

Collisional-Radiative modeling of the Tungsten spectrum from the **EBIT and EAST Tokamak**

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1. Motivation & Background







EBIT(Rev. Sci. Instrum 85, 093301)



- W (Z=74) good candidate of the divertor:
- ♪ Low tritium retention
- W Impurities:



ITER(www.iter.org)

EAST (www.ipp.cas.cn)

3.Result & Dissusion: EUV spectrum of W¹³⁺-W¹⁵⁺ ions in the EBIT

Transition wavelength and rate of W^{13+} ions								
Key	Lower	Upper	λ	λ^{c}_{exp}	A(10 ¹¹ s ⁻¹)			
	$[(4f^{5}_{5/2}4f^{7}_{7/2})_{6}5p_{1/2}]_{13/2}$	$[(4f^{5}_{5/2}4f^{7}_{7/2})_{6}5d_{3/2}]_{15/2}$	18.18		1.26			
	$[(4f^{6}_{7/2})_{6}5p_{3/2}]_{15/2}$	$[(4f^{6}_{7/2})_{6}5d_{5/2}]_{17/2}$	21.03		1.52			
	$[(4f^{5}_{5/2}4f^{7}_{7/2})_{5}5p_{3/2}]_{13/2}$	$[(4f^{5}_{5/2}4f^{7}_{7/2})_{5}5d_{5/2}]_{15/2}$	21.05		1.49			
	$[(4f^4{}_{5/2})_45p_{3/2}]_{11/2}$	$[(4f^4_{7/2})_45d_{5/2}]_{13/2}$	21.07		1.41			
	$[(4f^{5}_{5/2}4f^{7}_{7/2})_{5}5p_{3/2}]_{15/2}$	$[(4f^{5}_{5/2}4f^{7}_{7/2})_{6}5d_{5/2}]_{17/2}$	21.13		1.50			
1	$[(4f^{5}_{5/2})_{5/2}5s^{2}]_{5/2}$	$[((4f^{5}_{5/2})_{5/2}5s_{1/2})_{3}5p_{3/2}]_{5/2}$	24.09 23.87 ^a 24.00 ^c		0.62 0.63 ^a			
2	$[(4f^{7}_{7/2})_{7/2}5s^{2}]_{7/2}$	$[((4f^{7}_{7/2})_{7/2}5s_{1/2})_{4}5p_{3/2}]_{7/2}$	24.17 23.95 ^a 24.06 ^c	24.32	0.55 0.54ª			
3	$[(4f^{5}_{5/2})_{5/2}5s^{2}]_{5/2}$	$[((4f^{5}_{5/2})_{5/2}5s_{1/2})_{2}5p_{3/2}]_{7/2}$	24.61 24.41 ^a 24.57 ^c	24.77	0.53 0.51 ^a			
4	$[(4f^{7}_{7/2})_{7/2}5s^{2}]_{7/2}$	$[((4f^{7}_{7/2})_{7/2}5s_{1/2})_{3}5p_{3/2}]_{9/2}$	24.69 24.53° 24.64°	24.83	0.55 0.61 ^a			
5	$[(4f^{7}_{7/2})_{7/2}5s^{2}]_{7/2}$	$[((4f^{7}_{7/2})_{7/2}5s_{1/2})_{4}5p_{3/2}]_{5/2}$	24.76 24.71° 24.70°	24.91	0.57 0.54ª			
6	$[(4f^{5}_{5/2})_{5/2}5s^{2}]_{5/2}$	$[((4f^{5}_{5/2})_{5/2}5s_{1/2})_{3}5p_{3/2}]_{3/2}$	24.93		0.58			

The spectrum of W^{13+} ions by CRM (a) Transition Rate 5p - 5s 5d - 5p (b) CRM $E_e = 280 \text{eV} n_e = 10^{10} \text{cm}^{-3}$







	Transition way	elength and rate of V	V^{15+}	ions	
Key	Lower	Upper	λ	A(10 ⁻¹⁰ s ⁻¹) Int	
1	$[(4f^{5}_{7/2})_{15/2}5s^{2}]_{15/2}$	$[((4f^{s}_{7/2})_{15/2}5s_{1/2})_{8}5p_{3/2}]_{15/2}$	22.48	5.89	2.36
2	$[(4f^{5}_{7/2})_{11/2}5s^{2}]_{11/2}$	$[((4f^{5}_{7/2})_{11/2}5s_{1/2})_{6}5p_{3/2}]_{11/2}$	22.54	5.59	1.13
	$[(4f^{5}_{5/2}4f^{6}_{7/2})_{13/2}5s^{2}]_{13/2}$	$[((4f^{s}_{5/2}4f^{s}_{7/2})_{13/2}5s_{1/2})_{7}5p_{3/2}]_{13/2}$	22.55	4.26	1.09
3	$[(4f^{5}_{7/2})_{15/2}5s^{2}]_{15/2}$	$[((4f^{5}_{7/2})_{15/2}5s_{1/2})_{8}5p_{3/2}]_{13/2}$	22.66	6.20	2.21
4	$[(4f^{5}_{7/2})_{9/2}5s^{2}]_{9/2}$	$[((4f^{5}_{7/2})_{9/2}5s_{1/2})_{4}5p_{3/2}]_{11/2}$	22.70	6.74	1.38
	$[((4f^4{}_{5/2})_44f^7{}_{7/2})_{7/2}5s^2]_{11/2}$	$[((4f^{4}_{5/2}4f^{7}_{7/2})_{11/2}5s_{1/2})_{5}5p_{3/2}]_{13/2}$	22.70	6.83	1.14
	$[(4f^{5}_{7/2})_{11/2}5s^{2}]_{11/2}$	$[((4f^{s}_{7/2})_{11/2}5s_{1/2})_{5}5p_{3/2}]_{13/2}$	22.70	5.13	1.25
5	$[(4f^{5}_{5/2}4f^{6}_{7/2})_{13/2}5s^{2}]_{13/2}$	$[((4f^{s}_{5/2}4f^{6}_{7/2})_{13/2}5s_{1/2})_{6}5p_{3/2}]_{15/2}$	22.77	5.52	1.67
	$[(4f^{5}_{7/2})_{15/2}5s^{2}]_{15/2}$	$[((4f^{s}_{7/2})_{15/2}5s_{1/2})_{7}5p_{3/2}]_{17/2}$	22.78	7.63	3.61
6	$[(4f^{5}_{5/2}4f6_{7/2})_{6}5s^{2}]_{15/2}$	$[((4f^{5}_{5/2}4f^{6}_{7/2})_{15/2}5s_{1/2})_{7}5p_{3/2}]_{17/2}$	22.92	6.99	1.03



E1 transition wavelength and rate of W^{45+} ions

 $A(s^{-1})$ $A_{other}(s^{-1})$ Pop. Int. Type

2.28(11)ⁱ 1.79(-12) 0.48 E1

4.64(10)ⁱ 1.06(-9) 56.88

2. Method

Multi-configruation Dirac-Fock Hamiltonian.

$$\hat{H}_{DC} = \sum_{i=1}^{N} \hat{H}_i + \sum_{i=1}^{N-1} \sum_{j=i+1}^{N} \frac{1}{r_{ij}}$$

Radiative Transition Rates.

$$A_{fi} = \left| \left\langle \psi_f \left\| O_M^L \right\| \psi_i \right\rangle \right|^2$$

Collisional-Radiative Modeling. $\frac{dn(p)}{dt} = \sum_{q>p} F(q,p)n_e n(q) + \sum_{p<q} \left[C(q,p)n_e\right]$ $+A(q,p)]n(q) - \left[\sum_{q>p} C(p,q)n_e + \sum_{q>q} F(p,q)n_e + \sum_{p>q} A(p,q)\right] \times n(p)$

6. Conuslion

1. The 5p-5s transition spectra of $W^{13+}-W^{15+}$ ions have

4. Result & Dissusion: EUV spectrum of W⁴³⁺**-W**⁴⁵⁺ **ions in the EAST**

	E1 & M1 transition wavelength and rate of W^{43+} ions									
Кеу	Lower	Upper	λ(Å)	$\lambda_{\text{EXPT.}}(\text{\AA})$	$\lambda_{other}({\rm \AA})$	A(s ⁻¹)	A _{other}	.(s ⁻¹)	Int.	Туре
	4s ² 4p ² P _{1/2}	$4s4p^2 {}^2P_{3/2}$	40.46		40.44 ⁱ 40.2	27 ^j 6.80(9)	6.38(9) ⁱ	5.48(9) ^j	1.03(-3)	E1
	$4s^24p\ ^2P_{1/2}$	$4s4p^2\ ^2S_{1/2}$	40.98		40.92 ⁱ 40.5	81 ^j 5.43(9)	5.91(9) ⁱ	6.28(9) ^j	6.76(-4)	E1
1	4s ² 4p ² P _{1/2}	4s ² 4d ² D _{3/2}	47.56	$47.90^{g} \ 47.69^{i} 47.91^{j}$	47.63 ^h 47.	71 ^j 1.25(12)			50.96	E1
2	$4s^24p\ ^2P_{3/2}$	$4s4p^2 {}^2P_{3/2}$	59.46		59.50 ⁱ 59.	01 ^j 1.06(12)	1.05((12) ⁱ	1.12(12) ^j	0.16	E1
3	4s ² 4p ² P _{1/2}	$4s4p^2 {}^2P_{1/2}$	60.57	$60.61^g 60.61^i 60.63^j$	59.87 ^h 60.58 ⁱ 6	0.20 ^j 7.06(11)	6.79(11) ⁱ	7.47(11) ^j	28.96	E1
	$4s^24p\ ^2P_{3/2}$	$4s4p^2 {}^2S_{1/2}$	60.59		60.56 ⁱ 60.	27 ^j 4.99(11)	4.91(11) ⁱ	5.25(11) ^j	6.21(-2)	E1
4	4s ² 4p ² P _{1/2}	4s4p ² ² D _{3/2}	61.36	61.33^{g} $61.29^{i} 61.35^{j}$	60.82^{h} 61.32^{i} 60.82^{h}	51.11 ^j 3.61(11)	3.63(11) ⁱ	3.62(11) ^j	31.32	E1
5	$4s^24p\ ^2P_{3/2}$	$4s4p^2 \ ^4P_{5/2}$	64.03		63.97 ^h 64.03 ⁱ 6	3.95 ^j 5.58(11)	5.44(11) ⁱ	5.48 (11) ^j	0.20	E1
	$4s^24p\ ^2P_{1/2}$	$4s4p^2 \ ^4P_{3/2}$	68.40		68.36 ^h 68.24 ⁱ 6	8.21 ^j 2.78(9)	2.77(9) ⁱ	2.87(9) ^j	1.09	E1
6	$4s^24p\ ^2P_{_{3/2}}$	4s ² 4d ² D _{5/2}	70.28	h by RELAC 0.12%	70.66 ^h 70.	61 ^j 6.72(10)	9.23	(10) ^j	0.55	E1
7	$4s^24p{}^2P_{3/2}$	$4s4p^2 {}^2P_{1/2}$	116.10	j by MCDF 0.50%, 6.83%	116.50 ⁱ 114	.93 ^j 2.67(10)	2.64(10) ⁱ	2.82(10) ^j	1.10	E1
8	$4s^24p\ ^2P_{3/2}$	$4s4p^2 \ ^2D_{3/2}$	119.06		117.56 ^h 119.04 ⁱ 1	18.28 ^j 1.91(10)	1.91(10) ⁱ	2.01(10) ^j	1.66	E1
m	$4s^24p \ ^2P_{1/2}$	$4s^24p \ ^2P_{3/2}$	126.60	126.29 ^h 126.39 ^j	126.01 ^h 126.23 ⁱ	126.43 ^j 4.31(6)	4.36(6) ⁱ	4.33(6) ^j	13.33	M1
9	$4s^24p \ ^2P_{1/2}$	$4s4p^2 \ ^4P_{1/2}$	128.14	128.17 ^h 128.24 ^j	127.06 ^h 128.17 ⁱ	127.30 ^j 2.96(10)	2.96(10) ⁱ	2.90(10) ^j	16.08	E1
10	4s ² 4p ² P _{3/2}	4s4p ² ² D _{5/2}	134.85	134.81° 135.34 ^j	134.55 ^h 13 ^c	4.20 ^j 1.38(10)	1.38(10) ⁱ	1.41 (10) ^j	2.46	E1



]	E1 &	M1 t	rans	ition wave	ele	ngth	and ra	te of	W^{44-}	+ion	S
ey	Lower	Upper	$\lambda(\text{\AA})$	$\lambda_{\text{EXPT.}}(\text{\AA})$	λ.	other(Å)	A(s ⁻¹)	Aother(s ⁻¹)	Pop.	Int.	Туре
	4s4p ³ P ₁	4s4d ¹ D ₂	44.49	44.52 ^g	44.38	3 ^h 44.49 ⁱ	5.43 (10)	5.53(10) ⁱ	2.57(-11)	1.37	E1
2	$4s^{1}4p^{-3}P_{0}$	4s4d ³ D ₁	47.86		4	47.81 ⁱ	6.02 (11)	6.04(11) ⁱ	8.60(-13)	0.40	E1
	4s4p ³ P ₁	4s4d ³ D ₂	48.54	48.61 ^d	4	8.41 ^h	1.01 (12)	1.02(12) ⁱ	2.22(-12)	2.73	E1
ļ	$4s4p$ $^{3}P_{1}$	4s4d ³ D ₁	49.21		4	19.19 ⁱ	3.18 (11)	3.19(11) ⁱ	8.60(-13)	0.20	E1
5	$4s^2$ 1S_0	4s4p ¹ P ₁	60.90	$\begin{array}{rrr} 60.93^{d} & 60.87^{f} \\ & 60.93^{g} \end{array}$	60.73	^{3g} 60.66 ^h	6.59 (11)	6.85(11) ⁱ	2.23(-10)	1.94(2)	E1
5	$4s4p$ $^{3}P_{2}$	4s4d ¹ D ₂	66.66	66.93 ^d	66.40	5 ^h 66.66 ⁱ	2.00 (11)	1.99(11) ⁱ	2.57(-11)	5.04	E1
7	$4s4p$ $^{3}P_{2}$	4s4d ³ D ₃	68.77		e	58.76 ⁱ	3.77 (11)	3.78(11) ⁱ	1.94(-11)	0.17	E1
	$4s4p \ ^1P_1$	4s4d ¹ D ₂	73.66		73.43	3 ^h 73.86 ⁱ	1.04 (11)	1.06(11) ⁱ	2.57(-11)	2.63	E1
	$4s4p$ $^{3}P_{2}$	4s4d ³ D ₂	76.17			76.15 ⁱ	1.92 (10)	1.94(10) ⁱ	2.22(-12)	0.05	E1
	$4s4p \ ^3P_2$	4s4d ³ D ₁	77.83	i by MCDF 0.13%, 1.3	%	77.82 ⁱ	7.08 (9)	7.12(9) ⁱ	8.60(-13)	0.01	E1
	$4s4p$ $^{1}P_{1}$	4s4d ³ D ₂	85.45			85.69 ⁱ	2.94 (8)	2.87(8) ⁱ	2.22(-12)	7.91(-4)	E1
)	$4s^2 {}^1S_0$	4s4p ³ P ₁	132.97	132.88° 132.75 ^f 132.87 ^g	132.0	7 ^h 132.60 ⁱ	1.73 (10)	1.78(10) ⁱ	3.35(-9)	57.88	E1
1	4s4p ³ P ₁	4s4p ³ P ₂	133.80	134.80 ^e	133.6	0 ^h 133.45 ^e	4.19(6)		1.28(-6)	5.35	M1





5 4d ${}^{2}D_{5/2}$ 4f ${}^{2}F_{7/2}$ 74.34

been calculated by the RCI and CRM. The present theoretical results are in good agreement with the experimental results

2. The transition data and spectra of $W^{43+}-W^{45+}$ ions have been calculated by the RCI method and CRM in different plasma conditions. The present theoretical results are in good agreement with the experimental results and previous theoretical values. All the observed transitions of $W^{43+}-W^{45+}$ ions are assigned according to the present calculation.

3. A reasonable CRM has been constructed to simulate and explain the M1 visible spectrum of W^{13+} ion observed in EBIT. The present calculations are in reasonable agreement with the available theoretical and experimental data. For the first time, the corresponding transitions of the 5 measured lines are identified.

7. References

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5.Result & Dissusion: The M1 transitions and visible spectra of W^{13+} ion

\mathbb{N}	M1 transition wavelength and rate of W^{13+} ions								
Key	Upper	Lower	λ(nm)	А	I _{Theo}	$\lambda_{Expt}(nm)$			
k	$[(4f^4{}_{5/2})_45p_{3/2}]_{11/2}$	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{5}5p_{3/2}]_{13/2}$	368.83	266.20					
α	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{3}5p_{1/2}]_{7/2}$	$[(4f^{6}_{7/2})_{4}5p_{1/2}]_{7/2}$	385.03	127.20	$\langle \leq$	0.36%			
m	$[(4f^4{}_{5/2})_25p_{1/2}]_{3/2}$	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{2}5p_{1/2}]_{3/2}$	395.02	196.90					
1	$[((4f^{5}{}_{5/2}){}_{5/2}4f^{7}{}_{7/2}){}_{3}5p{}_{1/2}]_{7/2}$	$[(4f^{6}_{7/2})_{4}5p_{1/2}]_{9/2}$	430.19	74.31	0.18	429.03ª			
β	$[((4f^{5}{}_{5/2})_{5/2}4f^{7}{}_{7/2})_{3}5p_{1/2}]_{5/2}$	$[(4f^{6}_{7/2})_{4}5p_{1/2}]_{7/2}$	449.09	144.10					
2	$[(4f^4{}_{5/2})_45p_{1/2}]_{9/2}$	$[((4f^{5}{}_{5/2}){}_{5/2}4f^{7}{}_{7/2}){}_{5}5p{}_{1/2}]_{11/2}$	458.90	132.90	0.22	459.08 ^b			
3	$[(4f^4{}_{5/2})_45p_{1/2}]_{9/2}$	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{5}5p_{1/2}]_{9/2}$	473.82	27.03	0.04	472.68 ^b			
4	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{5}5p_{1/2}]_{9/2}$	$[(4f^{6}_{7/2})_{6}5p_{1/2}]_{11/2}$	494.26	180.40	0.96	495.16ª			
n	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{5}5p_{3/2}]_{13/2}$	$[(4f^{6}_{7/2})_{6}5p_{3/2}]_{15/2}$	495.00	199.80					
5	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{3}5p_{1/2}]_{5/2}$	$[(4f^{6}_{7/2})_{4}5p_{1/2}]_{7/2}$	552.27	27.05	0.31	553.81ª			
6	(4f ⁵ _{5/2}) _{5/2}	$(4f^{7}_{7/2})_{7/2}$	558.21	88.38	1.00	560.25 ^a			
γ	$[((4f^{5}_{5/2})_{5/2}4f^{7}_{7/2})_{4}5p_{1/2}]_{9/2}$	$[(4f^{6}_{7/2})_{4}5p_{1/2}]_{9/2}$	577.79	40.39					

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