# (CTAMOP, Queen's University of Belfast)

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### **Overview of talk**

- 1. Brief reminder of the expt/theory and the capabilities of R-matrix theory and other theory results within the literature, our experimental collaborators and the interface of our results with ADAS.
- 2. Development of the code base to meet the challenge of heavy complex species
- 3. Electron-impact excitation of W I, WII
- 4. Electron-impact ionisation of W I
- 5. Uncertainty quantification work progresses

We validate our theoretical synthetic spectra against ongoing spectral measurements at CTH(Auburn University,USA) and DIID (General Atomics, CA, USA)

- Tungsten employed at JET, ITER, DIII-D and
- (CTH -Compact Toroidal Hybrid), Auburn University)
- Tungsten has favourable physical properties such as high thermal conductivity.

#### CTH (Auburn University)





#### **R-matrix/R-matrix with Pseudostates (RMPS) review**



$$\Psi_k(x_1 \dots x_{N+1}) = A \sum_{ij} c_{ijk} \bar{\Phi}_i(x_1 \dots x_N, \hat{r}_{N+1} \sigma_{N+1}) u_{ij}(r_{N+1}) + \sum_j d_{jk} \phi_j(x_1 \dots x_{N+1})$$

### Capabilities

- Most first order electron-impact driven processes connorb.freeshell.org (login and password available on request)
   Electron-impact excitation
   Electron-impact ionisation
   Electron-impact recombination (DR/radiative)
- + photoionisation , photon-excitation (opacity)
- The codes should cover most of the periodic table, and there are LS coupling (non-relativistic), Breit-Pauli (semi-relativistic) and Dirac R-matrix suites of codes. The results are stored in ADAS(O'Mullane), CLOUDY(G.Ferland), Chianti(Del Zanna) formats

### Photoionisation/photo-excitation

Traditionally, we compared our results against astronomical observation and laboratory measurement. We still do, either remaining observations from the ALS (Advanced Light Source, CA,US) or the SOLEIL experiment (France)



Theory can aid by suggesting wave length windows and distinct isolated diagnostic lines



FIG. 6. Measured spectrum from the CTH plasma (solid blue line), compared with theoretical results. The solid black sticks show the PEC coefficients for the Mo I transitions, while the dashed red curve shows a theoretical spectrum based upon Gaussian convolved PEC data. A FWHM for the Gaussian convolution of 0.15 nm was used, based upon the instrument resolution, and the PECs are shown for an electron temperature of 6 eV and an electron density of  $1 \times 10^{12}$  cm<sup>-3</sup>.

#### **Electron-impact excitation**

R-matrix strength is near neutral open shell systems such as Fe II (3d^4,4s^2) (Rosetta Stone), which has a long history ....

Smyth et al, Monthly Notices of the Royal Astronomical Society. 483, 1, p. 654-663 2019





Various Calculations for the 1-2 transition in Fe II (^6D groundstate) J=9/2-7/2)

### **Stellar Opacities**

High performance computing + scripting = comprehensive data sets (bound-bound, bound-free, free-free transitions)



## All the R-matrix codes, but in particular the Dirac R-matrix codes required major revision.

- Tungsten excitation/ionisation for many ion stages involves open d and shell systems, which requires a target description of several hundred of thousand levels.
- 2. From the scattering perspective (whether excitation or ionisation) involves thousands of scattering channels. Unlike perturbative methods these channels are are all coupled.
- Extensive work (in terms of multi-level MPI) is required if we are to build Hamiltonian matrices in excess of 250K by 250 K in a finite period of time.
- 4. Of particular note is the inclusion of GPU (Graphical Processing Units), that assist greatly with dense matrix multiplies

You have mentioned 10,000 channels and matrices exceeding 100 K by 100 K, but does not the R-matrix have to be calculated for every energy ? 10,000\*10,000\*100,000= 10^13 operations ..... and modern CPUs only are of the order 10^9 operations per sec. Do you wait an hour per energy point ? No fortunately, we can employ GPUs (Graphical Processing Units) for the dense matrix multiplies



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 top - 09:11:42 up 180 days, 20:47, 2 users, load average: 12.31, 11.15, 6.66

 Tasks: 790 total, 14 running, 771 sleeping, 1 stopped, 4 zombie

 %Cpu(s): 17.8 us, 1.2 sy, 0.0 ni, 80.9 id, 0.0 wa, 0.0 hi, 0.1 si, 0.0 st

 KiB Mem : 13191987+total, 4994796 free, 33108388 used, 93816688 buff/cache

 KiB Swap: 67108860 total, 66708020 free, 400840 used. 97612336 avail Mem

PID	USER	PR	NI	VIRT	RES	SHR	S	%CPU	%MEM	TIME+	COMMAND
44564	3049992	20	0	18.325g	1.460g	125464	R	100.3	1.2	12:15.15	pstgb blas v8.g
44566	3049992	20	0	19.117g	2.355g	125576	R	100.3	1.9	12:15.64	pstgb blas v8.g
44569	3049992	20	0	20.493g	3.355g	125688	R	100.3	2.7	12:15.70	pstgb blas v8.g
44570	3049992	20	0	20.492g	3.620g	125476	R	100.3	2.9	12:15.71	pstgb blas v8.g
44571	3049992	20	0	20.661g	3.766g	125472	R	100.3	3.0	12:15.63	pstgb_blas_v8.g
44572	3049992	20	0	21.962g	4.787g	125684	R	100.3	3.8	12:15.75	pstgb_blas_v8.g
44563	3049992	20	0	17.970g	1.264g	125564	R	100.0	1.0	12:15.43	pstgb_blas_v8.g
44565	3049992	20	0	19.118g	2.356g	125520	R	100.0	1.9	12:15.62	pstgb_blas_v8.g
44567	3049992	20	0	20.014g	3.197g	125752	R	100.0	2.5	12:15.61	pstgb blas v8.g
44568	3049992	20	Θ	21.082g	4.038g	125756	R	99.3	3.2	12:15.71	pstgb_blas_v8.g
44561	3049992	20	0	17.150g	492216	125648	R	96.1	0.4	12:11.47	pstgb_blas_v8.g
44562	3049992	20	0	17.150g	545540	125640	R	95.1	0.4	12:11.79	pstgb_blas_v8.g
46186	3049992	20	0	37360	4356	2988	R	2.0	0.0	0:02.94	top
46837	3049992	20	Θ	12772	2828	2228	R	1.6	0.0	0:01.43	watch
8	root	20	Θ	0	0	0	S	0.3	0.0	36:39.64	rcu_sched
34128	root	20	Θ	Θ	Θ	0	S	0.3	0.0	0:00.27	kworker/30:0
43669	3049992	20	Θ	102240	5020	3888	S	0.3	0.0	0:00.25	sshd
46509	3049992	20	Θ	102140	3352	2304	S	0.3	0.0	0:00.09	sshd
56341	root	20	Θ	0	0	0	S	0.3	0.0	0:18.05	kworker/0:1
1	root	20	0	57400	7156	5376	S	0.0	0.0	1:22.58	systemd
2	root	20	0	0	0	0	S	0.0	0.0	0:06.66	kthreadd
3	root	20	0	0	0	0	S	0.0	0.0	0:17.29	ksoftirqd/0
9	root	20	0	0	0	0	S	0.0	0.0	0:00.00	rcu_bh
10	root	rt	Θ	Θ	0	Θ	S	0.0	0.0	0:13.28	migration/0
11	root	Θ	-20	Θ	Θ	Θ	S	0.0	0.0	0:00.00	lru-add-drain
12	root	rt	Θ	Θ	Θ	0	S	0.0	0.0	0:23.99	watchdog/0
13	root	20	Θ	Θ	0	0	S	0.0	0.0	0:00.00	cpuhp/0
14	root	20	0	0	0	0	S	0.0	0.0	0:00.00	cpuhp/1
15	root	rt	0	0	0	0	S	0.0	0.0	0:22.50	watchdog/1
16	root	rt	0	0	0	0	S	0.0	0.0	0:11.20	migration/1
17	root	20	0	0	0	0	S	0.0	0.0	0:13.35	ksoftirqd/1
19	root	Θ	-20	0	Θ	0	S	0.0	0.0	0:00.00	kworker/1:0H
20	root	20	Θ	Θ	Θ	Θ	S	0.0	0.0	0:00.00	cpuhp/2
21	root	rt	Θ	Θ	Θ	Θ	S	0.0	0.0	0:21.95	watchdog/2
22	root	rt	0	Θ	Θ	Θ	S	0.0	0.0	0:11.53	migration/2
23	root	20	0	Θ	Θ	Θ	S	0.0	0.0	0:07.52	ksoftirqd/2
25	root	0	-20	0	Θ	0	S	0.0	0.0	0:00.00	kworker/2:0H

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GPU Fan	Name Temp Perf	Persis Pwr:Us	tence-M  age/Cap	Bus-Id	Disp Memory-Usa	o.A   age	Volatile GPU-Util	Uncorr. ECC Compute M.	+
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Proce GPU	esses: PID	Туре	Process	name				GPU Memory Usage	+
0	44561	С	./pstgb	blas_v8	.gpu.x			291MiB	
0	44562	C	./pstgb	blas_v8	.gpu.x			291MiB	
0	44503	C	./pstgb	blac v8	.gpu.x			291M1B	
0	44565	c	/pstgb	blas v8	.gpu.x			291MiB	
0	44566	č	./pstgb	blas v8	.apu.x			291MiB	
0	44567	C	./pstgb	blas v8	.qpu.x			291MiB	
0	44568	С	./pstgb	blas_v8	.gpu.x			291MiB	
Θ	44569	С	./pstgb	blas_v8	.gpu.x			291MiB	
Θ	44570	C	./pstgb	blas_v8	.gpu.x			291MiB	
0	44571	С	./pstgb	blas_v8	.gpu.x			291MiB	
Θ	44572	С	./pstgb	blas_v8	.gpu.x			1635MiB	

... I will talk about R-matrix results, but I'm aware of other approaches Duck-Hee Kwon (BEB), M S Pindzola (TDCC: configuration-average), Murakami (DWA: Cowan & Hullac)

### Neutral Tungsten Excitation/Ionization

### why tungsten ?

#### The merits of various wall-facing materials, from carbon to tungsten

- Allowable impurity concentration lower for high-Z materials
  - High-Z materials radiate much more than previously used materials
  - Radiation significant enough to denigrate plasma performance
    - Concentration needs to be less than ~1E-4 (Putterich)
  - Need to accurately quantify and minimize erosion of wall



#### Impurity influx diagnostics using SXB coefficients

The intensity of a spectral line can be related to its influx rate [Behringer PPCF 31 2059 (1989)] . However it must be corrected for the fact that some of the impurity has already ionized

 The number of 'ionizations per photon' (or SXB) is directly proportional to the impurity influx ( $\Gamma$ ).

$$\Gamma = \int_{0}^{\infty} N_{e} S^{z \to z+1} N^{z} dx$$

$$\Gamma = \int_{0}^{\infty} N_{e} \frac{S^{z \to z+1}}{A_{i \to j} \frac{N_{i}}{N^{z}}} (A_{i \to j} \frac{N_{i}}{N^{z}}) N^{z} dx = \int_{0}^{\infty} N_{e} SXB_{i \to j}^{z} (A_{i \to j} \frac{N_{i}}{N^{z}}) N^{z} dx$$
Effective ionisation rate (includes ground and excited state ionisation, and shall prove troublesome )
$$SXB_{i-j}^{z} = \frac{S^{z \to z+1} (Ne, Te)}{A_{i \to j} \frac{N_{i}}{N_{z}} (Ne, Te)}$$

prove

### Neutral Tungsten

### **Atomic Structure**

- Large scale structure calculations carried out by Mons group (Palmeri/Quinet) using Cowan code (i.e. HFR Hartree Fock Relativistic)
- We have employed (GRASP0): MCDF approach, but tungsten is not perfectly known

TABLE I. Fine-structure energies of W I, in Rydbergs, obtained from the GRASP<sup>0</sup> model (relative to the ground state) compared to the experimental values compiled by Kramida and Shirai [31]. Absolute energy differences are given in the final column.

No	Level	Expt [31]	GRASP <sup>0</sup>	$ \Delta E $
1	$5d^46s^2 {}^5D_0$	0.00000	0.00000	0.00000
2	$5d^46s^2 {}^5D_1$	0.01522	0.00936	0.00586
3	$5d^{5}(^{6}S)6s^{7}S_{3}$	0.02689	0.02983	0.00294
4	$5d^46s^2 {}^5D_2$	0.03030	0.02152	0.00878
5	$5d^46s^2 {}^5D_3$	0.04401	0.03477	0.00924
6	$5d^46s^2 {}^5D_4$	0.05667	0.04876	0.00791
7	$5d^46s^2 {}^3P_0$	0.08683	0.10237	0.01555
8	$5d^46s^2 {}^3H_4$	0.11083	0.13697	0.02614
9	$5d^46s^2 {}^3P_1$	0.12126	0.13705	0.01579
10	$5d^46s^2  {}^3G_3$	0.12164	0.14721	0.02577
11	$5d^46s^2 {}^3F_2$	0.12555	0.15237	0.02682
12	$5d^46s^2 \ ^3D_2$	0.13647	0.16166	0.02519
13	$5d^46s^2 {}^3H_5$	0.13733	0.16179	0.02446
14	$5d^46s^2 {}^3D_3$	0.14088	0.17371	0.03283
15	$5d^46s^2  {}^3G_4$	0.14973	0.17926	0.02953
16	$5d^46s^2 {}^3H_6$	0.15499	0.17959	0.02460
17	$5d^46s^2 {}^3F_4$	0.15589	0.17179	0.01590
18	$5d^46s^2 {}^3F_3$	0.16131	0.18253	0.02122
19	$5d^46s(^6D)6p\ ^7F_0^o$	0.17669	0.15519	0.02150
20	$5d^46s(^6D)6p\ ^7F_1^o$	0.18284	0.16060	0.02224
21	$5d^46s(^6D)6p^{-7}F_2^o$	0.19546	0.17048	0.02498
22	$5d^46s(^6D)6p^7D_1^o$	0.19550	0.17862	0.01689
23	$5d^46s(^6D)6p\ ^7F_3^o$	0.21002	0.18382	0.02620
24	$5d^46s(^6D)6p\ ^7D_2^o$	0.21838	0.19354	0.02484



FIG. 1. Energy level spectrum of neutral tungsten with each horizontal line representing an observed fine-structure level. (a) Even parity levels with a configuration and term classification; (b) unclassified even levels; (c) classified odd levels; (d) unclassified odd levels.

### Electron-impact excitation of W I/II

#### Neutral tungsten (adf04-excitation only) exists

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#### Dirac *R*-matrix calculations for the electron-impact excitation of neutral tungsten providing noninvasive diagnostics for magnetic confinement fusion

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Neutral tungsten is the primary candidate as a wall material in the divertor region of the International Thermonuclear Experimental Reactor (ITER). The efficient operation of ITER depends heavily on precise atomic physics calculations for the determination of reliable erosion diagnostics, helping to characterize the influx of tungsten impurities into the core plasma. The following paper presents detailed calculations of the atomic structure of neutral tungsten using the multiconfigurational Dirac-Fock method, drawing comparisons with experimental measurements where available, and includes a critical assessment of existing atomic structure data. We investigate the electron-impact excitation of neutral tungsten using the Dirac *R*-matrix method, and by employing collisional-radiative models, we benchmark our results with recent Compact Toroidal Hybrid measurements. The resulting comparisons highlight alternative diagnostic lines to the widely used 400.88-nm line.

DOI: 10.1103/PhysRevA.97.052705

#### Representative collision strengths for W I using DARC code

400.88nm 488.69nm Collision Strength Collision Strength Incident electron energy (eV) Incident electron energy (eV) 2.5 0.6 498.26nm 522.47nm Collision Strength Collision Strength 0.5 0.4 1.5 0.3 0.2 0.5 0.1 Incident electron energy (eV) Incident electron energy (eV)

FIG. 2. Plot showing collision strengths for the  $5d^46s6p \ ^7P_4^o \rightarrow 5d^56s \ ^7S_3$  (400.88 nm),  $5d^46s6p \ ^7F_5^o \rightarrow 5d^46s^2 \ ^5D_4$  (488.69 nm),  $5d^46s6p \ ^7F_1^o \rightarrow 5d^46s^2 \ ^5D_0$  (498.26 nm), and  $5d^46s6p \ ^7D_2^o \rightarrow 5d^46s^2 \ ^5D_3$  (522.47 nm) transitions from the present *R*-matrix calculation.

DIRAC R-MATRIX CALCULATIONS FOR THE ...

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#### Overview of CTH measurements for Tungsten

Looking for multiple ion stages of Tungsten within the same wavelength window

- W I 265.65 nm observed to be on the order of the widely used 400.89 line:
  - Atomic calculations using ADAS confirm that W I 265.65 nm is strong for divertor temperatures and densities ~1E19 m<sup>3</sup> ~ 10eV
- Multiple W I lines in the region around 265.65 region:
  - High density of lines in this region motivates higher resolution spectrometer/instrument



Tungsten ground and excited state ionisation (problematic)

A little context for RMPS ionisation

### R-matrix/RMPS : ionisation

We have the capability to calculate electron-impact ionisation (ground & metastable) for light to mid-Z elements. With the availability of Prof Badnell's DRMPS (Dirac R-matrix with Pseudo-States) code, the heavier elements are now feasible.

#### It is the accuracy of the excited states that can prove problematic



#### Total electron-impact ionisation of neutral and singly ionised Tungsten

#### ... the R-matrix results are close to the Distorted Wave results

Plasma and Fusion Research: Regular Articles

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Fig. 1 Total ionization cross sections of W atoms plotted as a function of incident electron energy, solid curve: present DWA results in HULLAC [19], dashed and dotted curves: present DWA results in Cowan formalism with fine-structure and configuration mode; dash-dotted curve: results of [12] and dash-dot-dotted curve: results of [11].



Fig. 3 Total ionization cross sections of W<sup>+</sup> ions plotted as a function of incident electron energy, dash-dot-dotted curve: results of [10]; dash-dotted curve: results of [8]; solid circles and hollow triangles: measurements [14] and [13]; other curves are the same as Fig. 1.

#### However, these are not the ionisation cross sections we should be concerned about (metastables !)

We may have to rely on the ECIP method to account for the excited state ionisation



(slide kindly provided by Connor Favreau)

There may be a linear scaling factor based upon the RMPS results for the ECIP

8 6 ECIP Scale Factor  $# 5d^4 6s 6p$  $5d^3 6s^2 6p$  $5d^5 6d$ ۸ \* ⋇  $5d^4$  6s 6d × 2  $5d^6$  $5d^5 6s$ 0 0.5 0.2 0.1 0.3 0.4 Ionization Potential (Ryd)

ECIP Scale Factor vs. Ionization Potential

### Uncertainty quantification

(progress on light fusion related elements, heavier elements require substantial resources)

#### **Uncertainty in Theoretical** Calculations ICFT script

#### **Baseline Studies**



### Thank-you for your attention