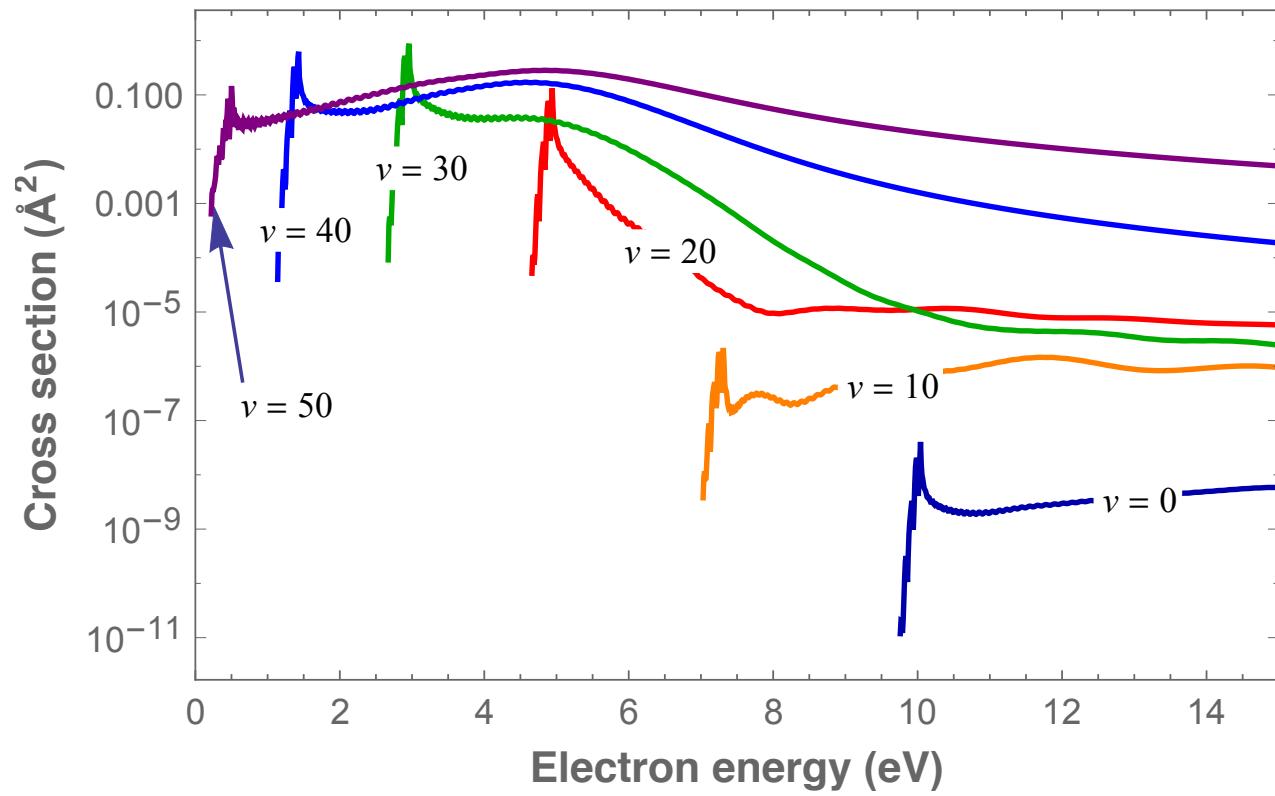
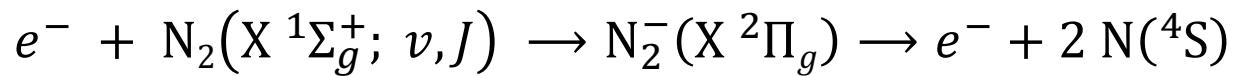


## Comparison with experiments

### Vibrational-excitation process:



## Electron-impact dissociation:



electron- $O_2(x, v)$  resonant scattering

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In order to describe the low-energy electron- $O_2(X\ ^3\Sigma_g^-)$  resonant scattering it needs to include in the calculations four resonant states,  $^2\Pi_g$ ,  $^2\Pi_u$ ,  $^4\Sigma_u^-$ ,  $^2\Sigma_u^-$  of  $O_2^-$

Potential energy curves and resonance widths were obtained by MOLPRO and R-matrix within aug-cc-pvQZ basis-set and MR-CI model

Orbital configurations for  $O_2$  target:

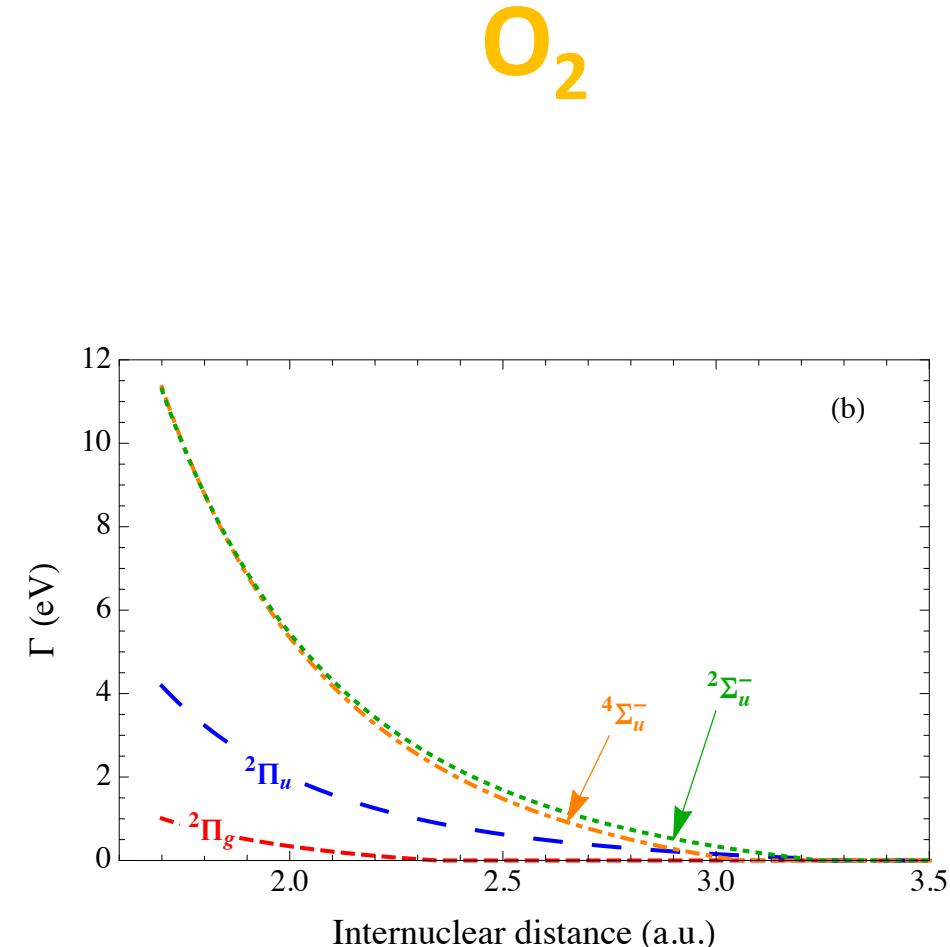
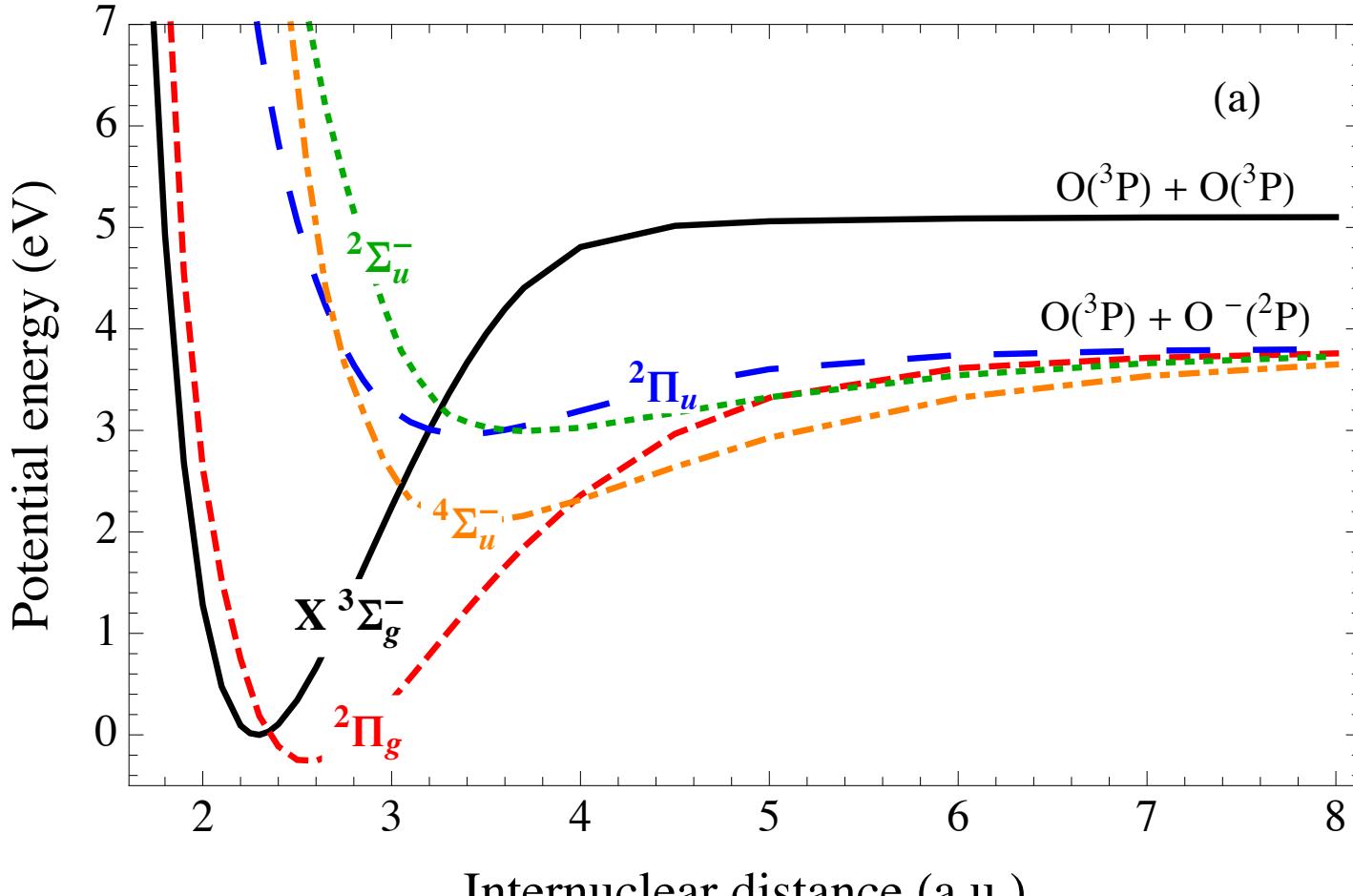


Two orbital configurations for  $e + O_2$  scattering:



and





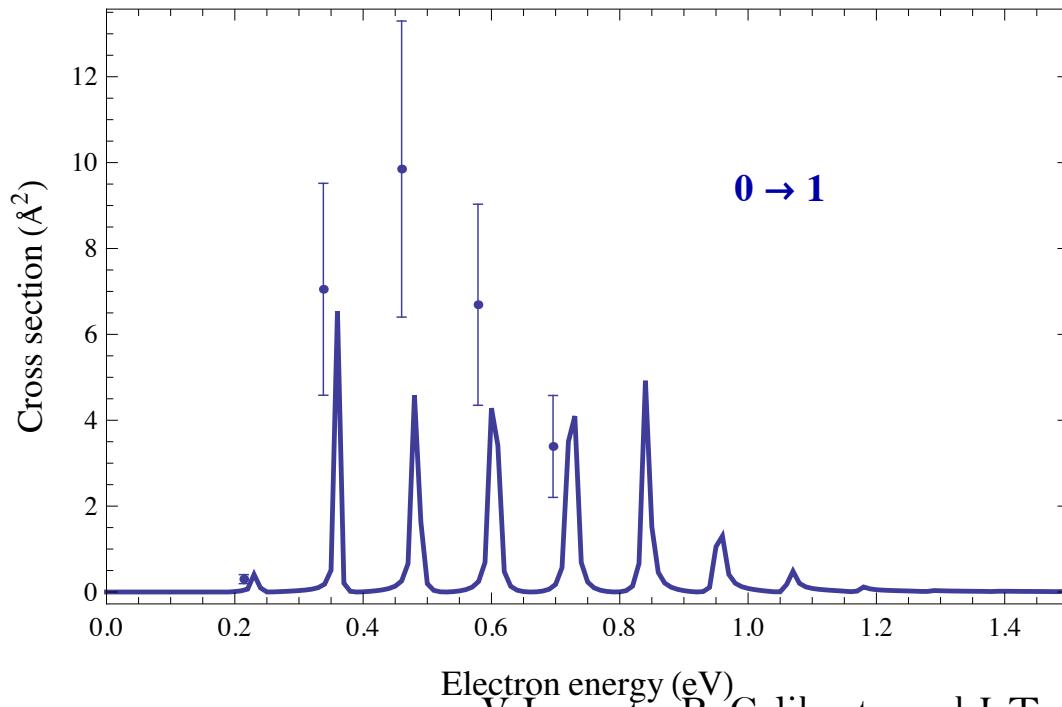
V. Laporta, R. Celiberto and J. Tennyson, *Phys. Rev. A* **91**, 012701 (2015).

V. Laporta, R. Celiberto and J. Tennyson, *Plasma Sources Sci. Technol.* **22**, 025001 (2013)

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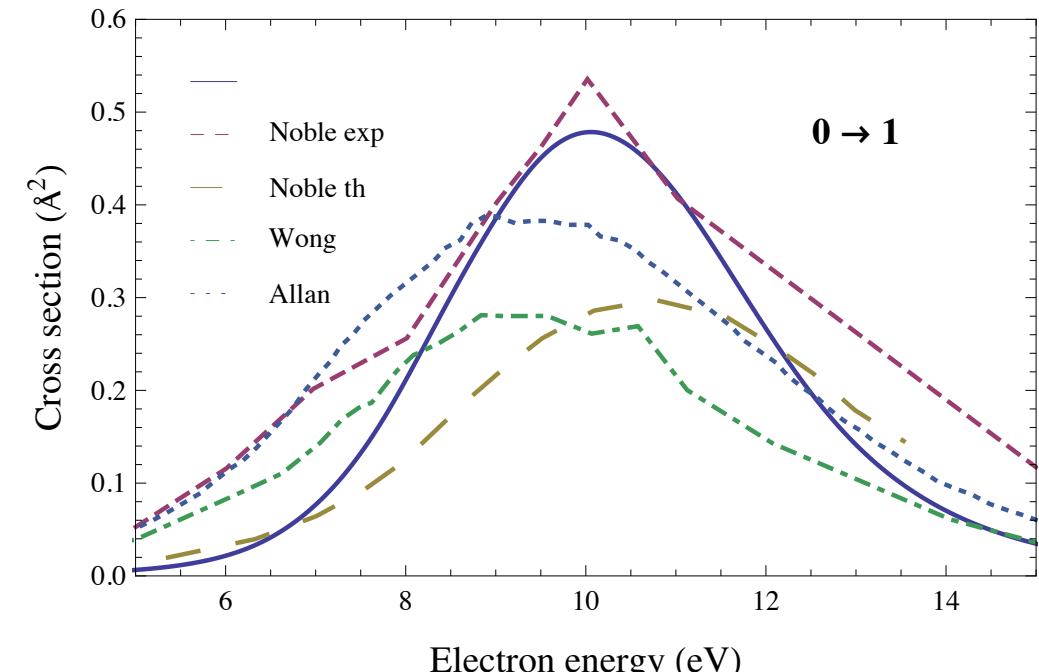
Low energy dominated by  $^2\Pi_g$  symmetry  
comparison with Allan's results



V. Laporta, R. Celiberto and J. Tennyson, *Phys. Rev. A* **91**, 012701 (2015).

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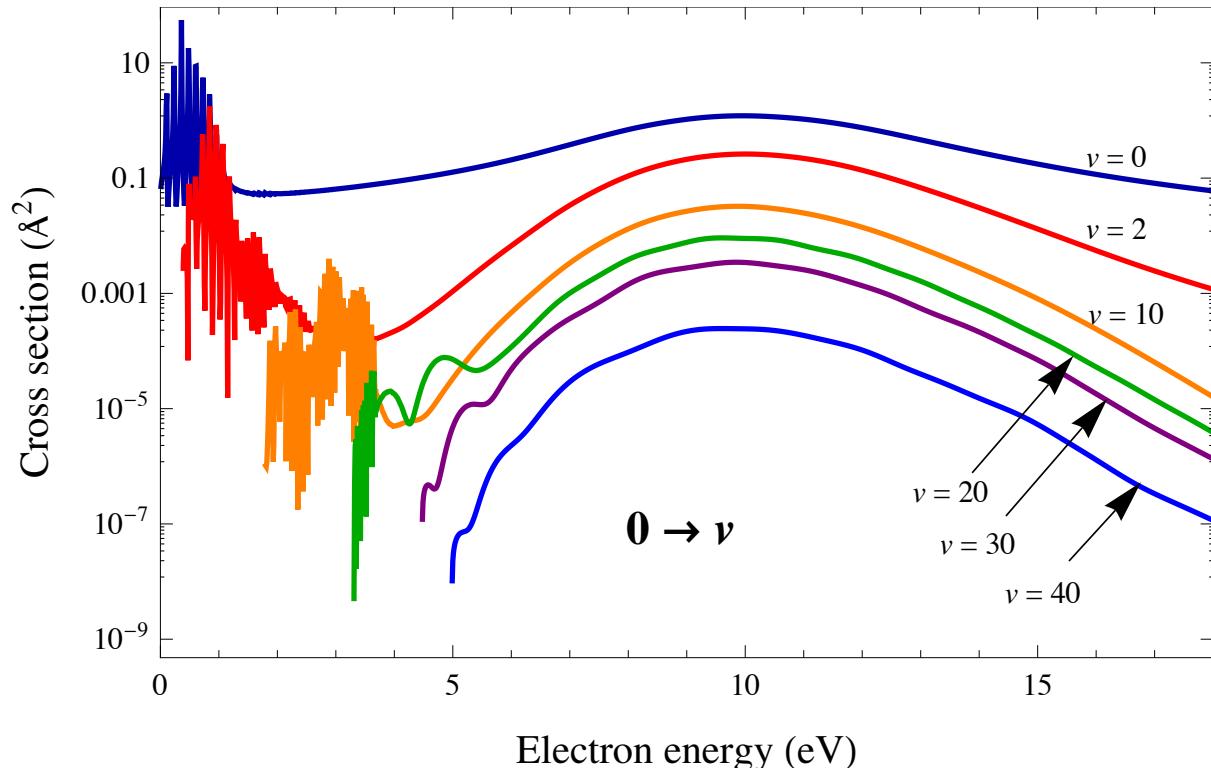
Resonance at 10 eV dominated by  $^4\Sigma_u^-$  symmetry



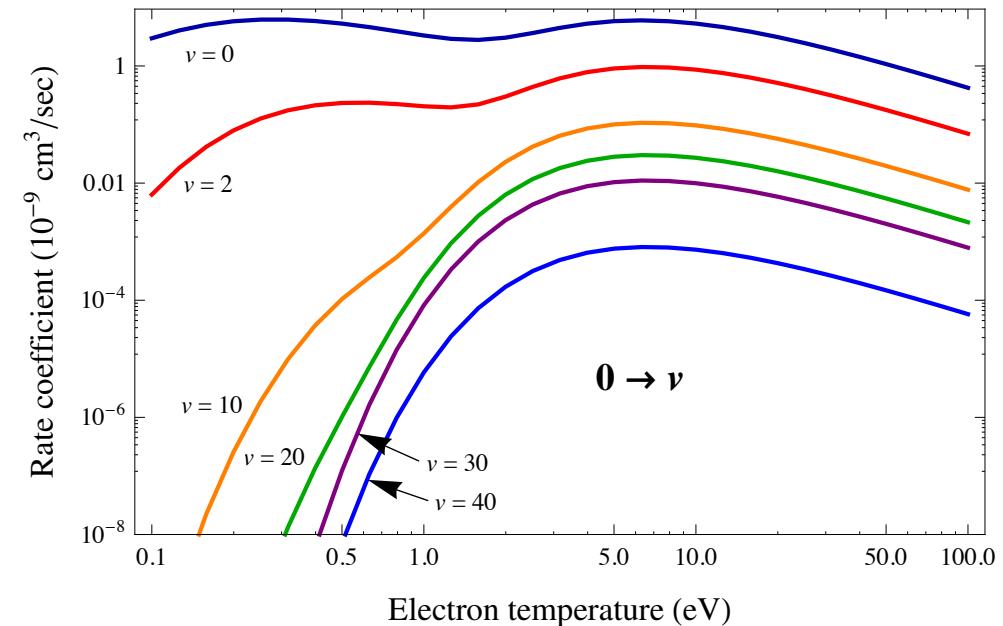
## Vibrational-Excitation process:



Full set of *Vibrational Excitation* cross sections for  $j = 1\dots$



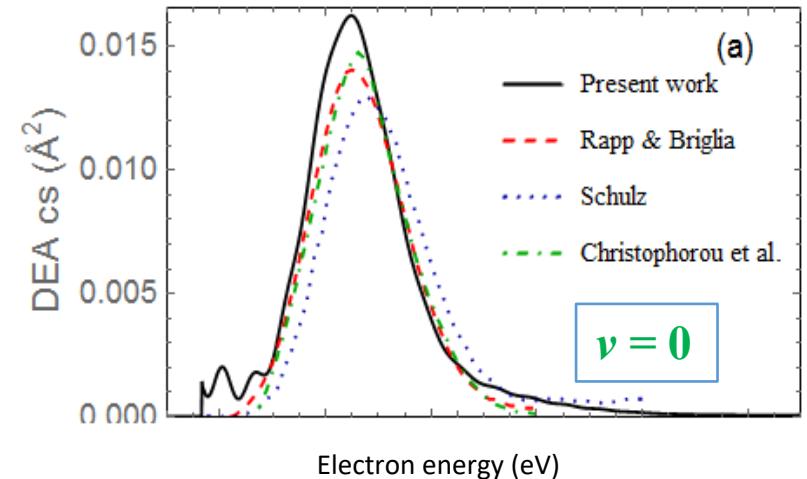
...and the corresponding rate coefficients



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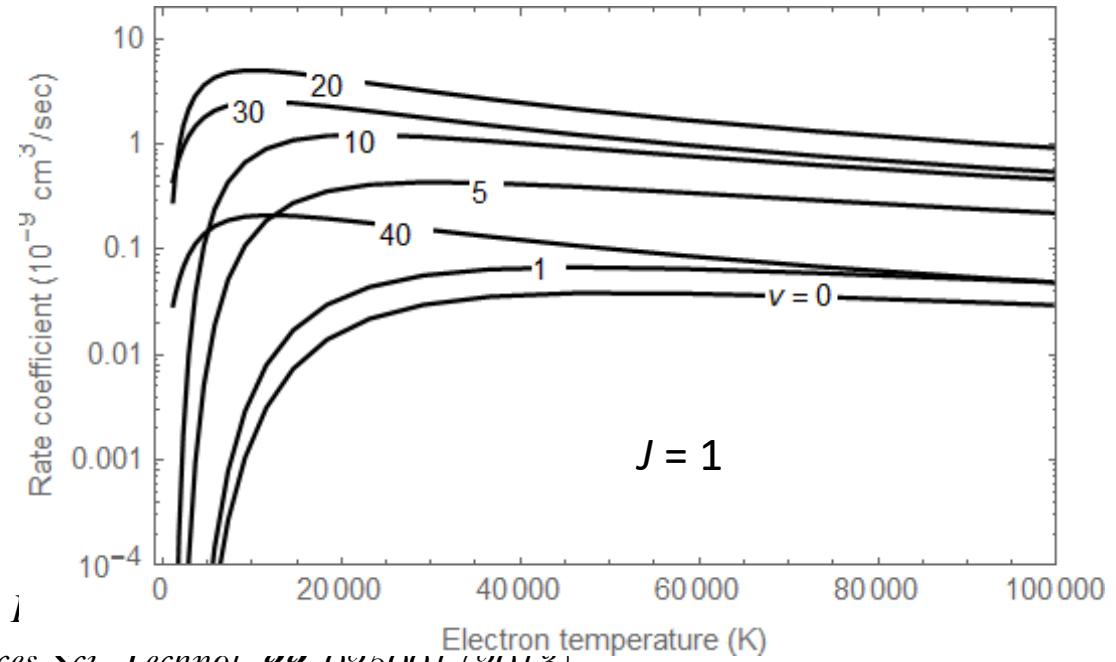
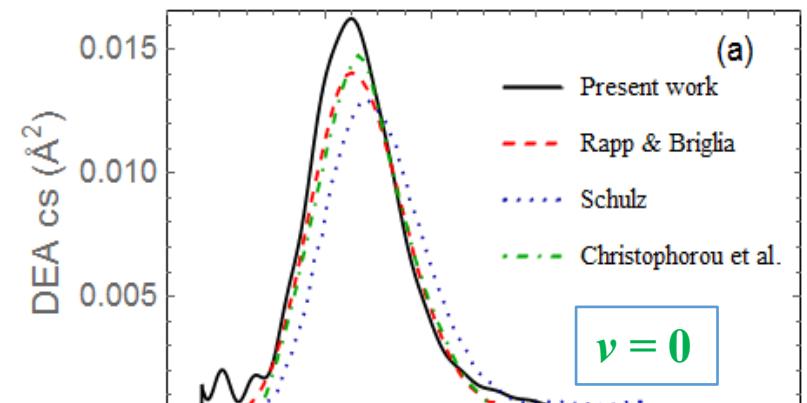
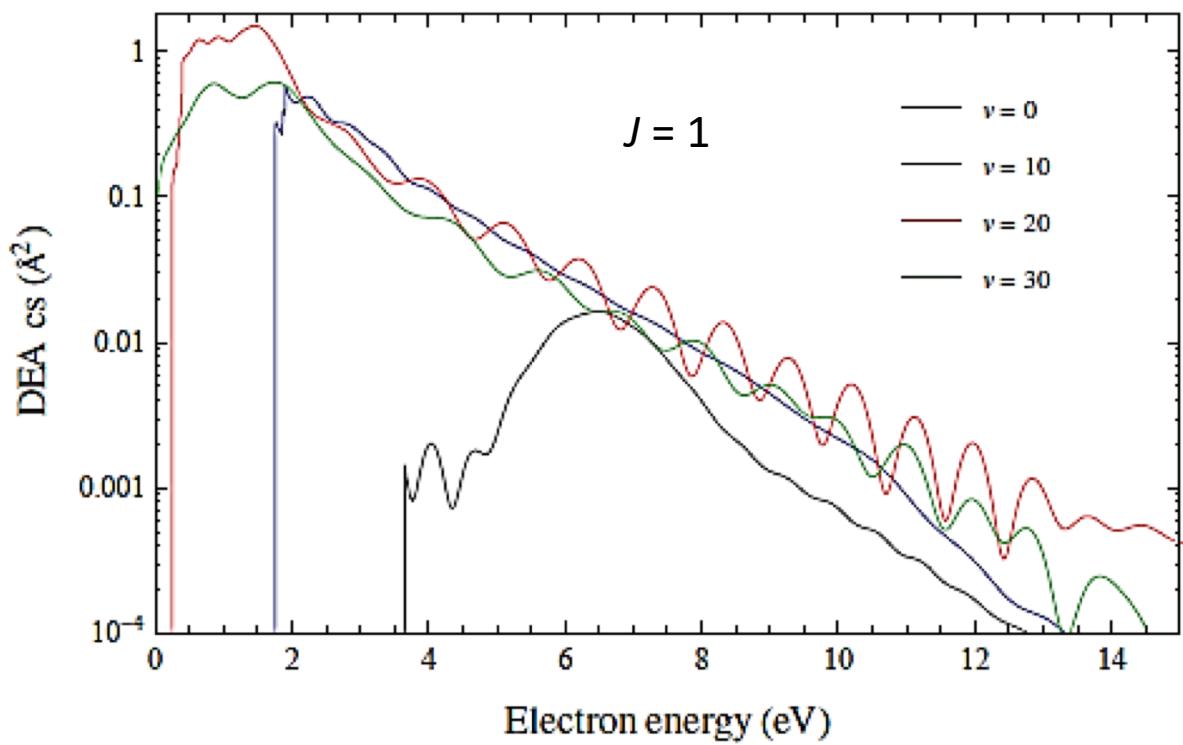
## Dissociative-Electron-Attachment



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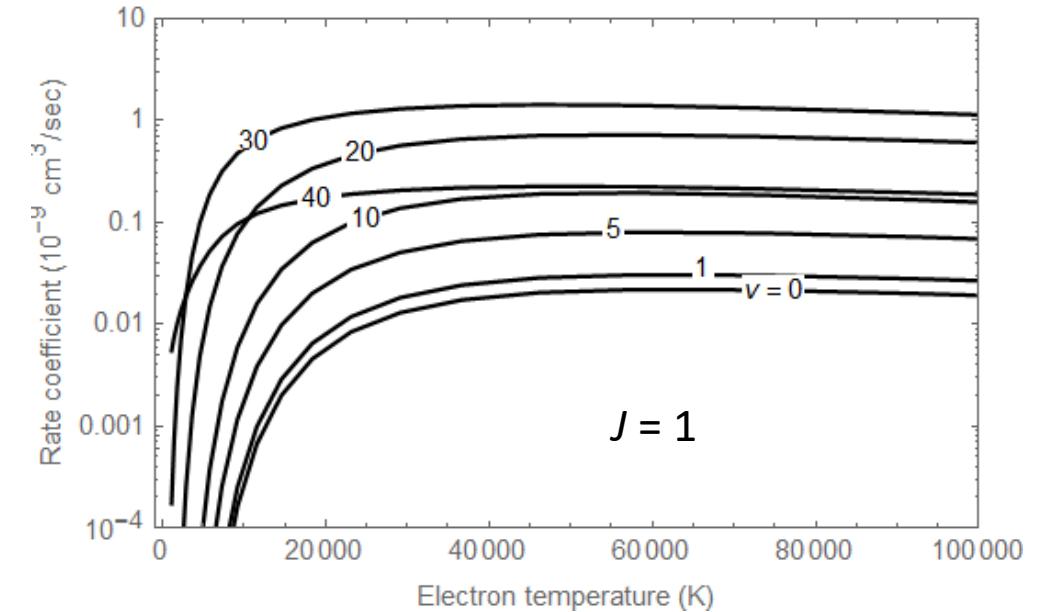
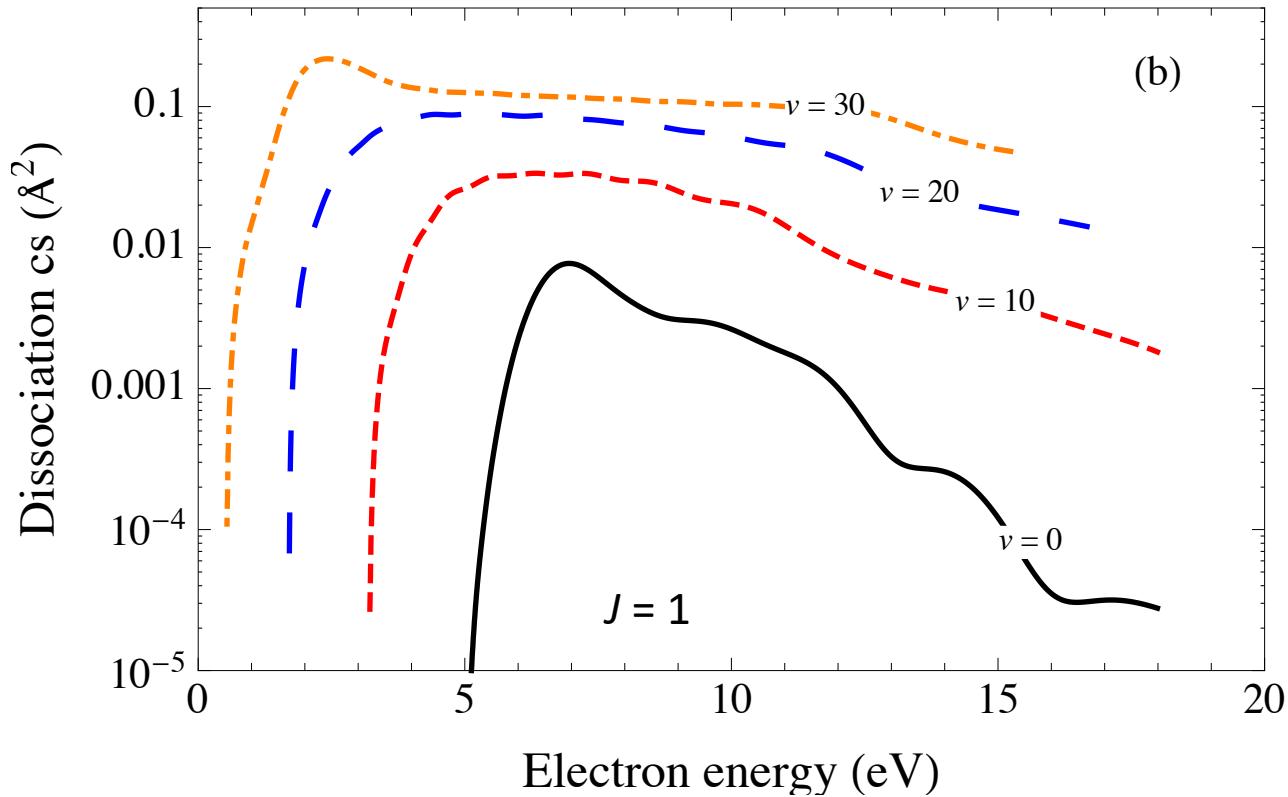
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V. Laporta, R. Celiberto and J. Tennyson, *Phys. I*

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## Electron-impact dissociative excitation:



V. Laporta, R. Celiberto and J. Tennyson, *Phys. Rev. A* **91**, 012701 (2015).

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Recently, worldwide attention has been focused on

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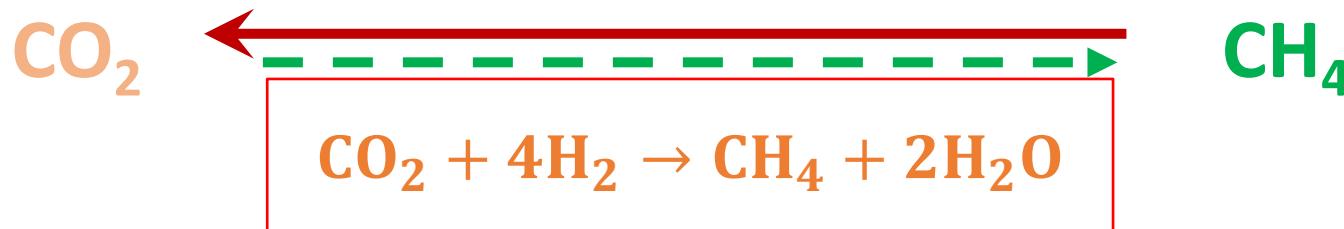


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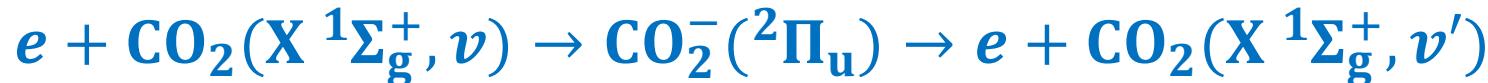


Highly endothermic carbon dioxide dissociation is one of the key processes affecting the overall reaction efficiency

A promising approach for this conversion involves the non-equilibrium chemistry in the plasma phase by electric discharges

# Electron-CO<sub>2</sub> cross sections

*Vibrational-excitation*



## CO<sub>2</sub> SYMMETRIC MODE

MOLPRO (MRCI model, aug-cc-pVQZ basis set,  $D_{2h}$ ):

3 CORE ORBITALS: ( 2A<sub>g</sub> + 0B<sub>3u</sub> + 0B<sub>2u</sub> + 0B<sub>1g</sub> + 1B<sub>1u</sub> + 0B<sub>2g</sub> + 0B<sub>3g</sub> + 0A<sub>u</sub> )<sup>6</sup>

12 VALENCE ORBITALS: ( 3A<sub>g</sub> + 2B<sub>3u</sub> + 2B<sub>2u</sub> + 0B<sub>1g</sub> + 3B<sub>1u</sub> + 1B<sub>2g</sub> + 1B<sub>3g</sub> + 0A<sub>u</sub> )<sup>16</sup>

## CO<sub>2</sub> BENDING/ANTISYMMETRIC MODE

MOLPRO (MRCI model, aug-cc-pVQZ basis set,  $C_{2v}$ ):

3 CORE ORBITALS: ( 2A<sub>1</sub> + 0B<sub>1</sub> + 1B<sub>2</sub> + 0A<sub>2</sub> )<sup>6</sup>

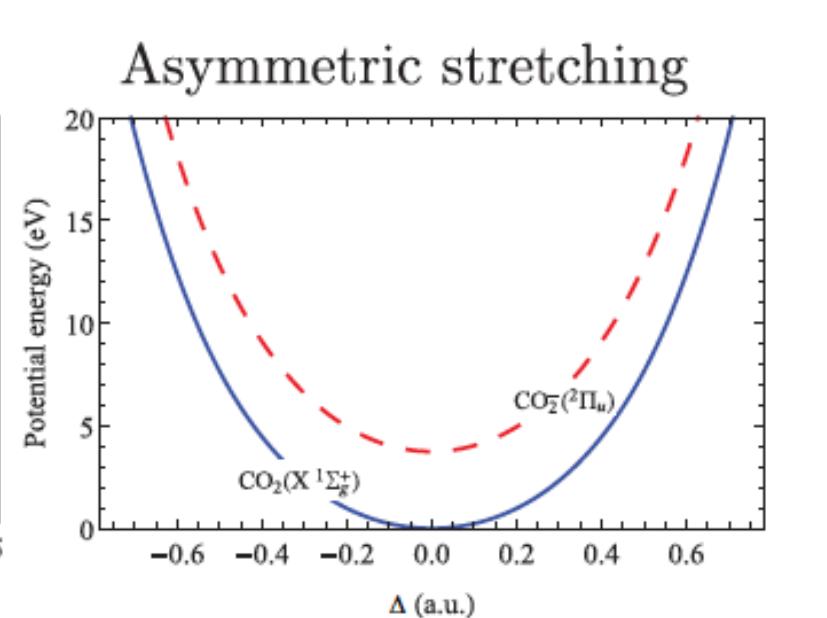
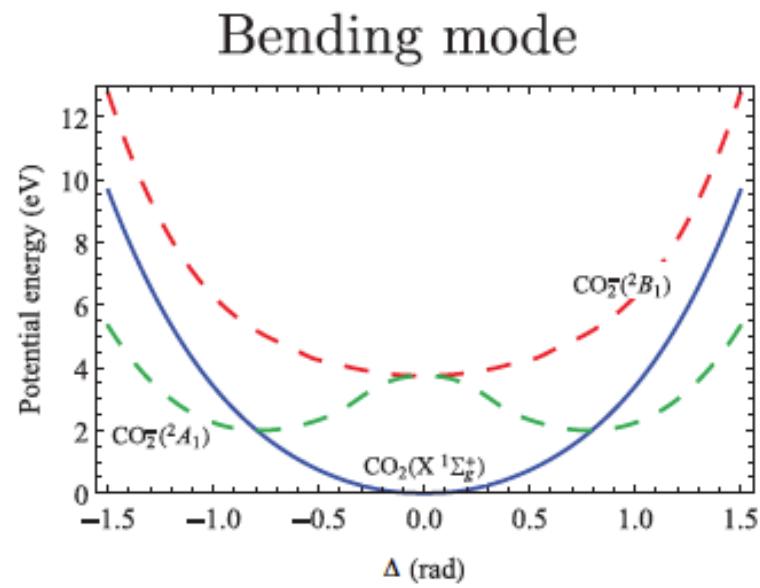
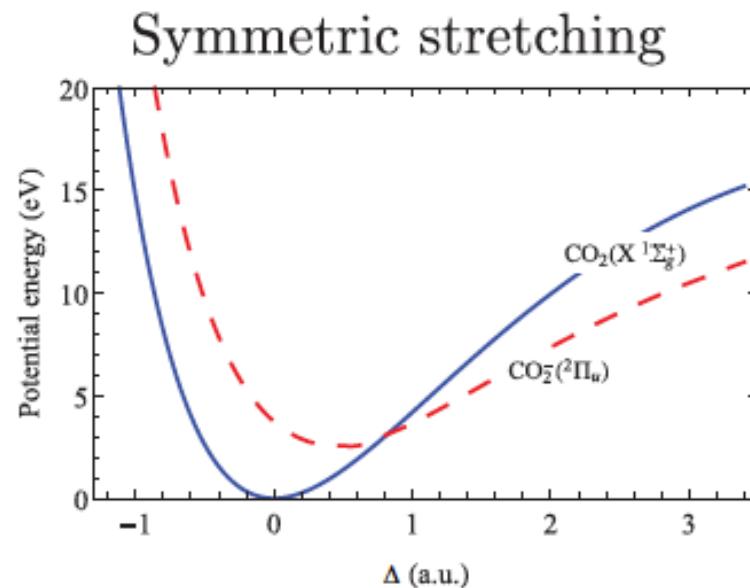
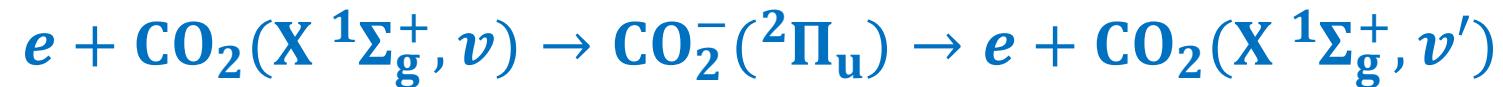
12 VALENCE ORBITALS: ( 5A<sub>1</sub> + 2B<sub>1</sub> + 4B<sub>2</sub> + 1A<sub>2</sub> )<sup>16</sup>

## Letter

# Calculated low-energy electron-impact vibrational excitation cross sections for CO<sub>2</sub> molecule

V Laporta<sup>1,2</sup>, J Tennyson<sup>2</sup> and R Celiberto<sup>1,3</sup>

## Vibrational-excitation



**R-Matrix** potential energy curves

## Letter

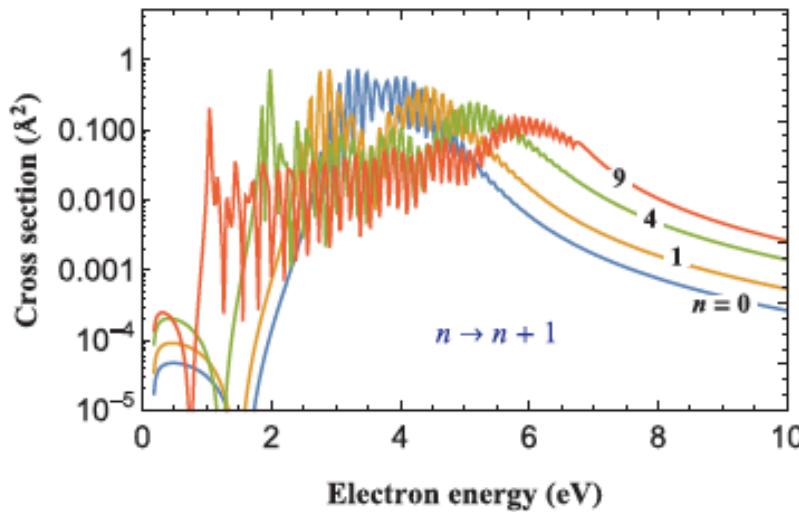
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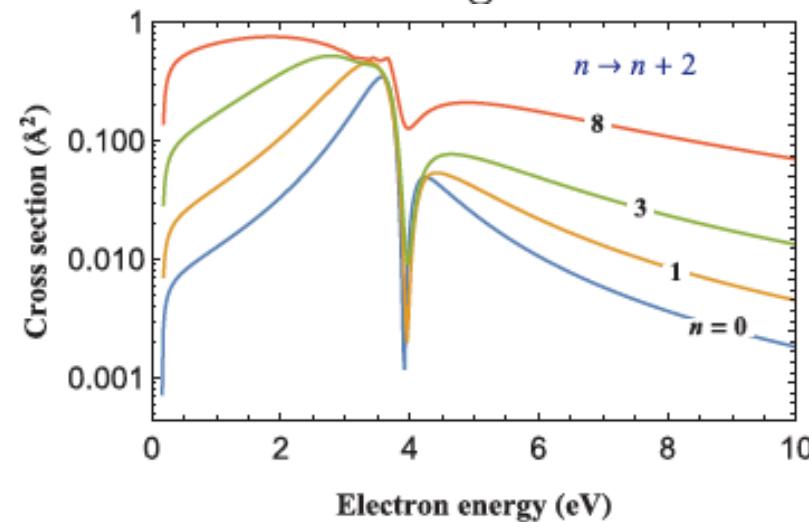
## Vibrational-excitation



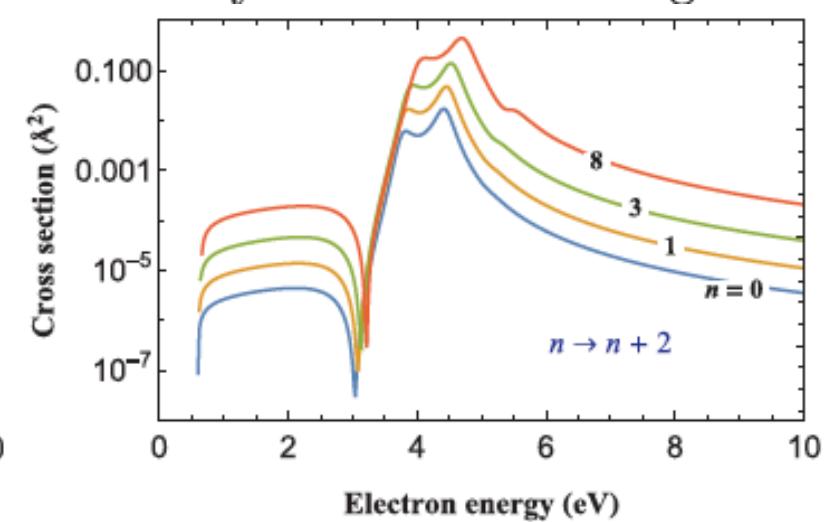
### Symmetric stretching



### Bending mode



### Asymmetric stretching



## Dissociative-attachment for CO<sub>2</sub>



## Dissociative-excitation for CO<sub>2</sub>



### CO<sub>2</sub>/CO<sub>2</sub><sup>-</sup>

MOLPRO (MRCl model, aug-cc-pVQZ basis set, C<sub>2v</sub>):

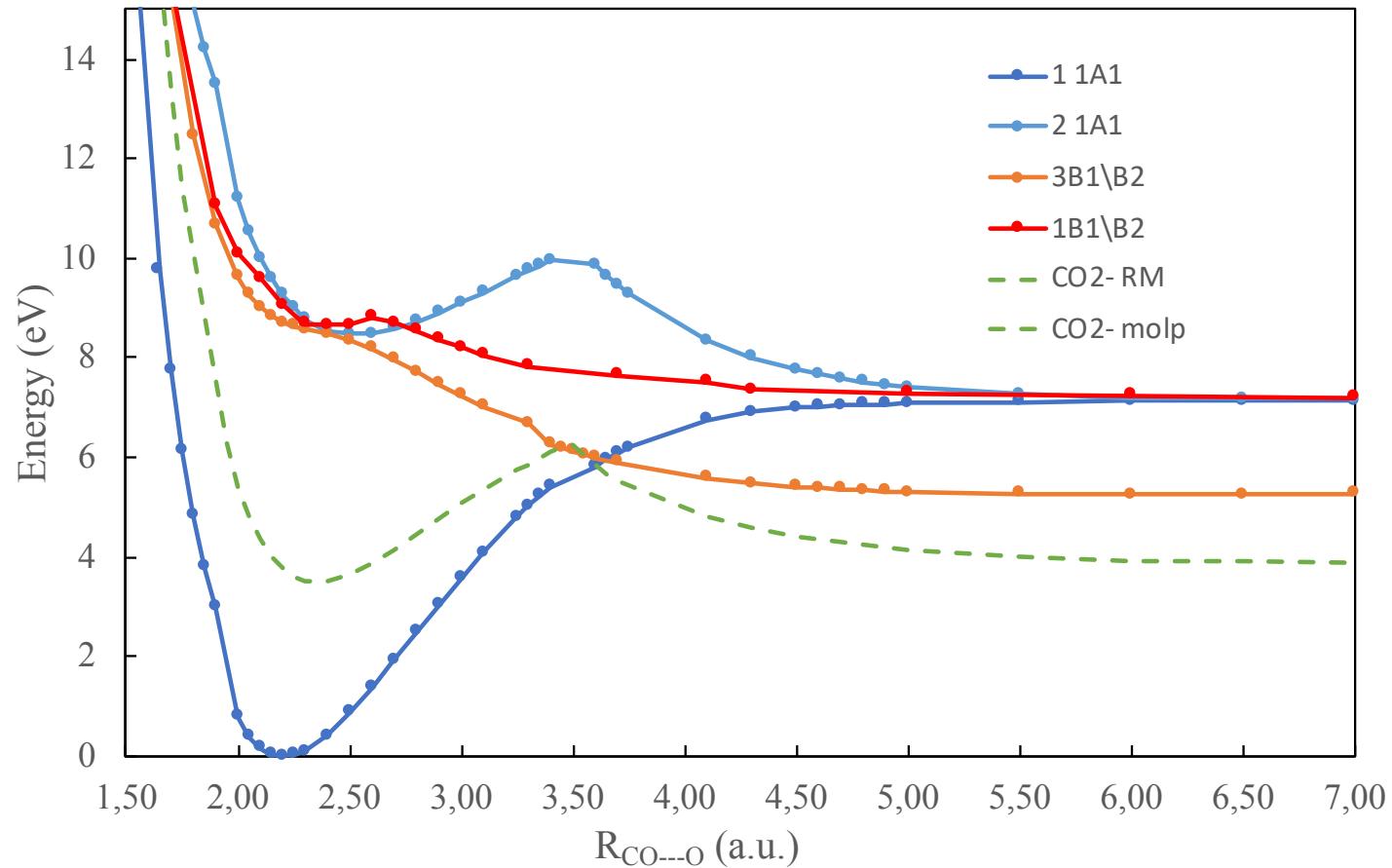
5 CORE ORBITALS: ( 5A<sub>1</sub> + 0B<sub>1</sub> + 0B<sub>2</sub> + 0A<sub>2</sub> )<sup>10</sup>

10 VALENCE ORBITALS: ( 4A<sub>1</sub> + 3B<sub>1</sub> + 3B<sub>2</sub> + 0A<sub>2</sub> )<sup>16</sup>

## Dissociative-attachment for CO<sub>2</sub>



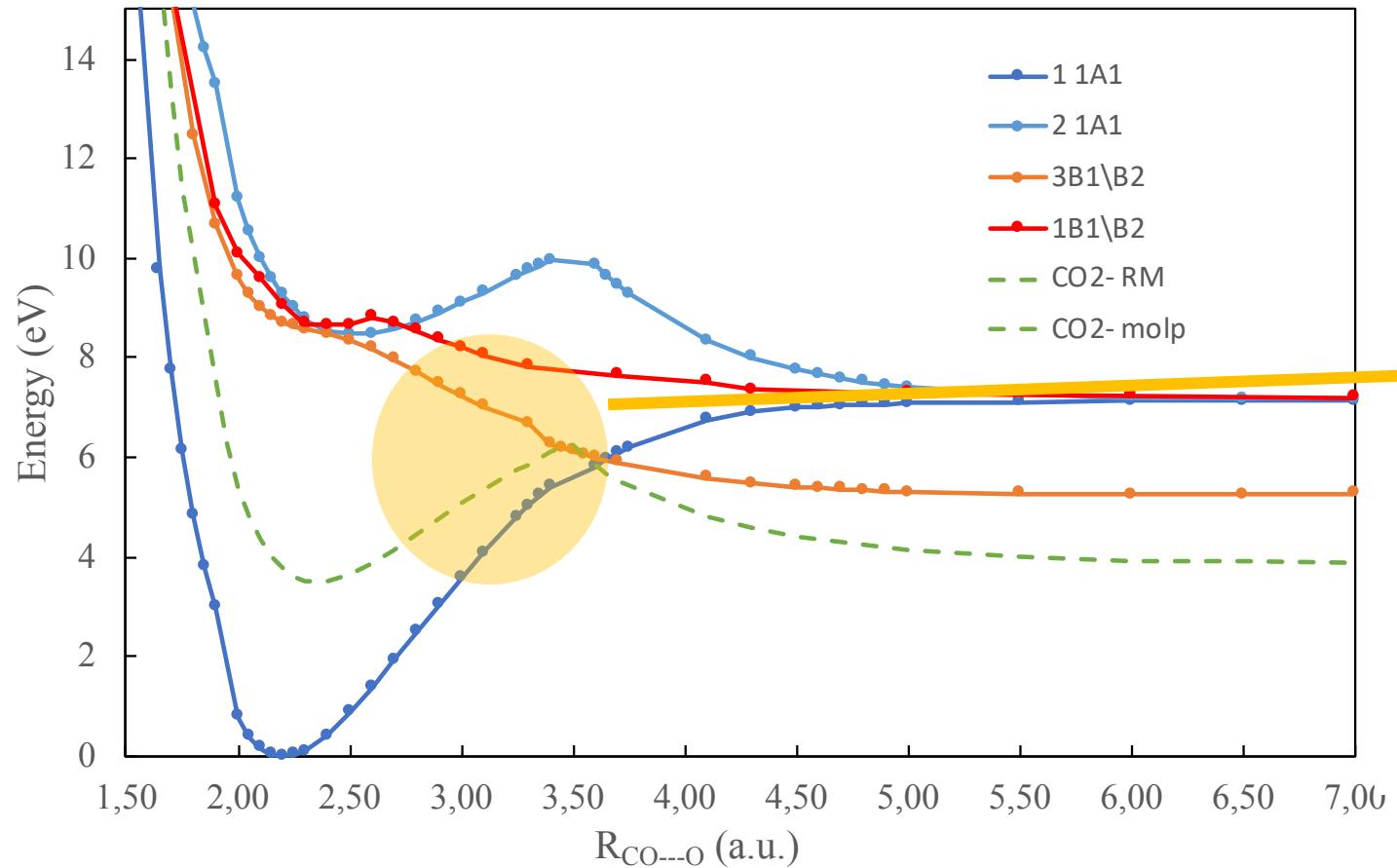
## Dissociative-excitation for CO<sub>2</sub>



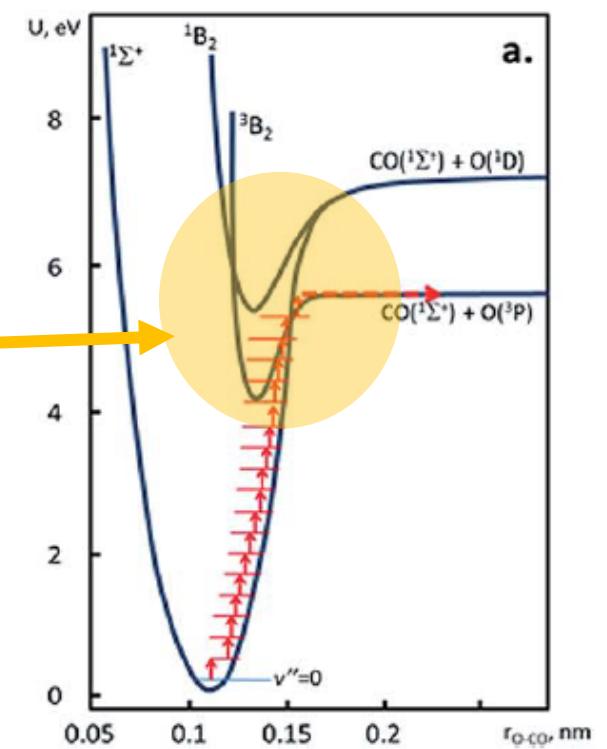
Abdillah Abdoulanziz

In preparation...

## Dissociative-attachment for CO<sub>2</sub>



## Dissociative-excitation for CO<sub>2</sub>



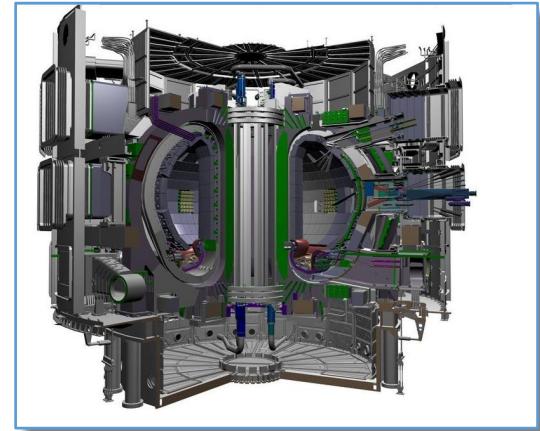
Abdillah Abdoulanziz

In preparation...

## Plan of the presentation:

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3. Conclusions and perspectives

# electron-BeH<sup>+</sup> and -BeD<sup>+</sup> scattering

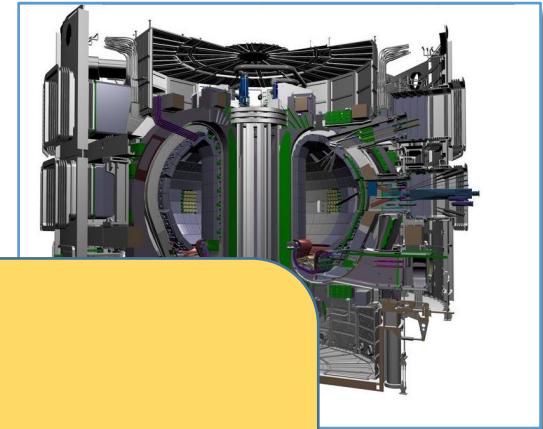


I.T.E.R.

V. Laporta, K. Chakrabarti, et al., *Plasma Phys. Control. Fusion* **59**, 045008 (2017)

S. Niyonzima, V. Laporta, et al., *Plasma Sources Sci. Technol.* **27**, 025015 (2018)

# electron-BeH<sup>+</sup> and -BeD<sup>+</sup> scattering



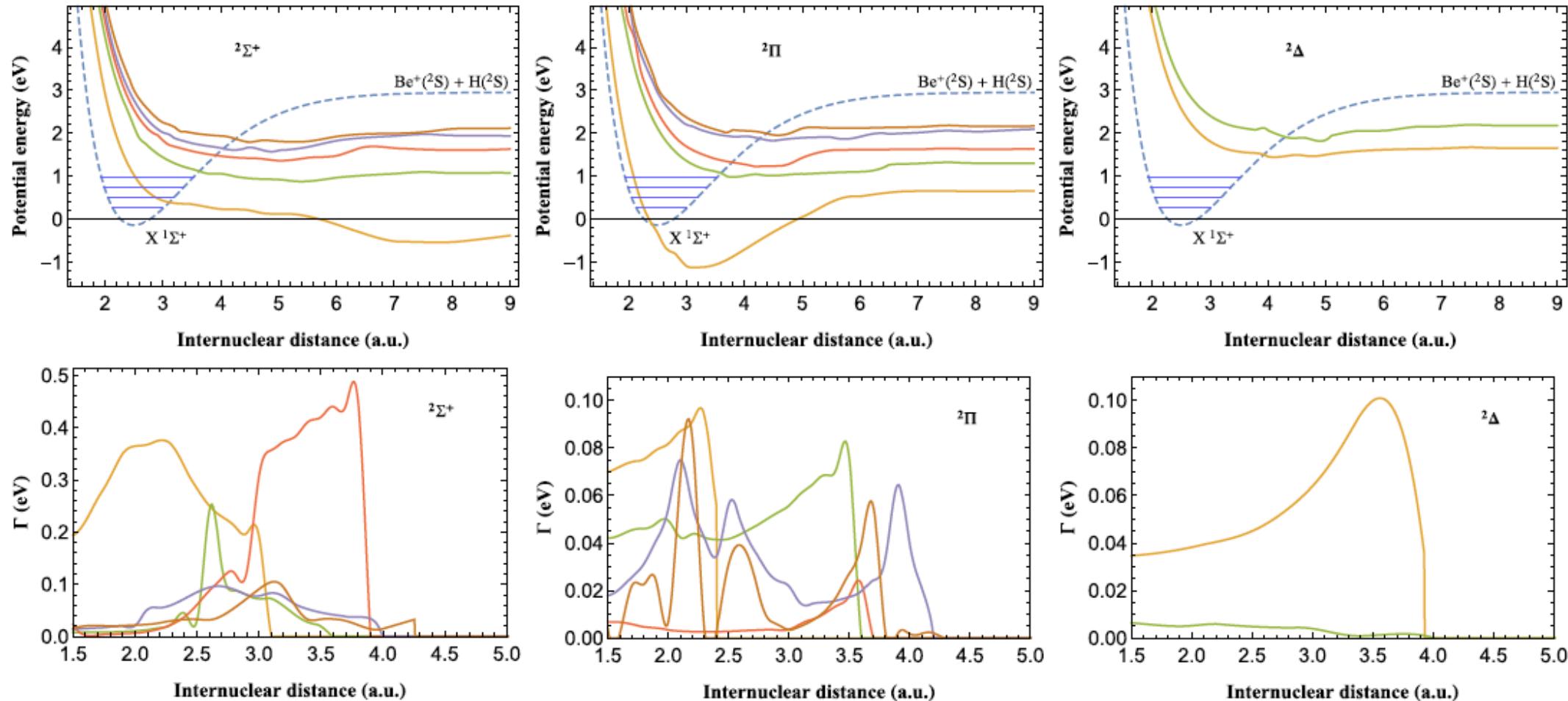
plasmas Be-wall interaction

E.R.

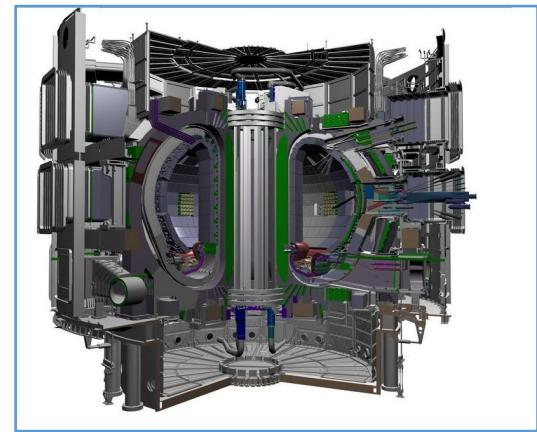
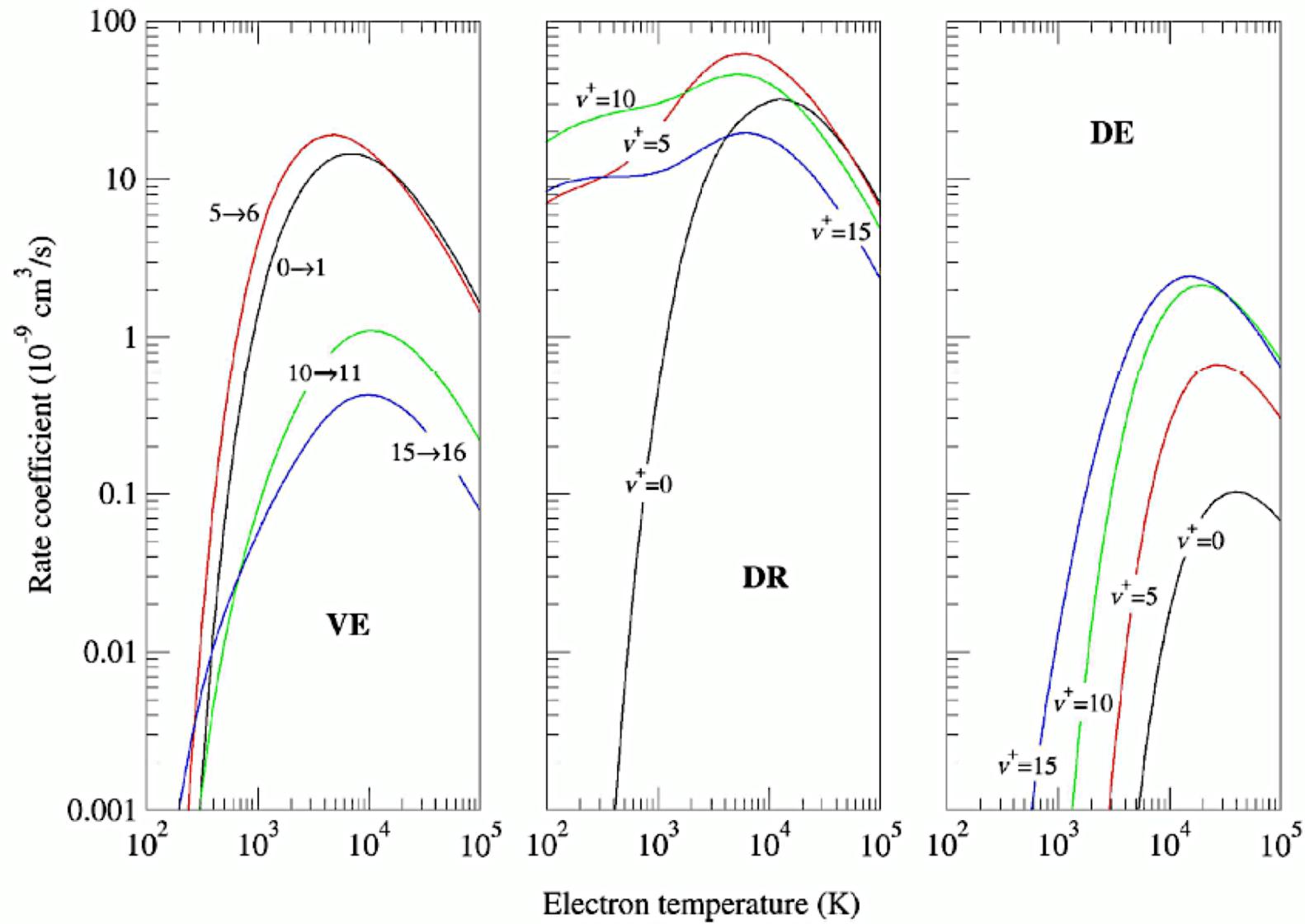
V. Laporta, K. Chakrabarti, et al., *Plasma Phys. Control. Fusion*

S. Niyonzima, V. Laporta, et al., *Plasma Sources Sci. Technol.*

## Potential energy curves and couplings

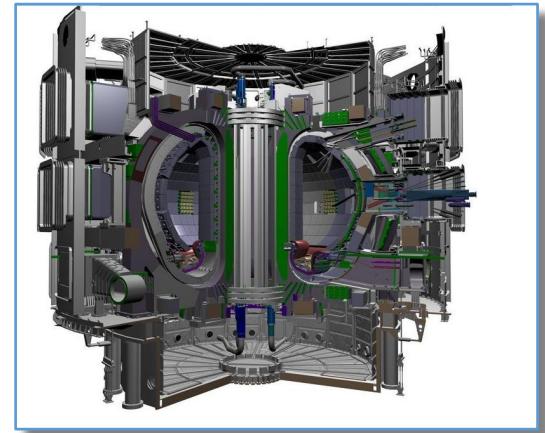
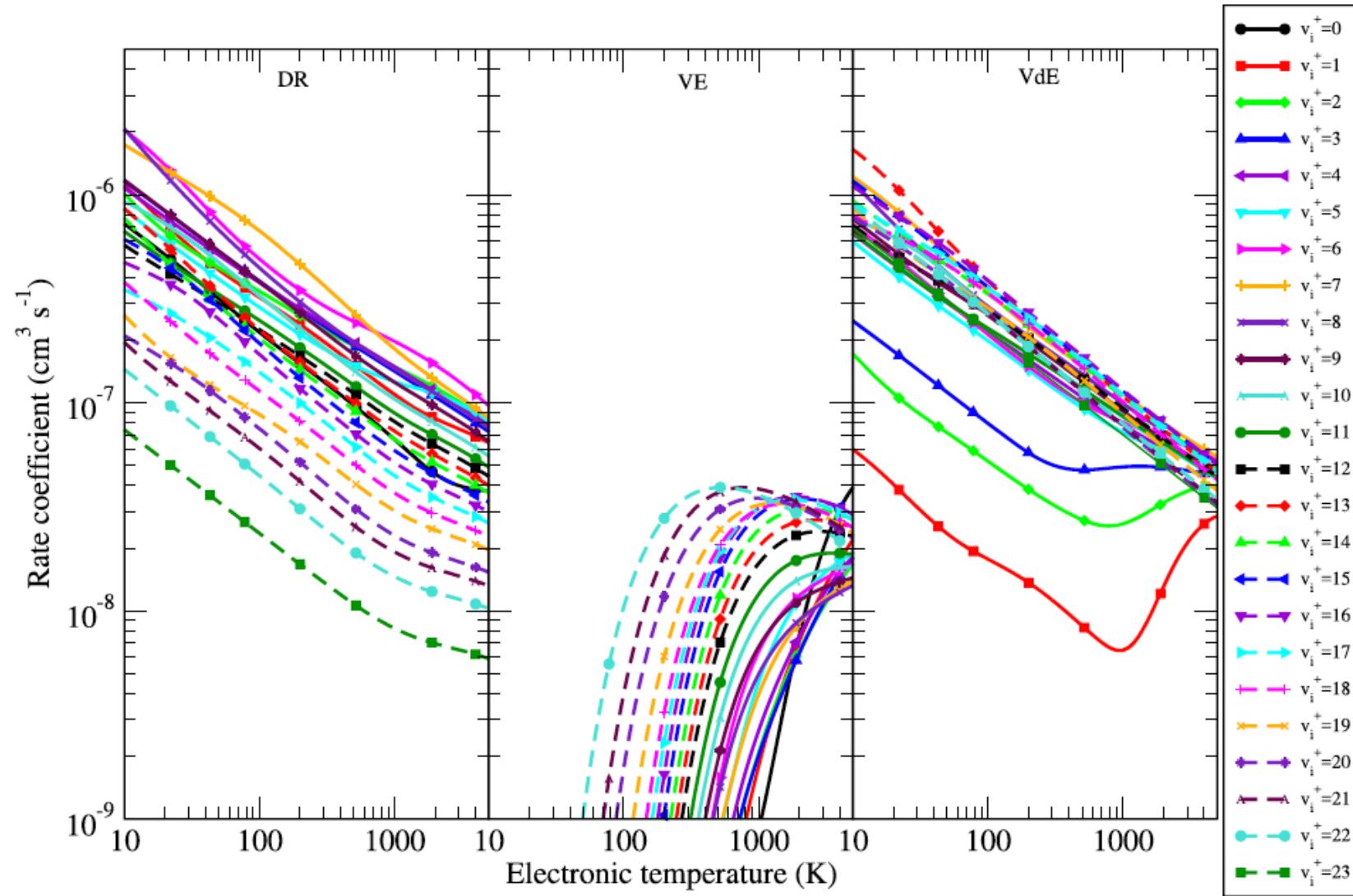


**Figure 1.** Potential energy curves (top line) and widths (bottom line) for  $\text{BeH}^{**}$  resonant states in  $^2\Sigma^+$ ,  $^2\Pi$  and  $^2\Delta$  scattering channels for  $j^+ = 0$ . Dashed line refers to potential energy curve for  $\text{BeH}^+$  ground electronic state where the first vibrational levels are marked.

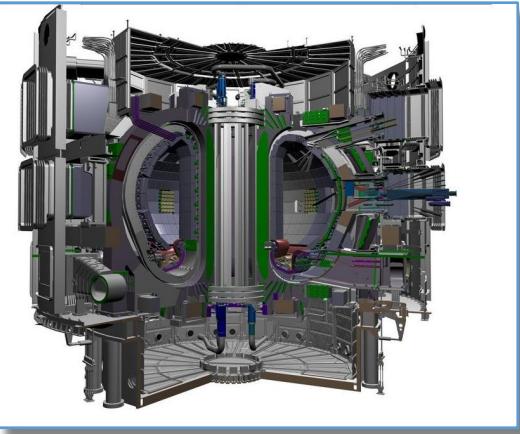


I.T.E.R.

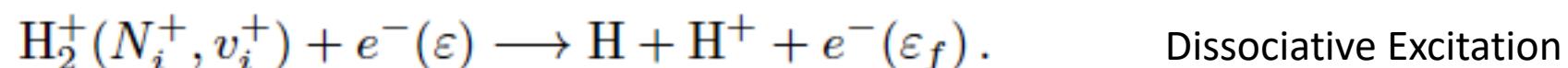
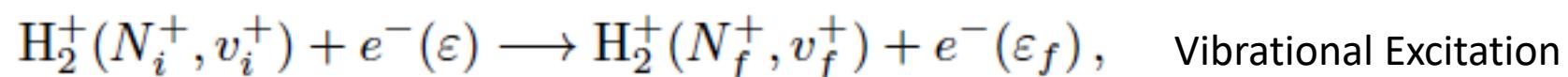
# $e + \text{BeD}^+$

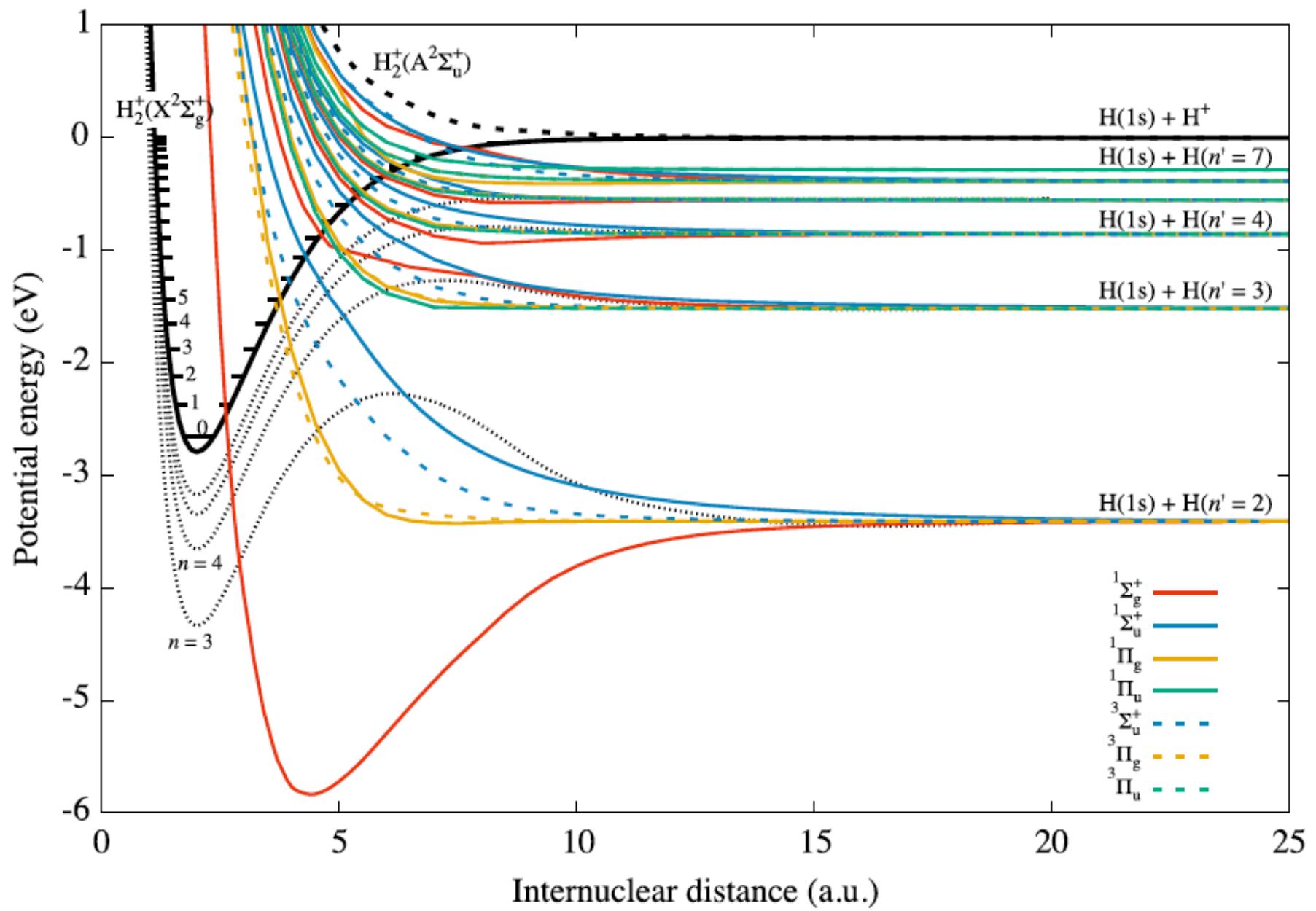


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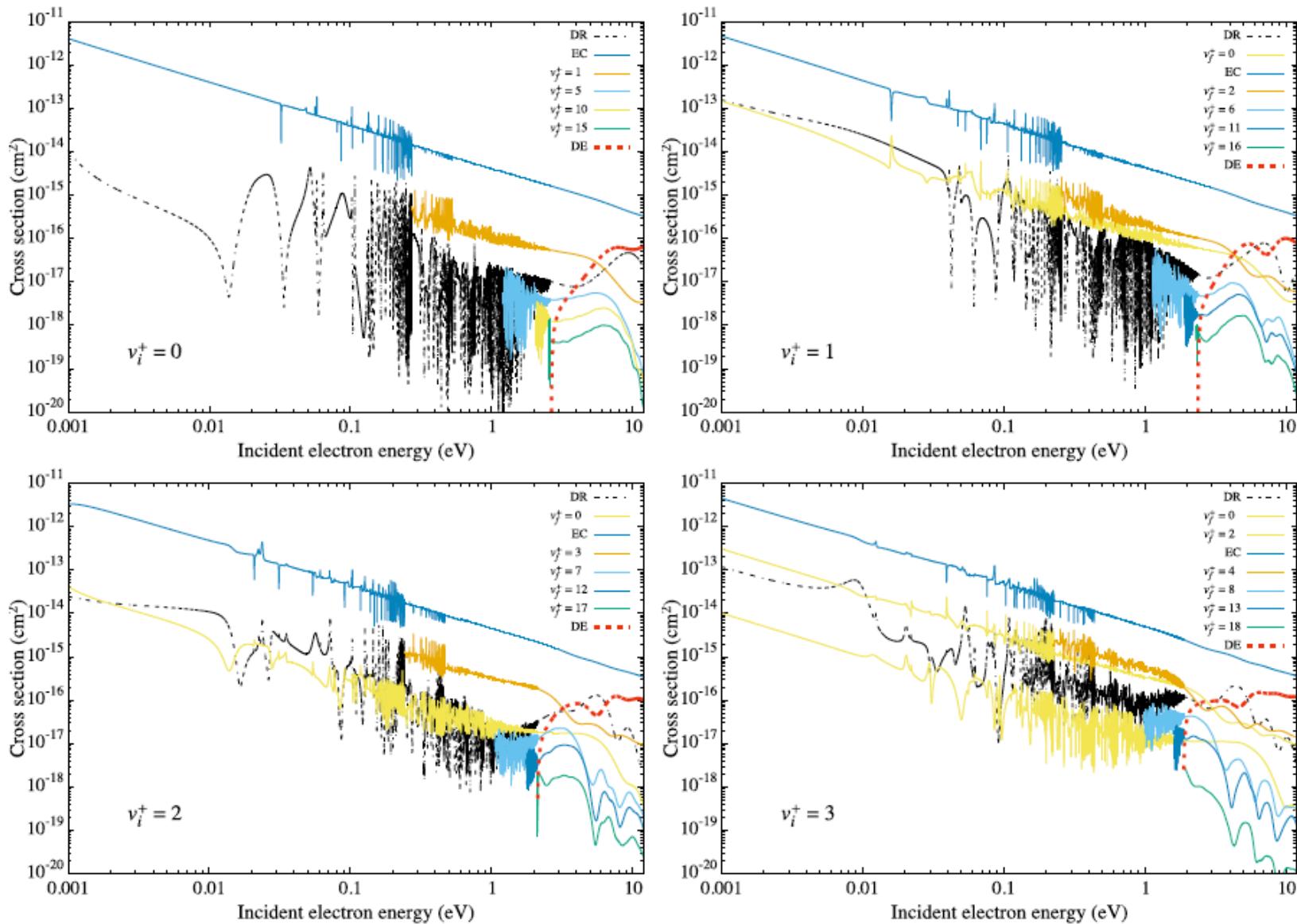


## electron-H<sub>2</sub><sup>+</sup>

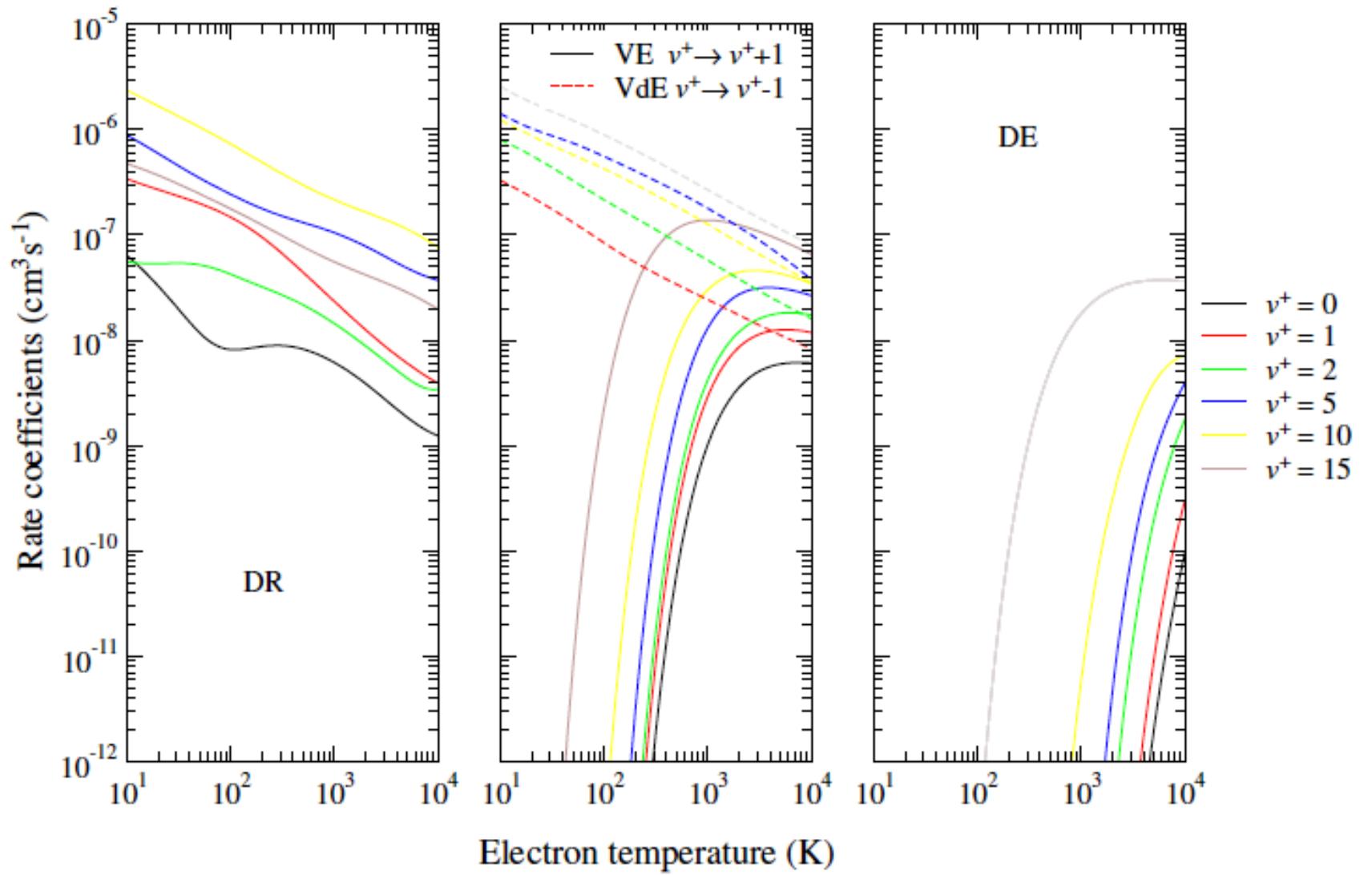




# electron-H<sub>2</sub><sup>+</sup>

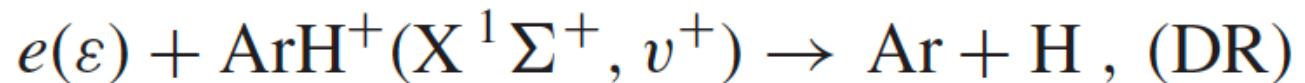


# electron-H<sub>2</sub><sup>+</sup>

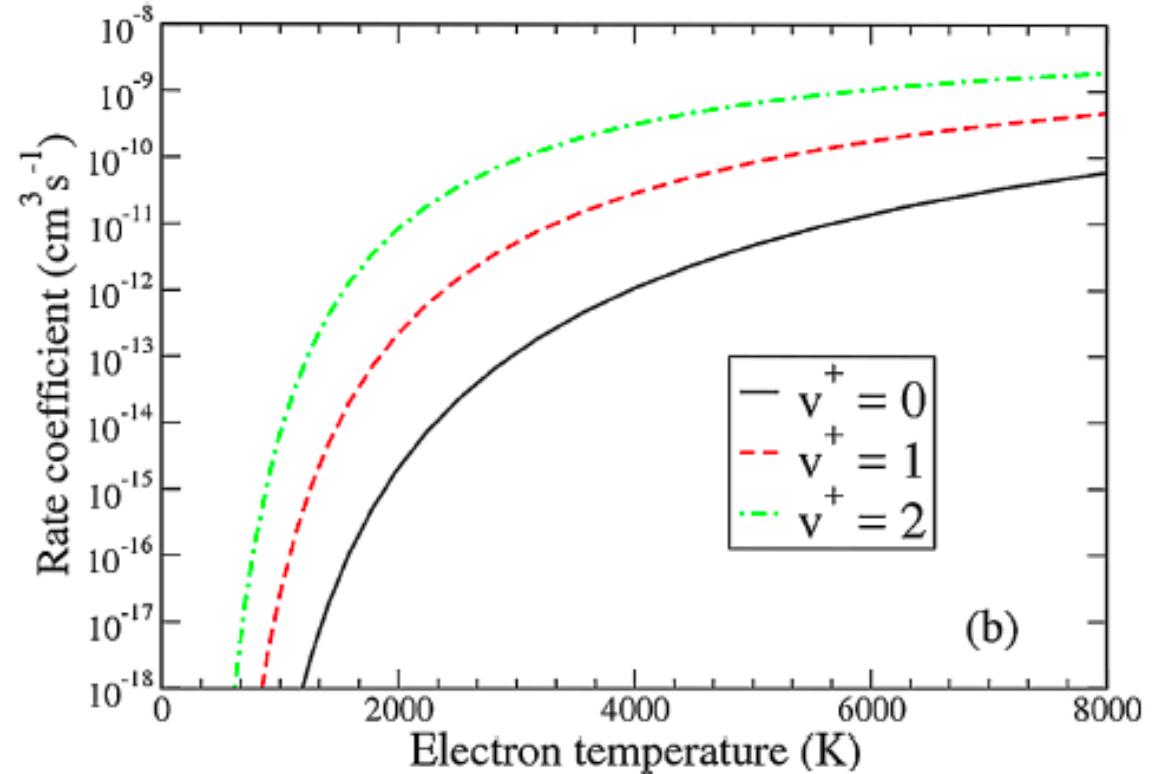
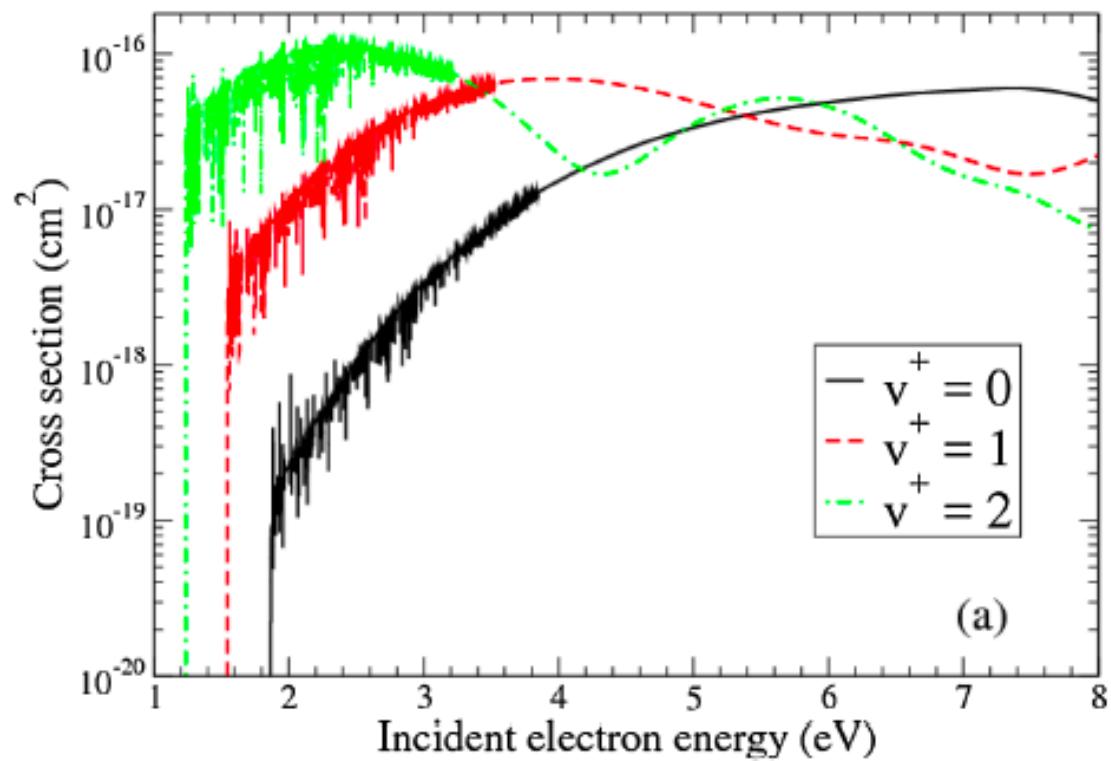
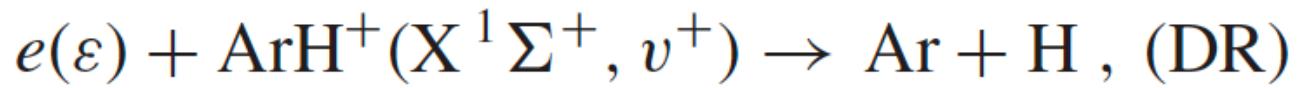




# e + ArH<sup>+</sup> collisions

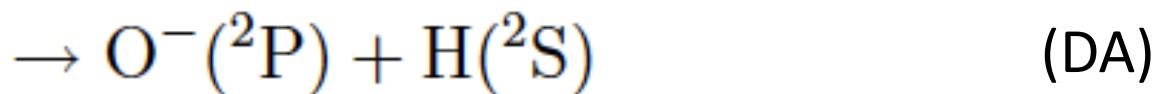
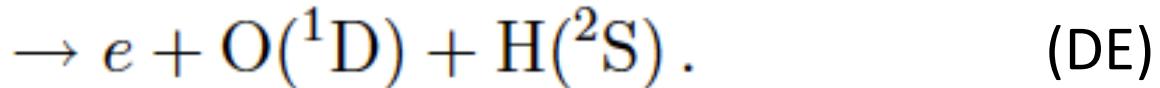
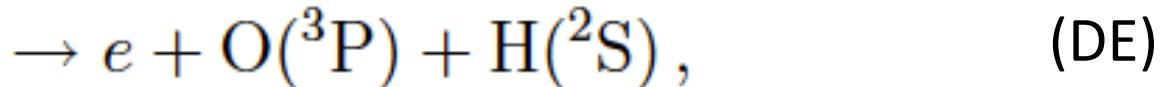
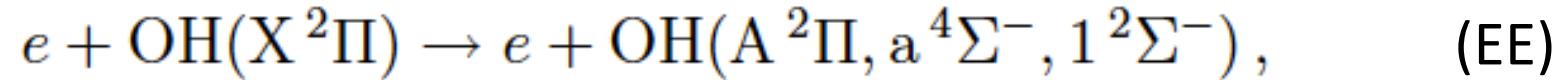


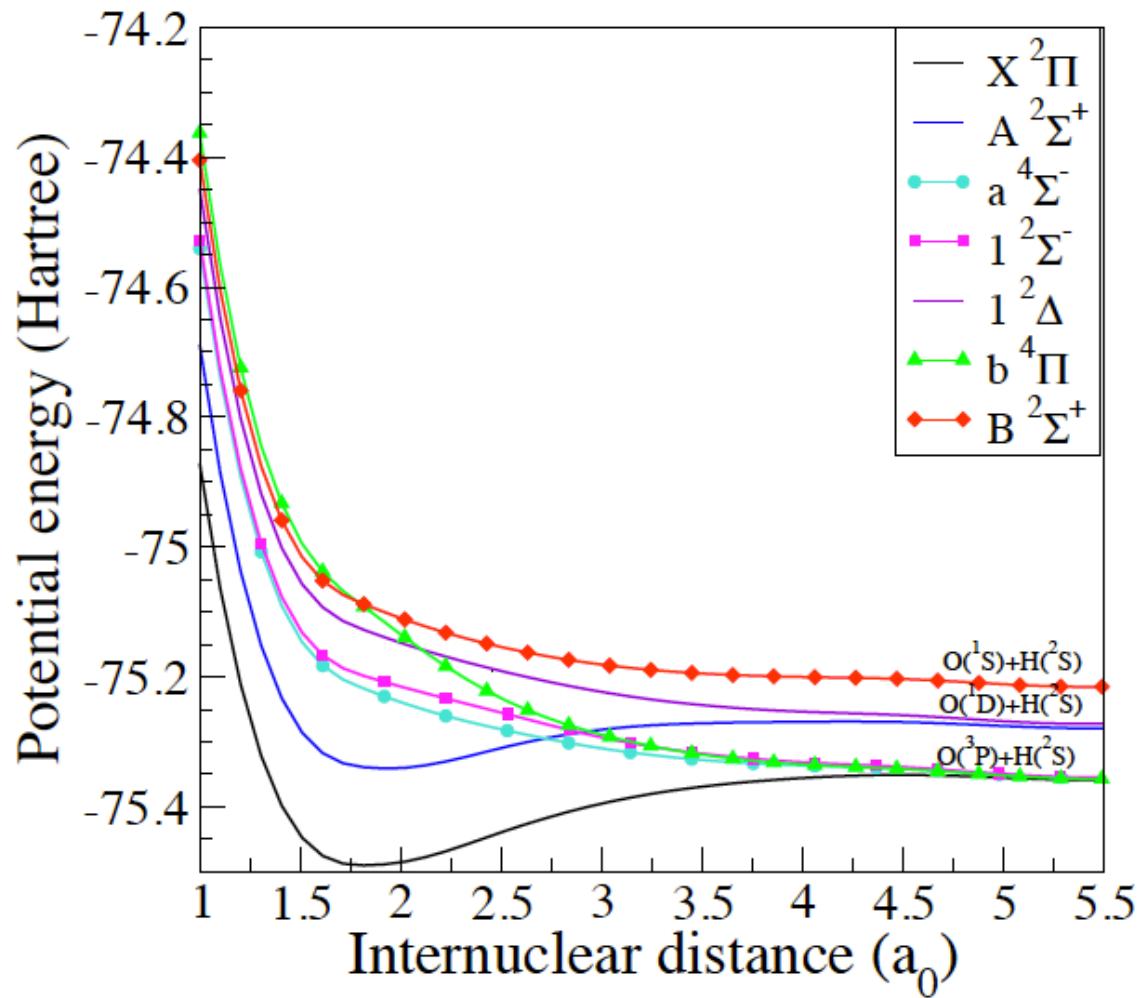
A. Abdoulanziz, F. Colboc, D.A. Little, Y. Moulane, J.Zs. Mezei, E. Roueff, J. Tennyson,  
I.F. Schneider and V. Laporta, [MNRAS 479, 2415 \(2018\)](#)

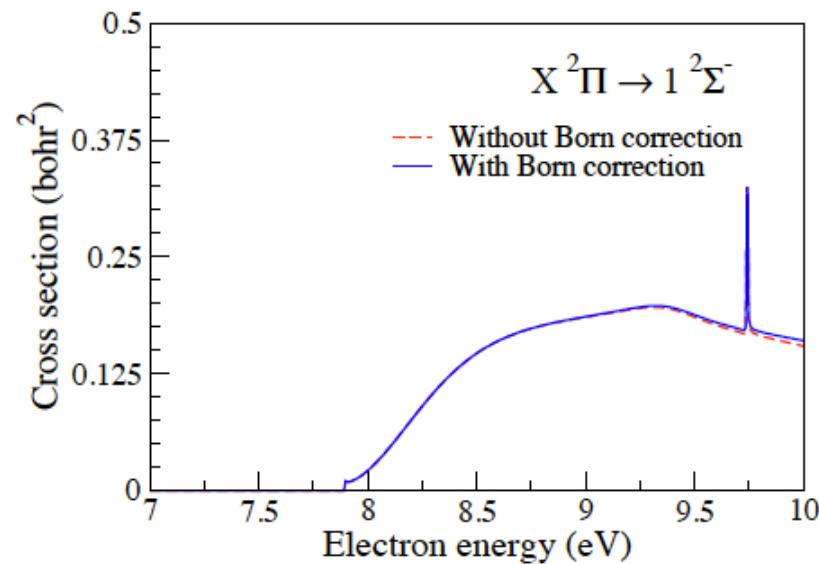
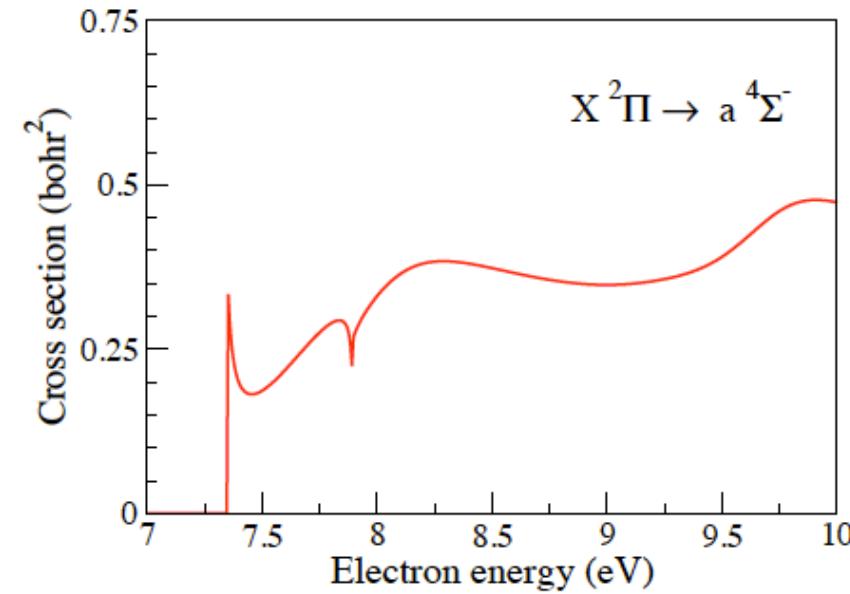
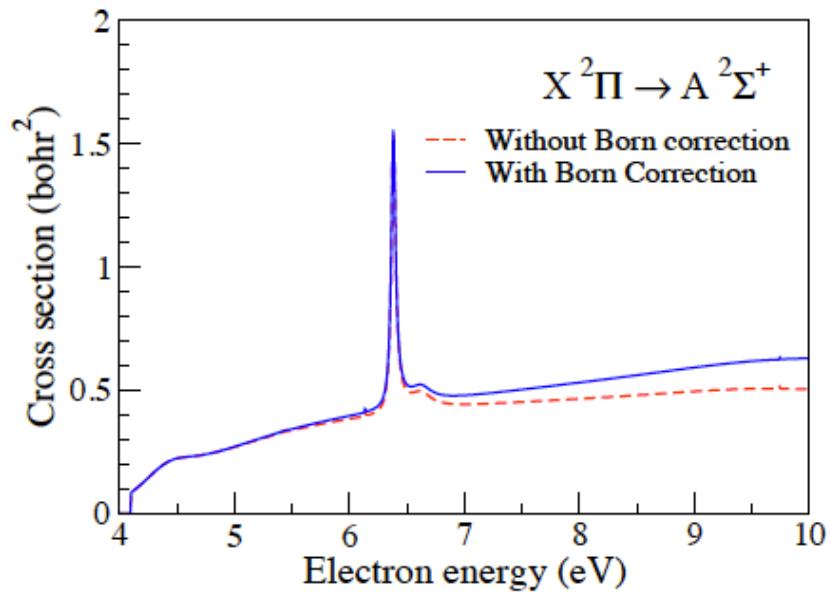


A. Abdoulanziz, F. Colboc, D.A. Little, Y. Moulane, J.Zs. Mezei, E. Roueff, J. Tennyson, I.F. Schneider and V. Laporta, [MNRAS 479, 2415 \(2018\)](#)

# ***e + OH collisions***

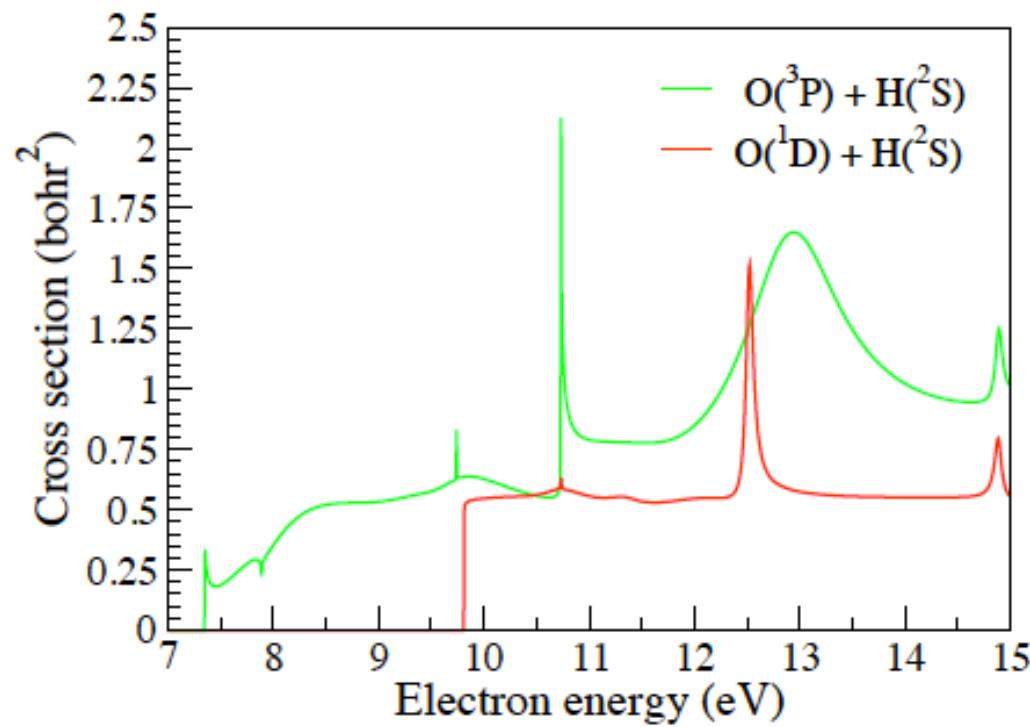




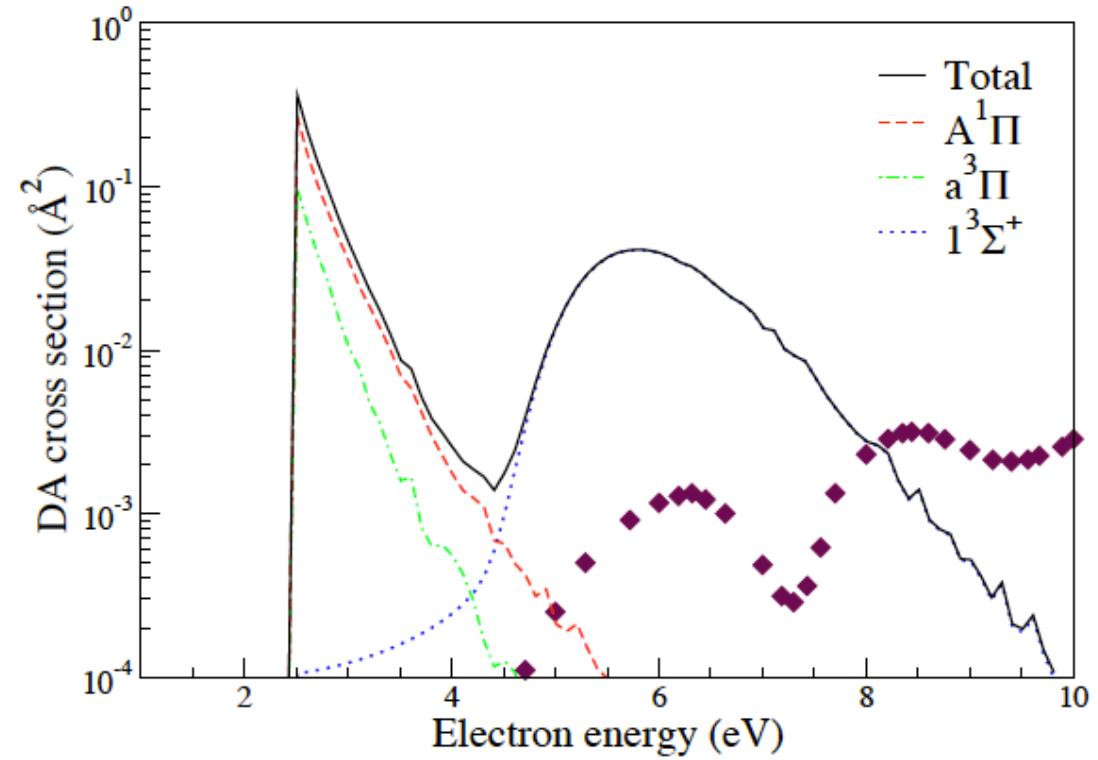


@  $R=R_{eq}$

## *Dissociation*



## *Dissociative electron attachment*

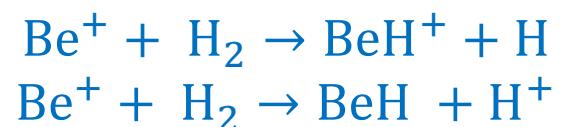


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## Conclusions and perspectives

- *Ab-initio* molecular Quantum dynamics;
- State specific cross sections and rate coefficients for vibrational excitation, dissociative attachment, dissociative recombination and dissociative excitation processes;
- Non-equilibrium molecular plasmas modelling;
- Extensions to atom-molecule and molecule-molecule scattering in particular for the reaction:



- Data base for  $e + \text{H}_2$  and  $e + \text{H}_2^+$  collisions.



Jonathan Tennyson  
(University College London, UK)



Ioan F. Schneider  
(Université du Havre, France)



Kalyan Chakrabarti  
(Scottish Church College, India)



Arnaud Bultel  
(CORIA, Rouen, France)



Marco Panesi  
(University of Illinois, (IL) USA)



Mario Capitelli  
(CNR, Bari, Italy)



Savino Longo  
(Università di Bari, Italy)

Thank you for your attention



# Carte du monde "électron-molécule"



# Carte du monde "électron-molécule"



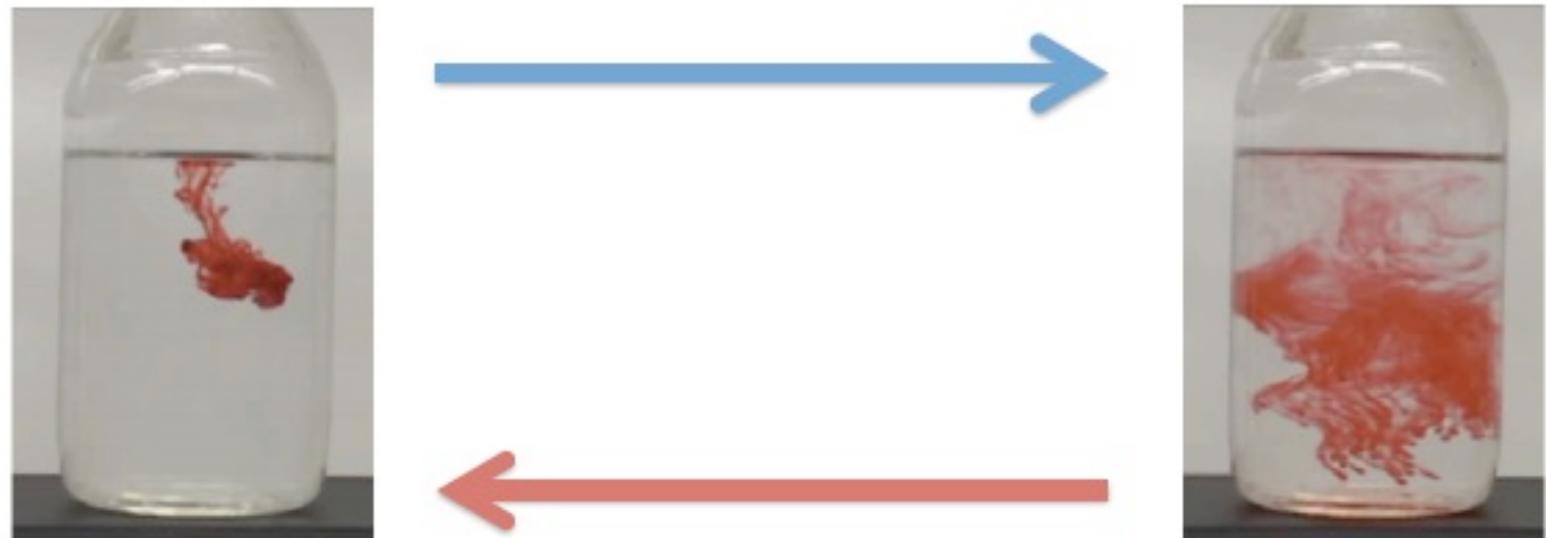
# Carte du monde "électron-molécule"



## Non-equilibrium molecular plasmas modelling

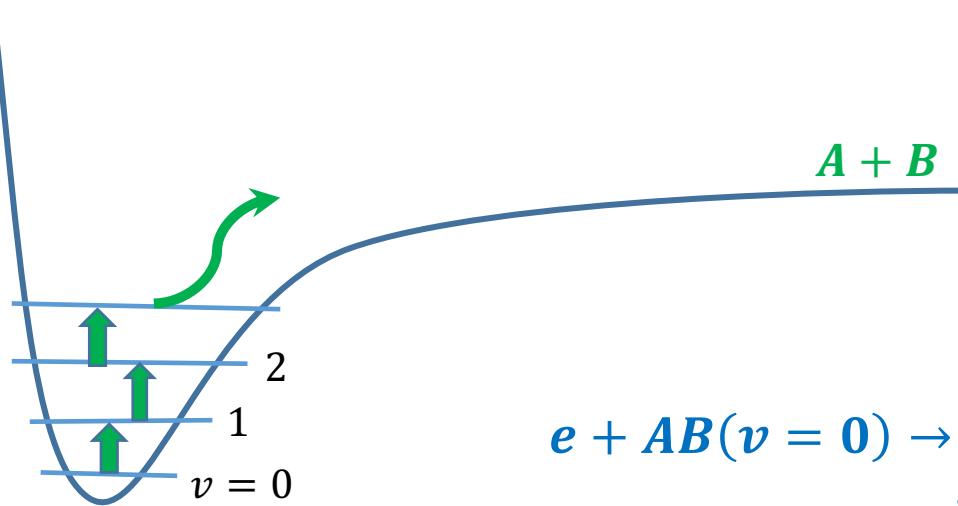
- *Non-equilibrium thermodynamics* is an extension of equilibrium thermodynamics it attempts to describe the physical processes in their time-courses in continuous detail.
- A central role in non-equilibrium thermodynamics is played by transport equations which are the corresponding to equations of state in equilibrium thermodynamics.
- Transport equations describe the amount of heat, mass, electrical charge... which are transferred per unit time between different systems and different regions of a system as a response to a non-homogeneity in temperature  $T$ , molar concentration  $c$ , electric potential  $\varphi_e$ ...

$$\begin{aligned} q &= -\lambda \nabla T \quad (\text{Fourier's law}), \\ J &= -D \nabla c \quad (\text{Fick's law}), \\ I &= \sigma_e \nabla \varphi_e \quad (\text{Ohm's law}). \end{aligned}$$

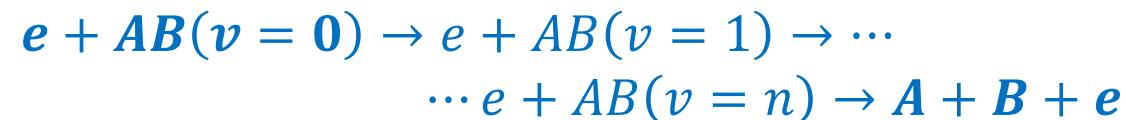


# Applications: non-equilibrium dissociation mechanism

- Despite its apparent simplicity, the dissociation rate for a molecule is very difficult to be determined
- Polak shows that experimental dissociation rates cannot be reproduced by direct electron impact dissociation involving vibrational ground state of molecules.
- The “pure-vibrational-mechanism” is the theoretical framework to explain the dissociation rate

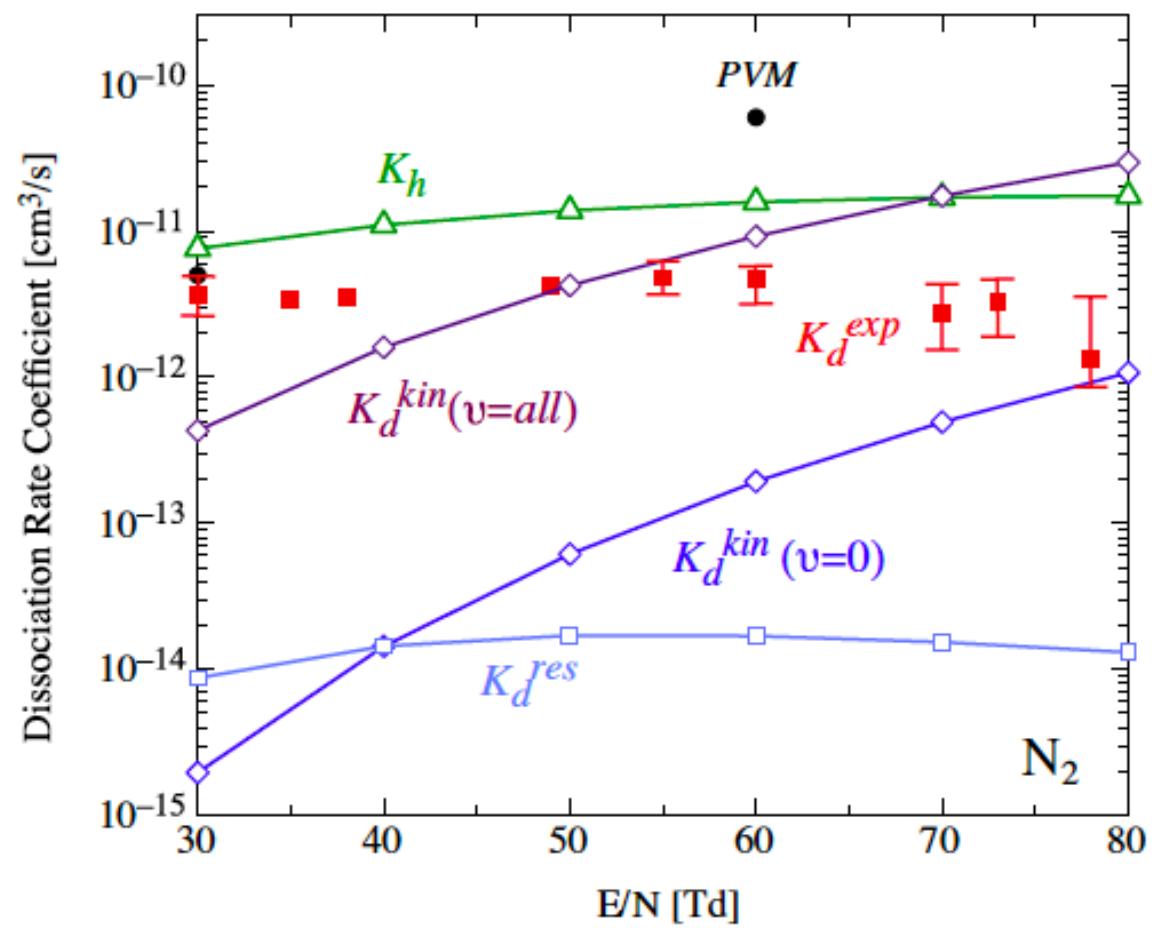
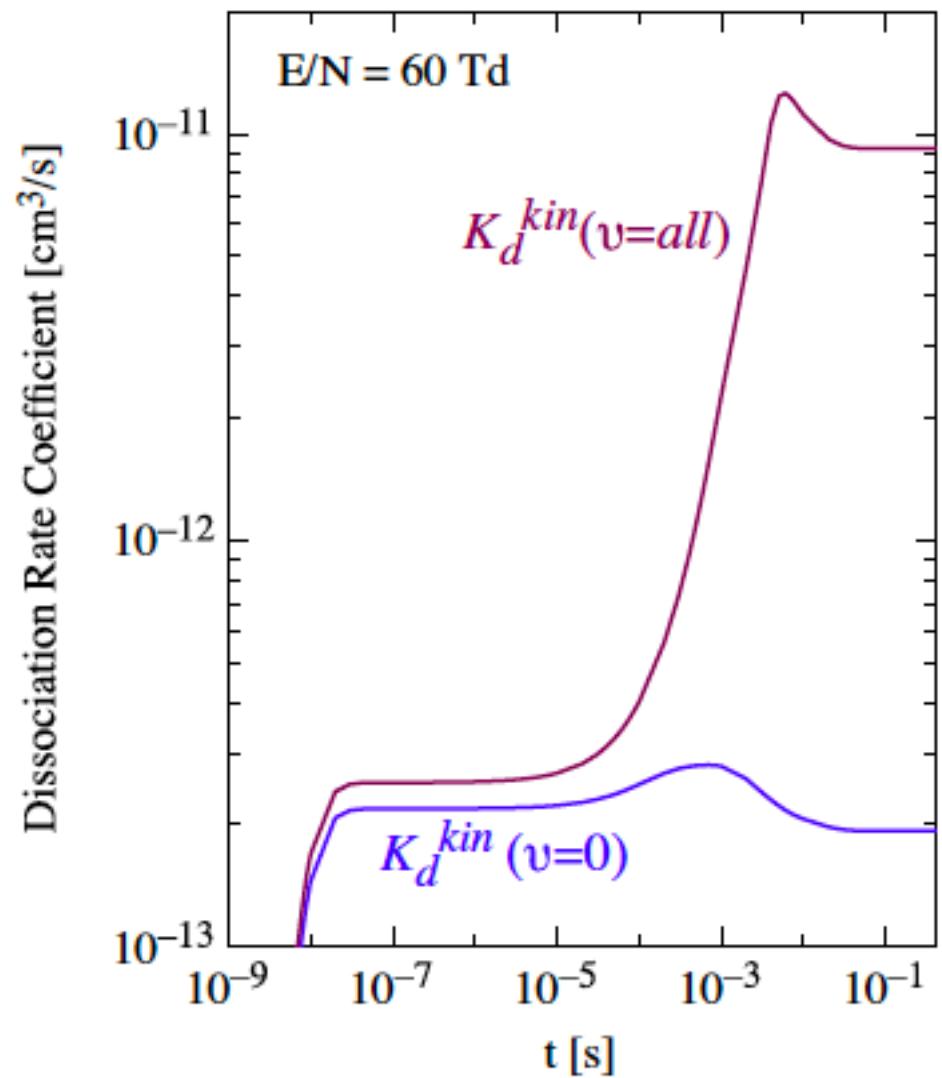


$$k_d^{kin} = \sum_{v=0}^{v_{max}} k_d^{kin}(v) \frac{N_v}{N_{tot}}$$



M. Capitelli, G. Colonna, V. Laporta et al., Chemical Physics 438, 31 (2014)





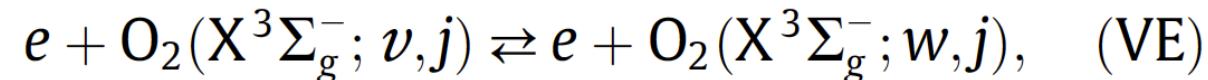
## **Titres universitaires :**

2007 – Doctorat en physique, Université de Bari, Italie (séjours à Lyon et au CERN à Genève)  
2010 – Qualification pour maitre de conférences - section 29 (France)  
2017 – Qualification pour maitre de conférences - section 30 (France)  
2017 – Habilitation scientifique national - section 02/B2 et 03/A2 (Italie)  
2017 – Habilitation à Diriger les Recherches, Université du Havre, France  
2018 – Qualification pour professeur - section 30 (France)

## **Parcours professionnel après la thèse :**

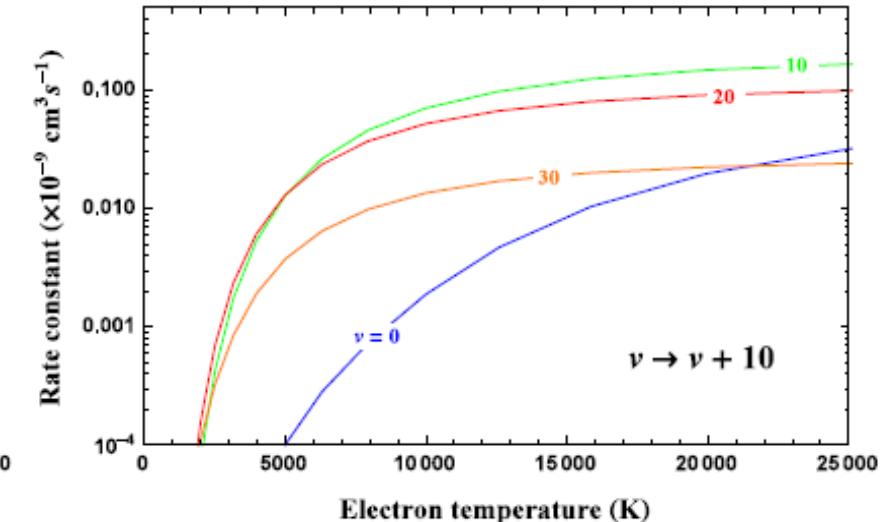
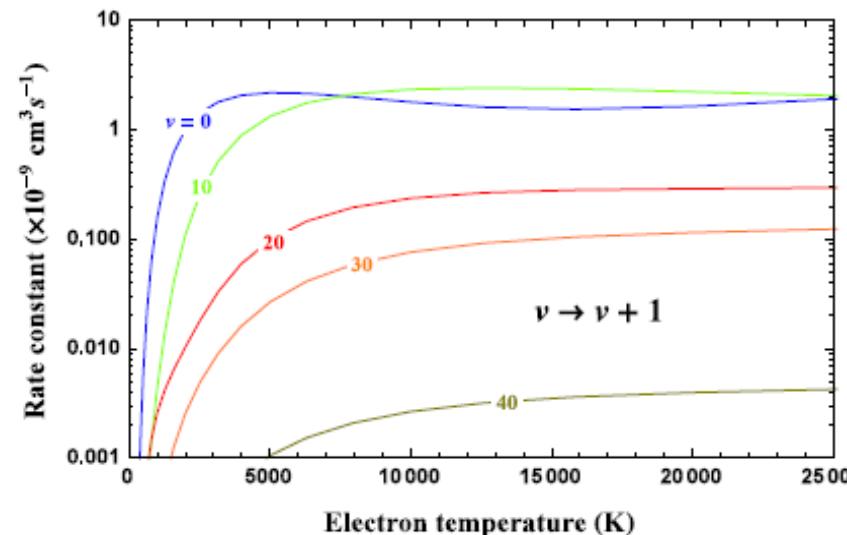
2006 – 2007 Centre de Physique Théorique, CNRS-École Polytechnique, Palaiseau Cedex, France  
2007 – 2009 Dipartimento interateneo di fisica, Università di Bari, Italia  
2009 – 2010 Institut de Physique Nucléaire de Lyon, Université Claude Bernard Lyon-1, France (**A.T.E.R.**)  
2010 – 2011 Istituto di Metodologie Inorganiche e dei Plasmi, Consiglio Nazionale delle Ricerche, Bari, Italie  
2011 – 2013 Department of Physics and Astronomy, University College London, London (UK); Prof. J. Tennyson  
2013 – 2015 Istituto di Nanotecnologia-CNR et DICATECh-Politecnico di Bari (Italie)  
Juillet 2013 Ames Research Center, NASA, Moffett Field (CA), USA; Prof. R.L. Jaffe;  
2015 – 2015 Ohio Aerospace Institute et Air Force Research Laboratory-WPAFB, Dayton (OH) - USA  
2015 – 2016 Istituto di Nanotecnologia-CNR et DICATECh-Politecnico di Bari (Italie)  
Juin 2017 Aerospace Engineering Department, University of Illinois at Urbana-Champaign (IL-USA)  
De Fevrier 2017 Laboratoire Onde et Milieux Complexes, CNRS-Université du Havre, Le Havre (France)

## *Application: Electron-vibration relaxation in oxygen plasmas*

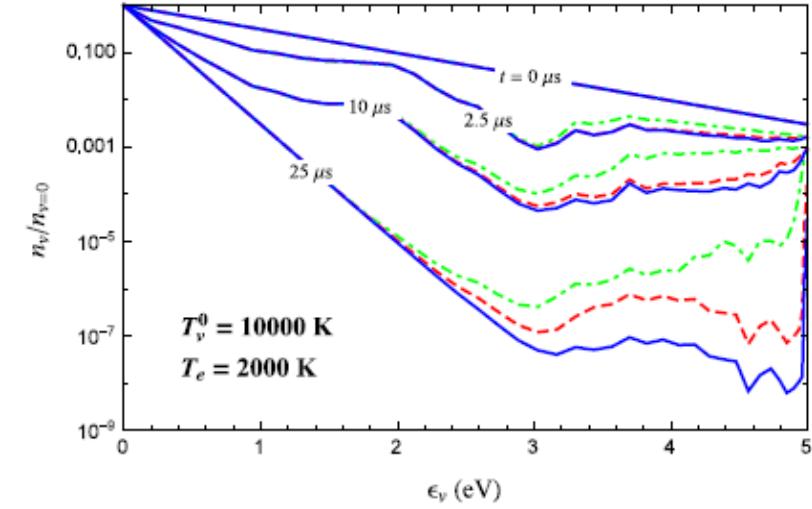
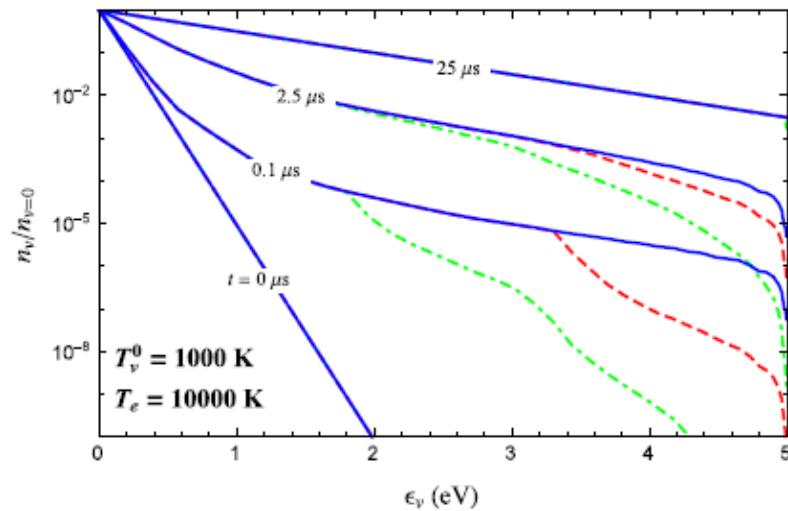


- State-to-State vibrational kinetics
- Vibrational relaxation time is comparable to chemical relaxation: **vibrational non-equilibrium**

$$\frac{dn_\nu}{dt} = n_e \sum_{w \in \mathcal{V}} [k_{w,\nu} n_w - k_{\nu,w} n_\nu], \quad \nu \in \mathcal{V},$$

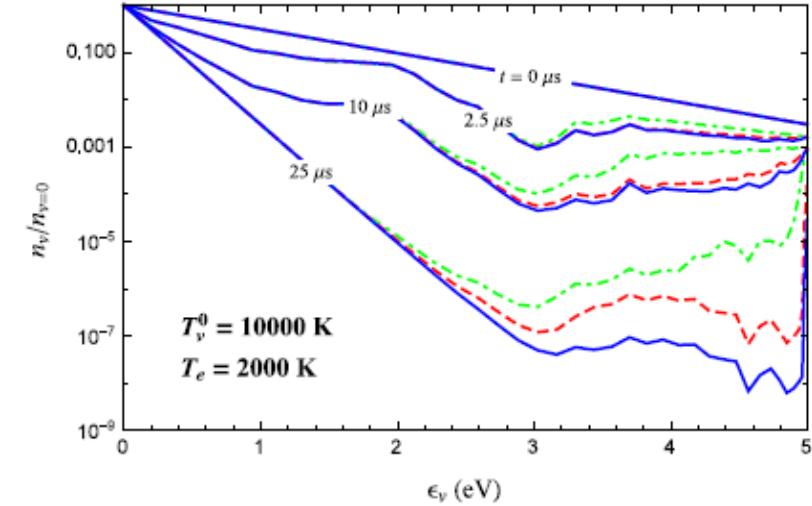
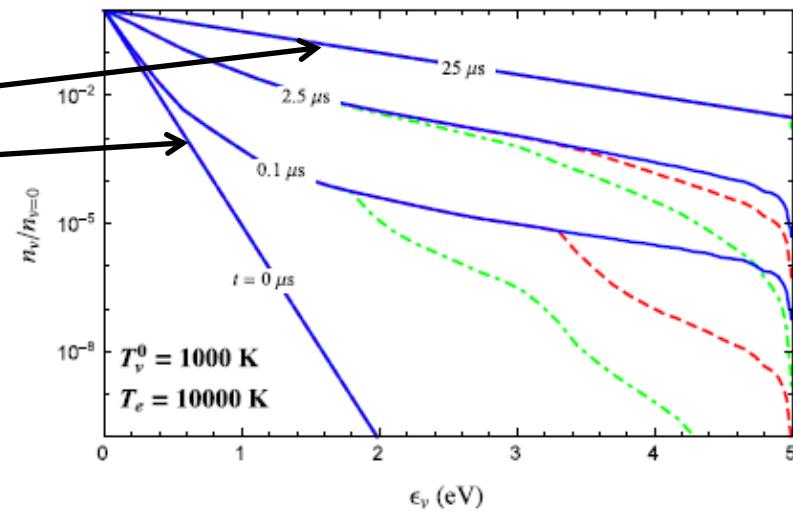


## Time evolution of **non-equilibrium** vibrational distribution function:



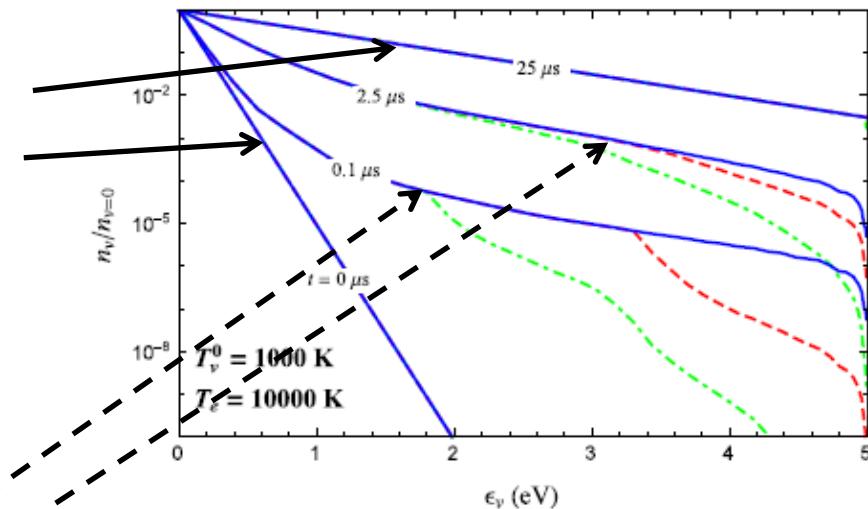
## Time evolution of **non-equilibrium** vibrational distribution function:

Equilibrium distribution

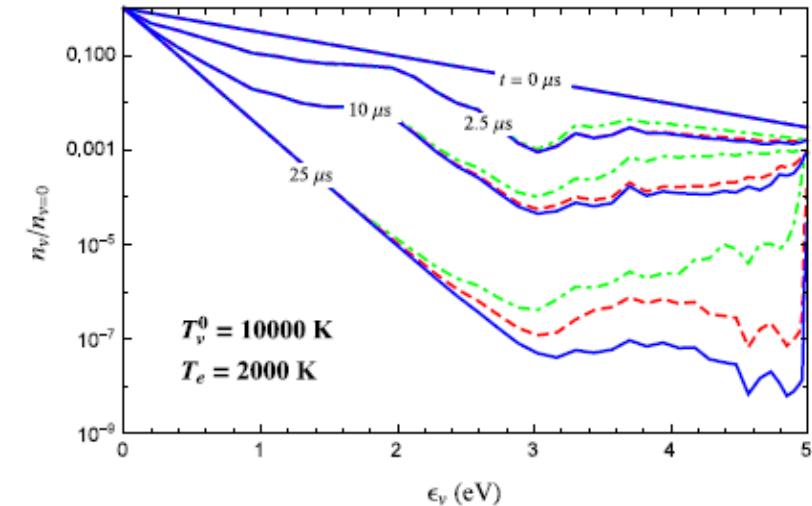


## Time evolution of non-equilibrium vibrational distribution function:

Equilibrium distribution



Non-equilibrium distribution



Vibrational relaxation time:

